



Tour de l'IGS 4th Stop: BDS Constellation Spotlight

## **Beidou Coordinate System: Its Realization and Maintenance**

Xiaogong Hu<sup>1</sup> Shanshi Zhou<sup>1</sup> Weijing Qu<sup>1</sup> Na Wei<sup>2</sup>

1. Shanghai Astronomical Observatory, Chinese Academy of Science

2. Wuhan University

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## Background

- Since July, 2020, Beidou Satellite Navigation System (BDS) has provided various PNT services.
- Both BDS services and the compatibility and interoperability with other navigation systems require high accuracy realization and maintenance of BDS coordinate system(BDCS).
- To meet the accuracy requirements, satellite geodesy techniques are used for coordinate estimation of BDS monitoring stations, and alignment to the International Terrestrial Reference Frame (ITRF).





## **1.1 First Realization of BDCS**

- Four joint campaigns with IGS stations. Coordinates of BDS monitor stations are aligned to ITRF2014 with a set of IGS stations.
  - $\checkmark$  1<sup>st</sup>, 2007 ~2009, station-wise surveying.
  - $\checkmark$  2<sup>nd</sup>, December 2011, campaign mode for 15 days.
  - $\checkmark$  3<sup>rd</sup>, April 2014, campaign mode for 15 days.
  - $\checkmark$  4<sup>th</sup>, 2016, regional joint surveying.
- Result: The first realization of BDCS is aligned to ITRF2014 with accuracy better than 1 cm.
  - Ref: F. Wu, BeiDou Coordinate System And Its First Realization , ICG-13, 2018





## 1.2 BDCS Update and Maintenance

#### Strategy:

- Daily network solutions with loose constrain obtained by estimating GNSS satellite orbital parameters and stations coordinates and then aligned to ITRF.
- Updating station coordinates when difference between estimated values and current values exceeding threshold (3 cm, currently)
- Annual maintenance

	Accuracy	Alignment to ITRF
WGS84 ( G1762 )	< 1 cm	ITRF2008
GTRF	< 1 cm	ITRF2014
PZ-90	< 2 cm	ITRF2014
BDCS ( 2019V01 )	< 1 cm	ITRF2014











## 2.1 Data Processing

- Strategy:
- ✓ **Continuous** GNSS tracking data.
- Daily network solutions with loose constrained obtained by estimating GNSS satellite orbital parameters and stations coordinates.
- Aligning to ITRF by minimum constrain IGS station coordinates in ITRF2014.
- > Data:
- pseudo-range and carrier phase ionospheric-free combinations, from 2019.01.01 to 2019.03.31 of more than 120 stations distributed globally (IGS stations and regional stations)

#### BDCS(2019V01)

	BeiDou Coordinate System
<b>Responsible Organization:</b>	China Satellite Navigation Office(CSNO)
Abbreviated Name:	BDCS
Associated TRS:	ITRS
Coverage of Frame:	Global
Type of Frame:	3-Dimensional
Latest Version:	2019V01

#### Brief Description

BDCS is an Earth-centered, Earth-fixed terrestrial reference system. The definition of BDCS is in accordance with the specifications of the International Earth Rotation and Reference System Service(IERS), and its realization is aligned to the latest International Terrestrial Reference System(ITRF). The BDCS(2019V01) is the current solution obtained by adopting more than 100 stations.

#### **Definition of Frame**

Origin:							
Axes:							
Z-	Axis: The d	lirection of t	he IERS Re	ference Pole	(IRP)		
X	Axis: the in	itersection o	of the IERS	Reference M	leridian (IR)	M) and the p	lane passing
th	rough the or	rigin and not	rmal to the 2	Z-Axis.			
Y- co	Axis: toge ordinate sys	ther with Z stem.	-Axis and	X-Axis, cor	nstitutes a i	right-handed	orthogonal
Scale:	The length u	mit is the int	ernational s	ystem of uni	ts(SI) meter.		
Orient: 1984.0	ntion: Given	a by the Bur	eau Internat	ional de l'He	eure (BIH) o	rientation of	
Time E	volution: I	s time evolu	tion in orier	ntation will c	reate no resi	dual global	rotation with
gards to the	emst.						
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offining Par	ystem: Car	The moment	linates(X, Y	, Z)	Ellipsoid and	incidae with	the Earth's
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#### www.beidou.gov.cn





## 2.1 Data Processing

- Data: 2019.0-2019.25 pseudo-range and phase LC from 120+ global stations.
- Processing: precise orbit determination
- ➢ Estimation:
  - > satellite orbital parameters
  - ► ECOM-9 SRP
  - station coordinates
  - > ZTD
  - phase ambiguity
  - satellite and station clock offsets
- Satellite Antenna PCO/PCV: IGS14.atx
- Alignment: minimum constrained IGS core station coordinate in ITRF2014









#### Coordinates time series

### Coordinates differences between BDCS(2019v01) and ITRF2014 solutions



The difference is better than 1cm.





## 2.2 Accuracy

#### Selected stations to assess alignment accuracy



#### Station list

СНРІ	VACS	DAEJ
MAW1	REDU	СНИМ
KOUR	BRUX	ULAB
GUAM	MKEA	URUM
CRO1	KIRU	CKIS
STHL	NAUR	SYDN
KOKV	WROC	DARW
MADR	MGUE	KAT1
CEBR	QUIN	FAA1
EBRE	SANT	PERT
AREQ		

#### **Transformation parameters from BDCS(2019v01) to ITRF2014**

	Trans_x mm	Trans_y mm	Trans_z mm	Rotate_x mas	Rotate_y mas	Rotate_y mas	Scal ppb
Estimation	-0.37	1.12	-0.55	0.01	-0.02	0.05	0.011
Sigma	0.74	0.74	0.74	0.03	0.03	0.04	0.012
3*Sigma	2.22	2.22	2.22	0.09	0.09	0.11	0.037

#### Alignment accuracy: 2 mm











## Methods

- > Several methods are adopted to assess the accuracy of BDCS maintenance
- ✓ 1. Consistency comparison of co-located station coordinates time series
- ✓ 2. Station coordinates repeatability
- ✓ 3. Station velocity comparisons
- ✓ 4. Transformation parameters between BDCS and ITRF2014
- ✓ 5. Broadcast ephemerides and precise orbit comparisons





## **3.1 Co-located stations**

#### Co-located stations coordinates time series



✓ Apparent trend changes in horizontal and vertical components.

✓ Co-located sites coordinate variations show good consistency.





### 3.2 Station coordinates repeatability



E:1.8mm; N: 1.8mm; U: 4.3mm





E: 1.9mm; N: 2.2mm; U: 8.2mm

#### **Repeatability better than 1 cm**





## 3.3 Station velocity



#### **BJFS velocity comparisons**

	N(mm/yr)	E(mm/yr)	U(mm/yr)
BJSH ( shao )	-10.3	28.4	3.1
BJFS ( shao )	-11.8	29.3	4.4
BJFS ( igs )	-11.6	31.7	1.9
BJFS ( ITRF14 )	-10.6	30.6	2.2
BJFS(IGb14)	-10.5	30.7	2.2

#### Velocity field comparisons



#### Velocity difference 2mm/yr (horizontal) and 3mm/yr (vertical)





### 3.4 Transformation between BDCS and ITRF2014



#### Daily solution transformation parameters time series



	Tx/mm	Ty/mm	Tz/mm	Rx/mas	Ry/mas	Rz/mas	Scal/ppb
Mean	-0.78	0.99	0.92	0.01	-0.01	0.03	-0.06
Std	1.25	1.58	1.32	0.08	0.05	0.06	0.04

#### Accuracy consistent with BDCS(2019V01)

#### Maintenance of the BDCS continuous and stabilization





- **Orbit comparison:** transformations between broadcast and precise orbits
- Station coordinates comparison: transformations between station coordinates of PPP using broadcast and precise products
- > Data:
  - BDS-3/GPS/GAL precise orbits of GFZ and broadcast ephemerides
  - 130 globally distributed MGEX stations for PPP processing
  - Time span from 2020.1 to 2020.12
  - PCO values :

BDS3: <u>http://www.beidou.gov.cn;</u> GPS:NGA(2018); GAL:GSC,(2019)







### Translations



#### **Blue/Red: orbit/coordinates comparison**

#### **Correlations between orbit/coor. comparisons**

	DX	DY	DZ
BDS-3	0.14	0.10	0.93
Galileo	0.10	0.20	0.50
GPS	0.28	0.33	0.68

- Annual systematic errors found in ztranslation for BDS-3, showing manufacturer- and orbit-plane-dependent characteristics
- Random errors dominating GPS/GAL
- Results from orbit and coordinate comparisons are at the same level





### Rotations



#### **Correlations between orbit/Coor. comparisons**

	RX	RY	RZ
BDS-3	0.79	0.94	0.91
Galileo	0.55	0.28	0.20
GPS	0.57	0.65	0.54

- Systematic errors in rotations also found in BDS-3 due to increasing errors of EOP predictions within one week, resulting in positioning errors up to 25 cm
- Rotations of GPS/GAL are stable within one week
- Results from orbit and SSC comparisons are also at the same level





### Scale



#### Correlations between orbit/coor. comparisons

	SCL
BDS-3	0.02
Galileo	0.11
GPS	0.05

- No systematic errors in scale found in three systems
- But, negative biases found between orbits and SSC comparisons due to highly correlation between clock offsets and scale factor during PPP











## 4.1 Data Processing

- > Strategy:
- ✓ Continuous BDS data.
- Daily network solutions with loose constrained obtained by estimating BDS satellite orbital parameters and stations coordinates.
- ✓ Aligning to ITRF by minimum constrain IGS station coordinates in ITRF2014.
- > Data:
- ✓ 2019.10.01-2020.03.19, more than 200 global stations, including IGS stations and BDS stations.
- Accuracy evaluation
- ✓ Consistency analysis of BDS station coordinate
- ✓ Transformation parameters





### 4.2 Coordinates Repeatability and Comparisons





E: 5.9mm

N: 4.5mm

U: 12.5mm

Coordinate differences between BDS and GPS

E: 7.0mm N: 4.8mm U:13.8mm



Accuracy of site coordinates using BDS data about 1 cm





## 4.3 Coordinates Time Series

**Time series comparison** 



#### Apparent trend changes in horizontal and vertical components.

Scatter of site coordinate time series larger when using BDS data!

	Tx/mm	Ty/mm	Tz/mm	Rx/mas	Ry/mas	Rz/mas	Scal/ppb
Mean	0.62	0.16	-0.61	0.02	0.00	-0.05	-0.01
Sigma	1.41	1.38	1.23	0.06	0.06	0.05	0.02

Accuracy of BDCS(BDS only) at millimeter level













# Summary

- BDCS in high accuracy alignment with ITRF2014. Although BDS-3 broadcast orbits are constrained only by several regional stations, TRF accessible via BDS-3 broadcast orbits still coincides with ITRF2014 at cm level.
- Nonlinear characteristic evident in BDS station coordinate time series need further modeling.
- Only using BDS data from global tracking stations, coordinates can be estimated accurately and BDCS can be aligned to ITRF at mm level.
- > Joint forces from GNSS community are mostly welcome to improve BDCS.





# THANKS !