

# Next Generation Radiation Pressure Modelling for GNSS Space Vehicles: Grid File Model Tests on GPS IIR

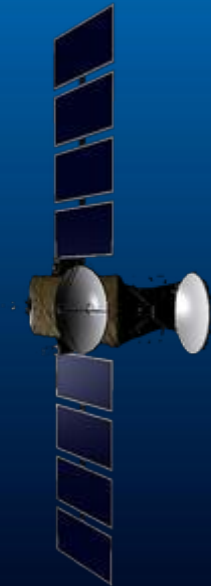
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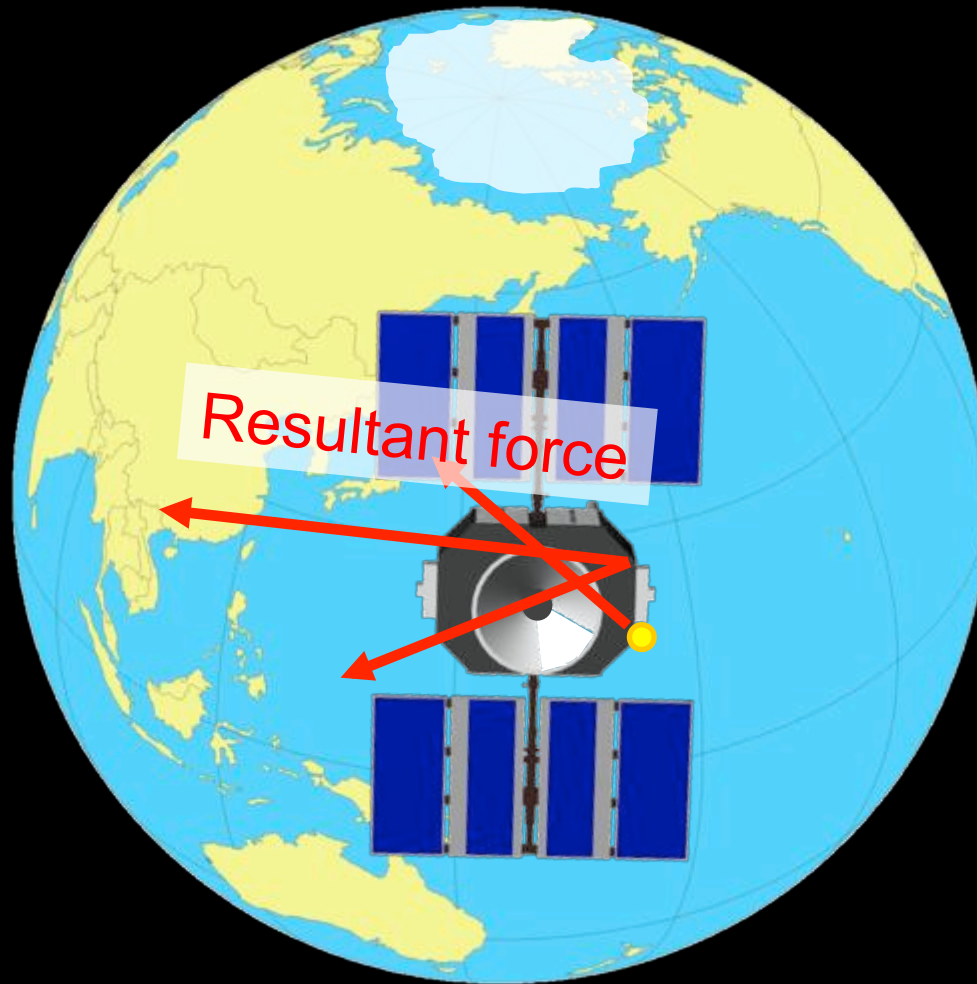
**The Maths.....**

$$E = mc^2$$

**For Photons:**

$$\rho = E/c$$

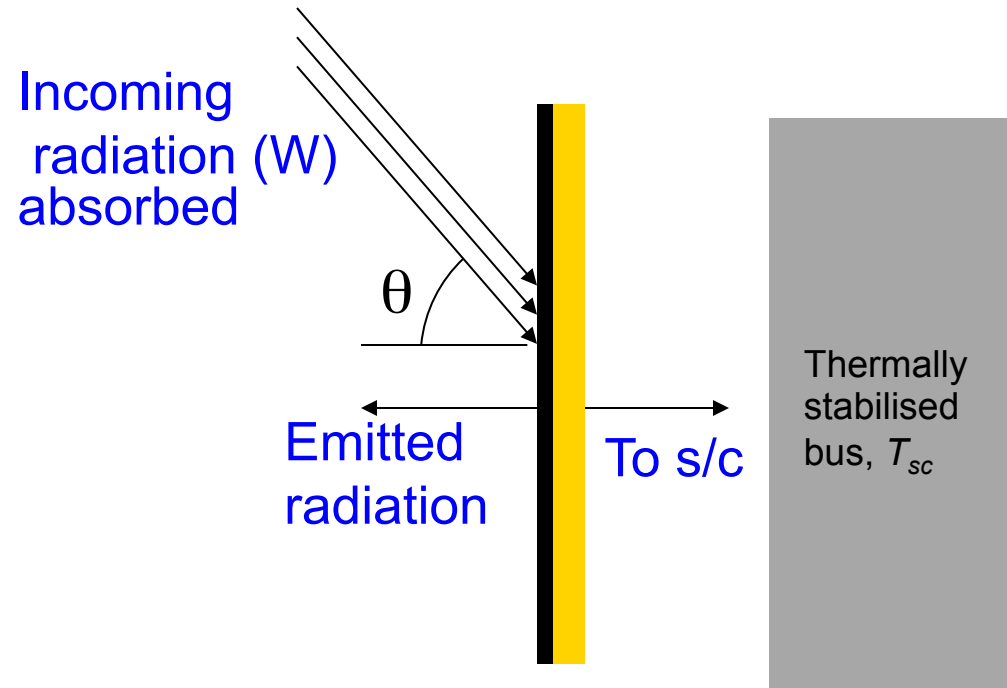
**Momentum = Energy/speed of  
light**



# Multilayer Insulation (MLI)

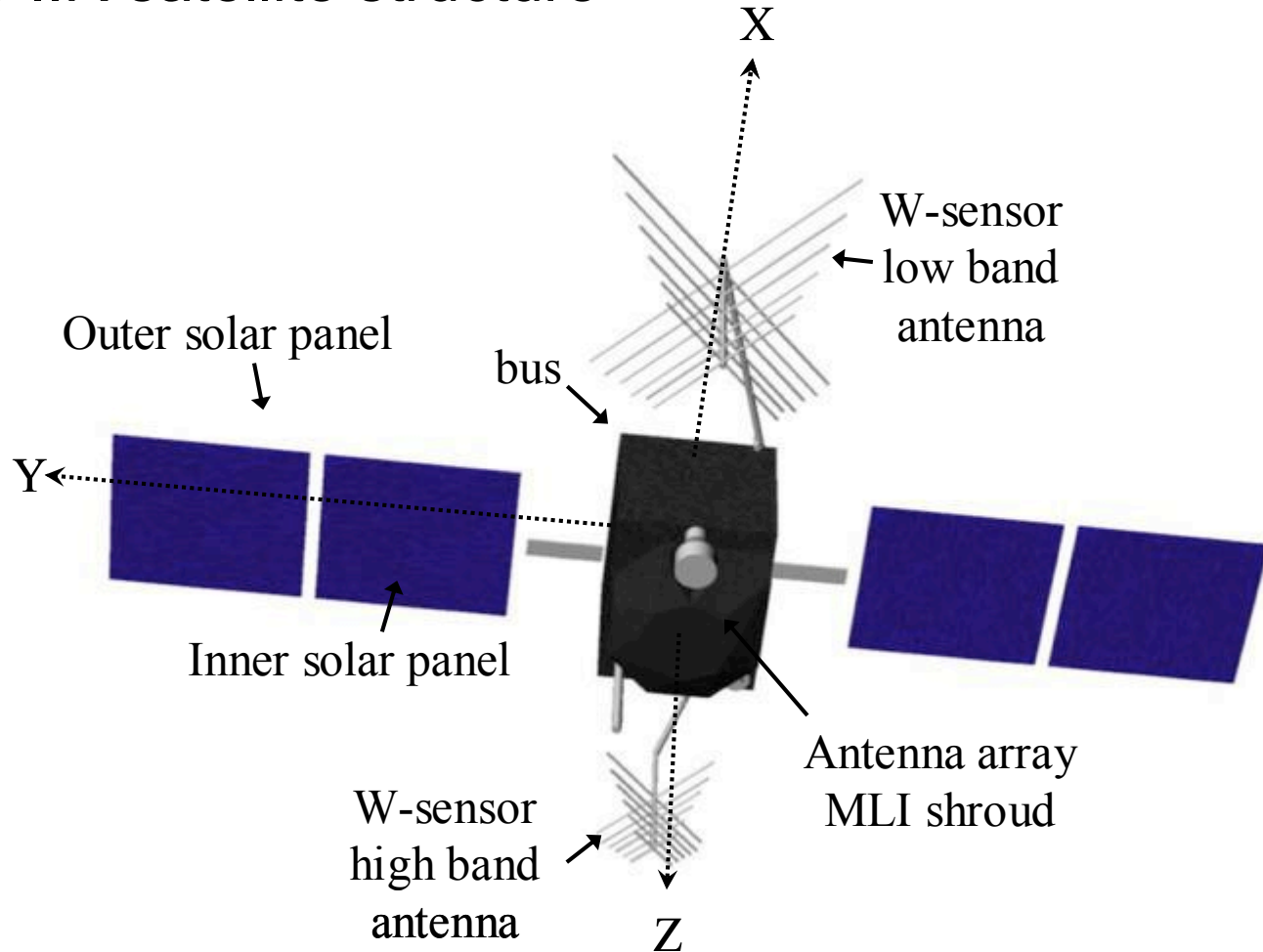
- Pixel array algorithm determines insolation of MLI
- 'Effective emissivity' ( $\epsilon_{eff}$ ) parameter governs heat transfer to bus
- MLI blackened,  $\alpha=0.94$   
 $\Rightarrow$  large thermal force

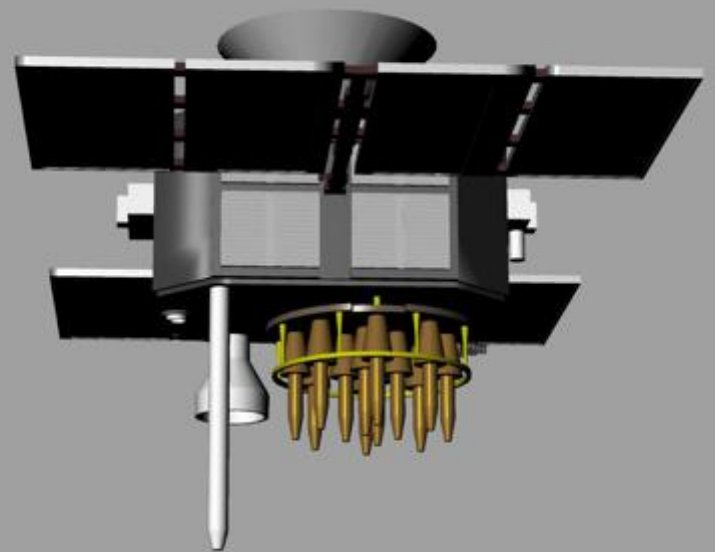
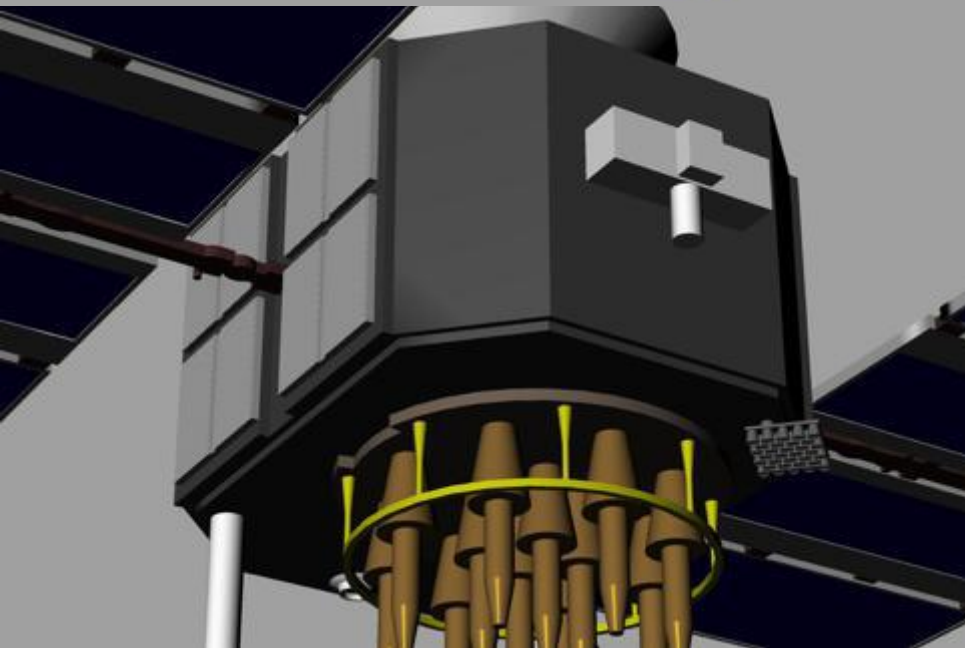
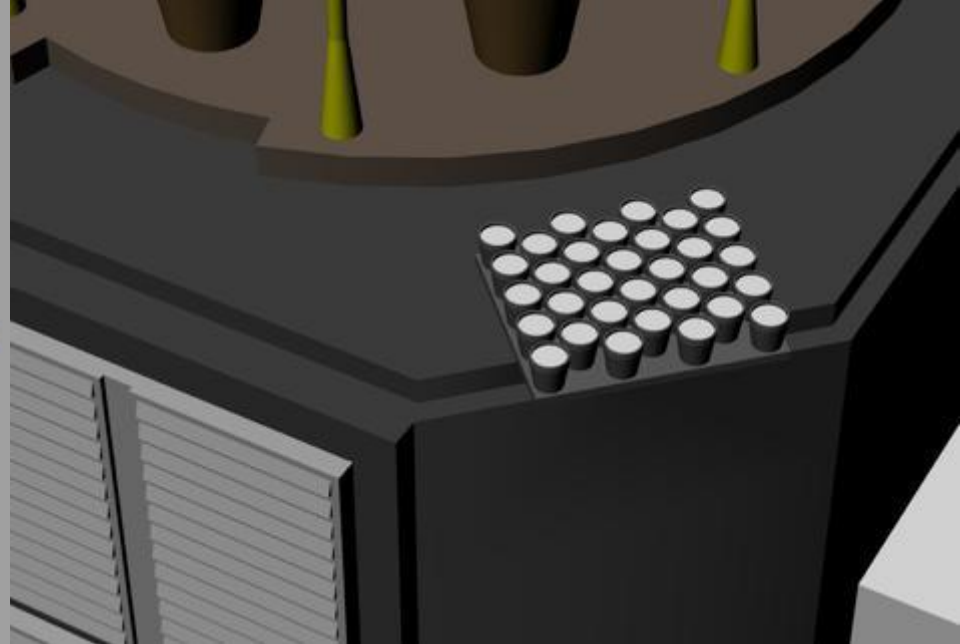
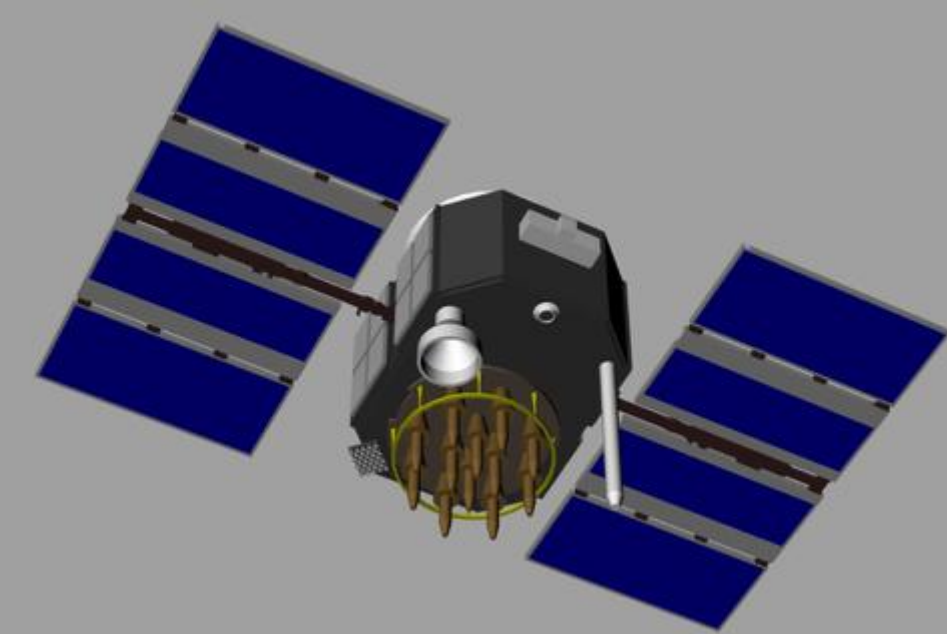
*Energy balance:*



$$T_{MLI}^4 = \frac{\alpha W \cos \theta + \epsilon_{eff} \sigma T_{sc}^4}{\sigma(\epsilon_{MLI} + \epsilon_{eff})}$$

# GPS IIR satellite structure



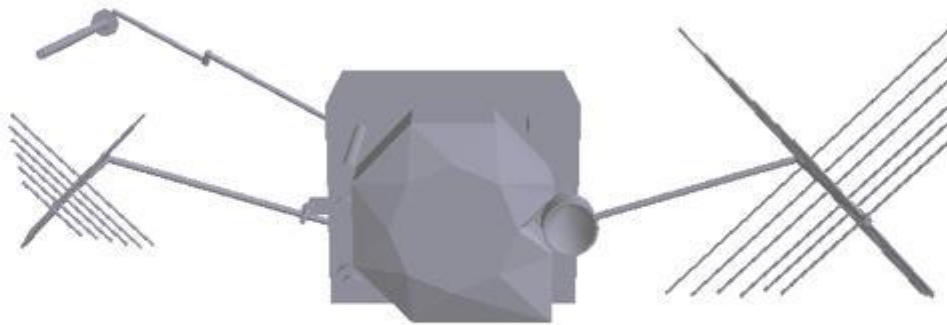


We develop a detailed structural computer model of the spacecraft

# Ray Tracing - 1

Geometry

Material types

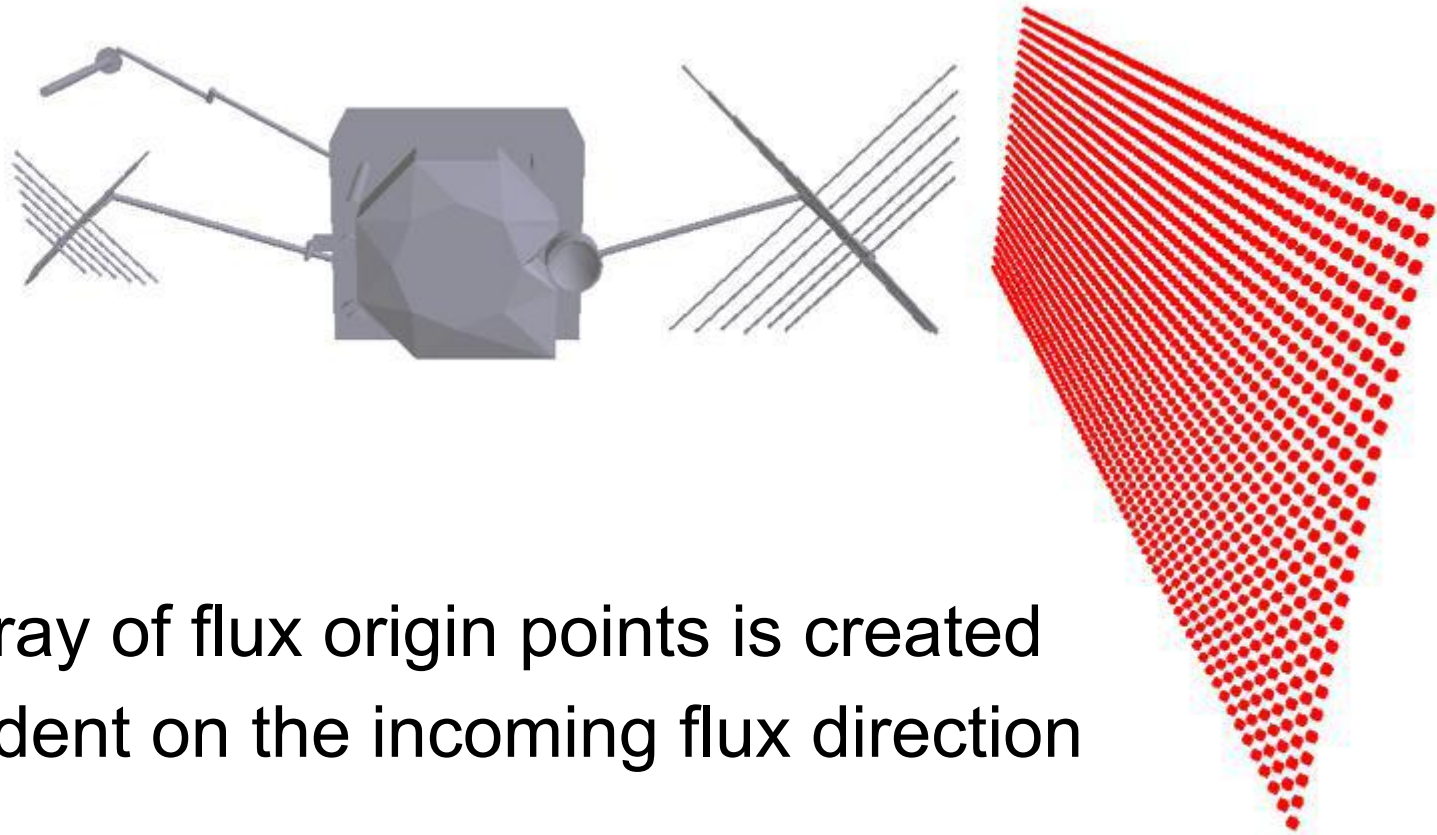


Optical and thermal properties

Spacecraft model represented in the SV body frame



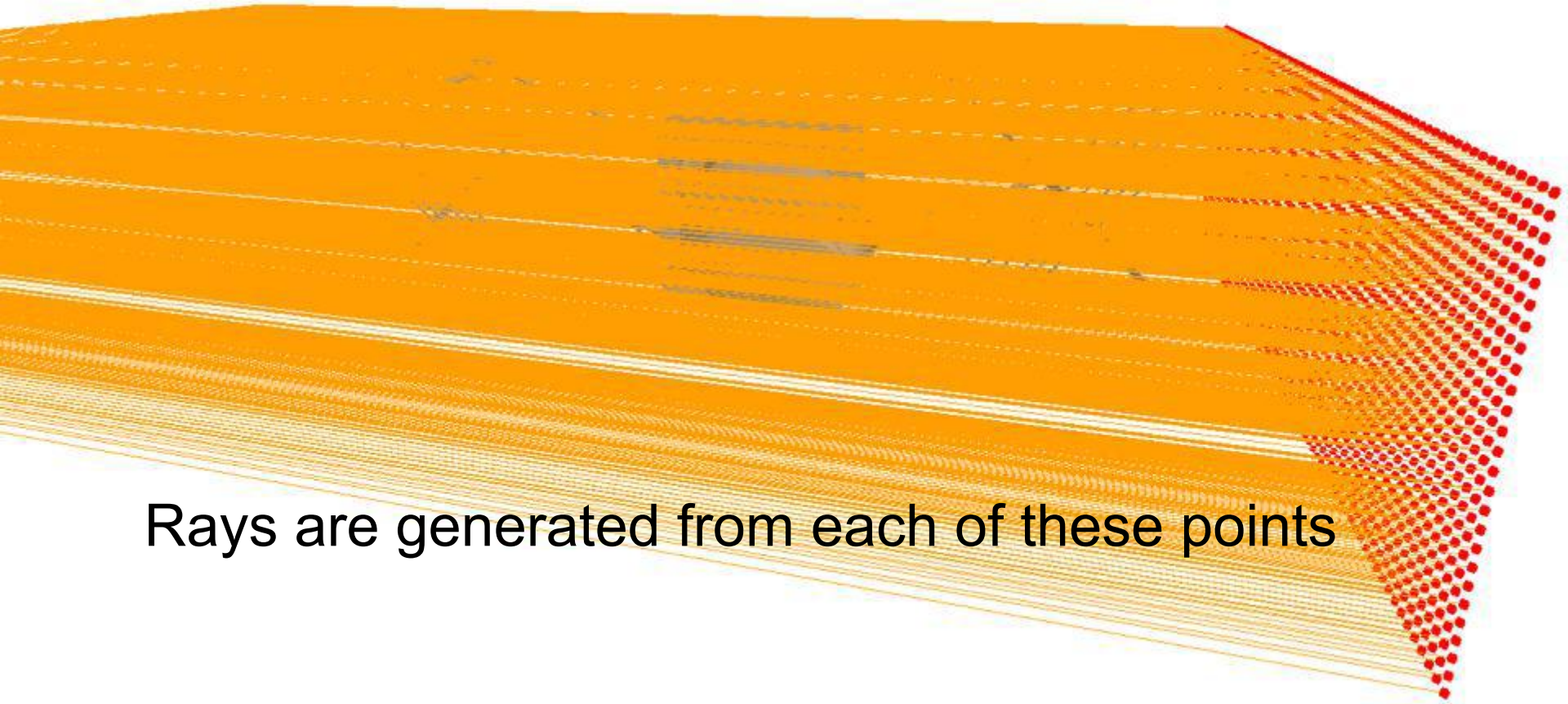
# Ray Tracing - 2



An array of flux origin points is created  
Dependent on the incoming flux direction

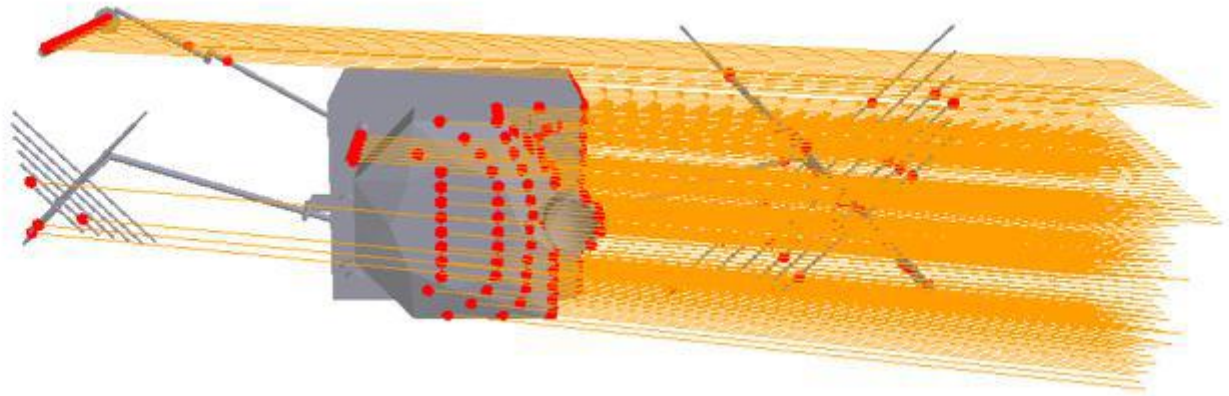


# Ray Tracing - 3



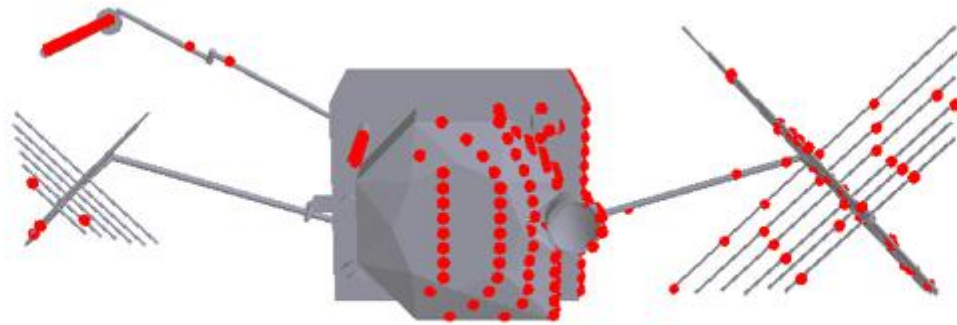
Rays are generated from each of these points

# Ray Tracing - 4



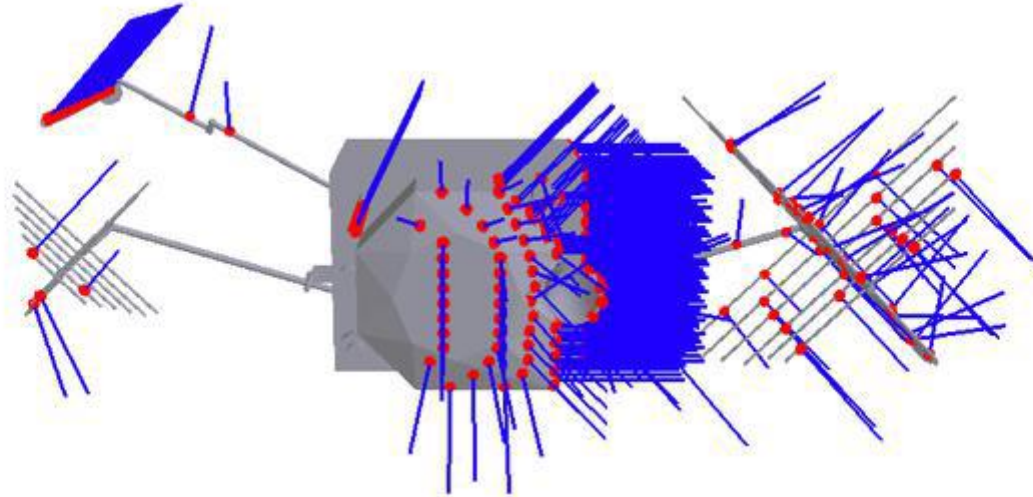
The intersection between each ray and the spacecraft is computed

# Ray Tracing - 5



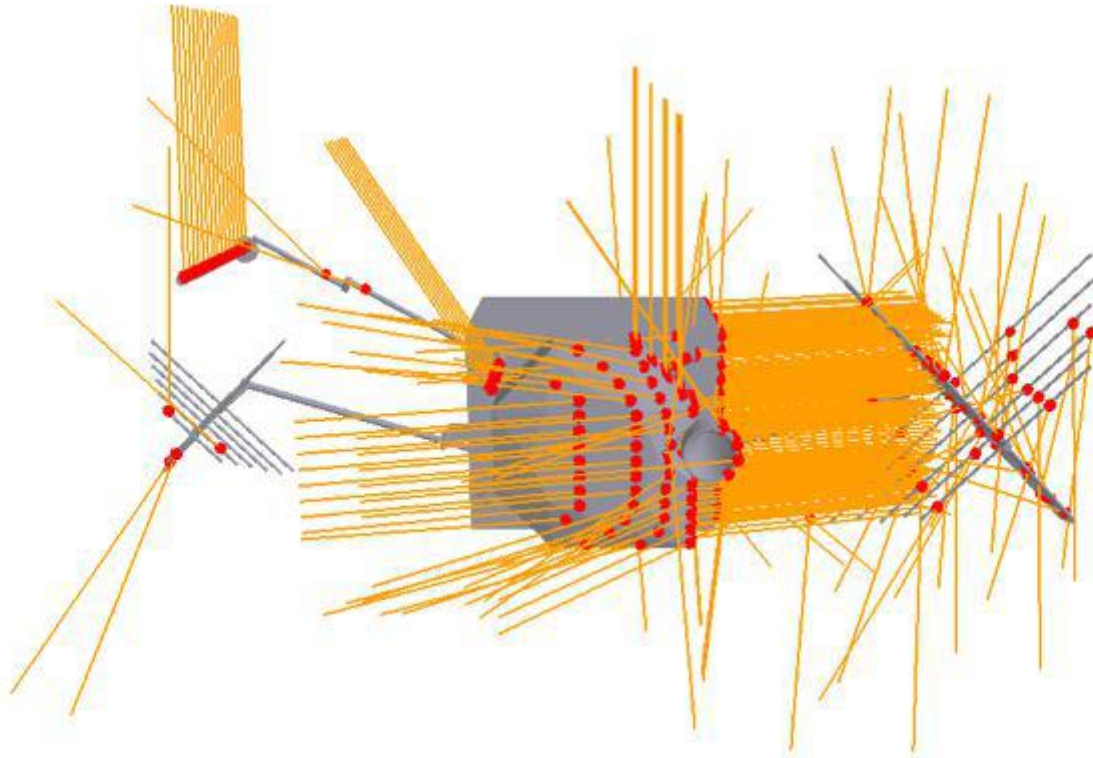
The material properties of the surface are known at each of these points

# Ray Tracing - 6



The surface normal is calculated at each of these points for planar or **curved** surfaces

# Ray Tracing - 7

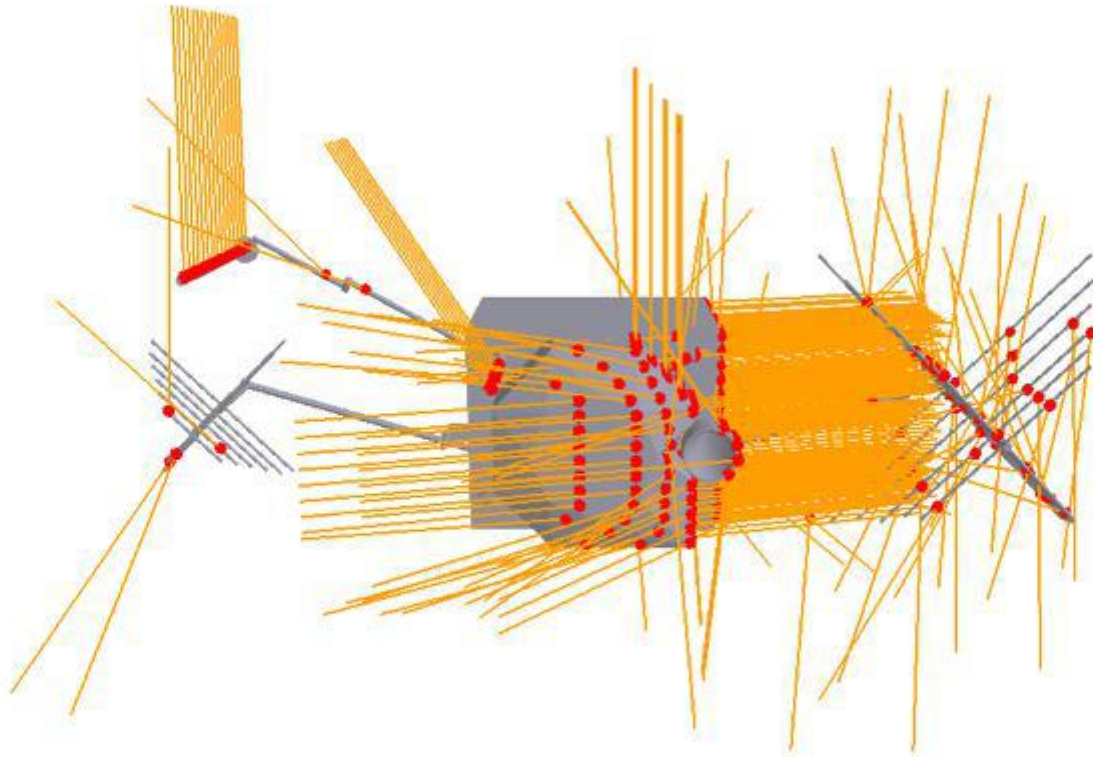


New rays are generated for each reflection and the intersection and reflection step repeated:

Secondary intersections



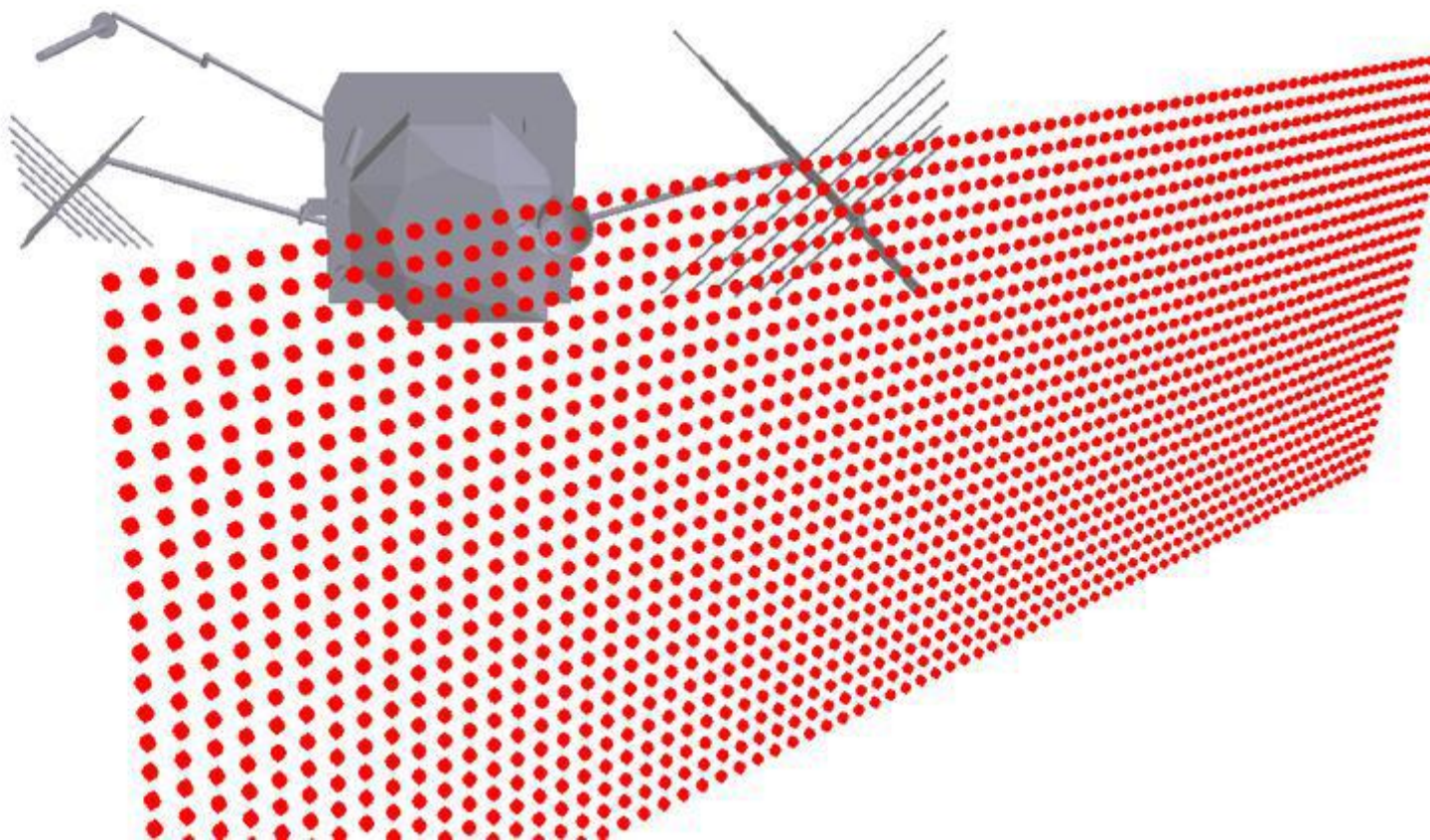
# Ray Tracing - 8



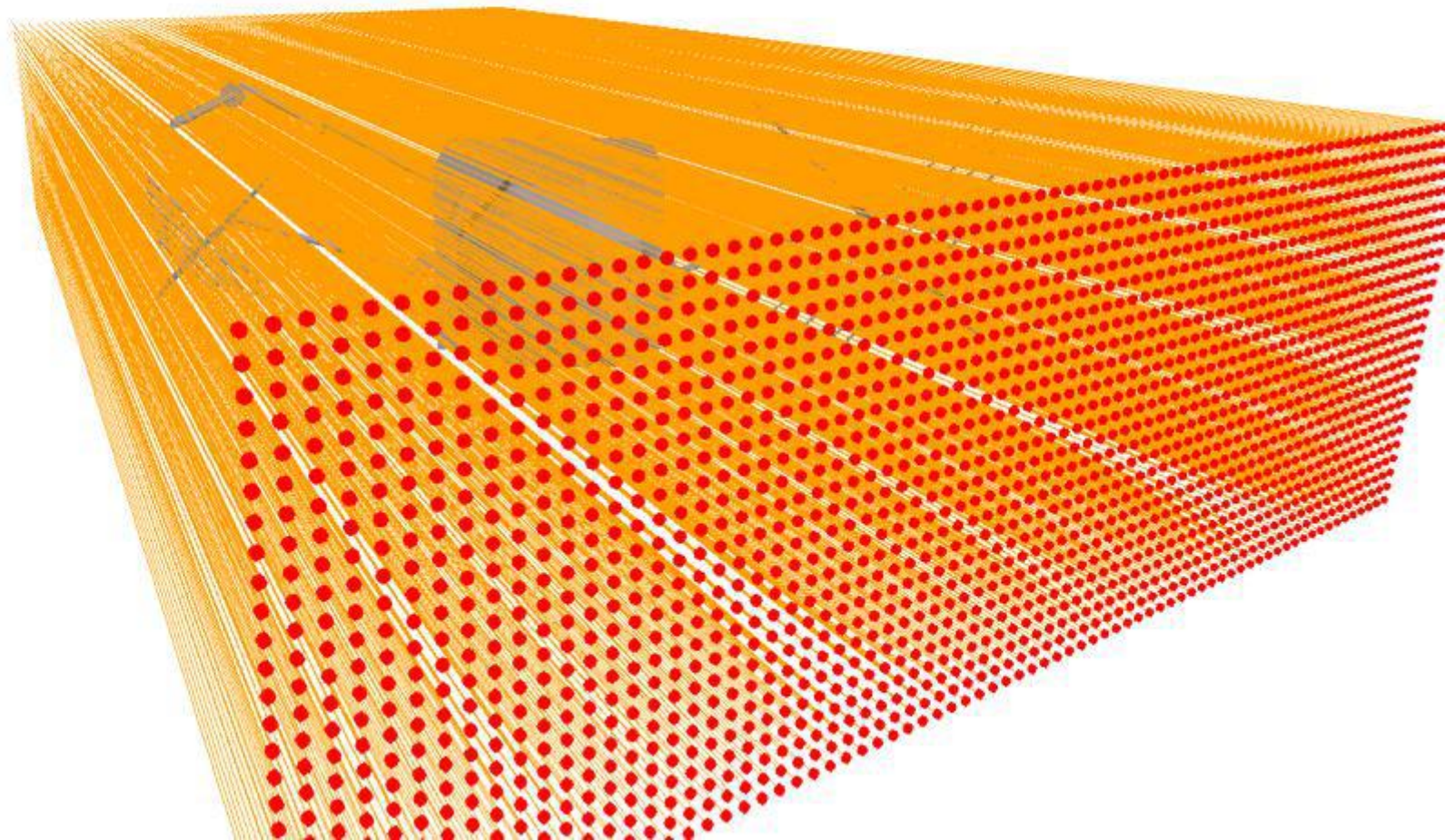
The acceleration data for all rays (primary and secondary) is collected:

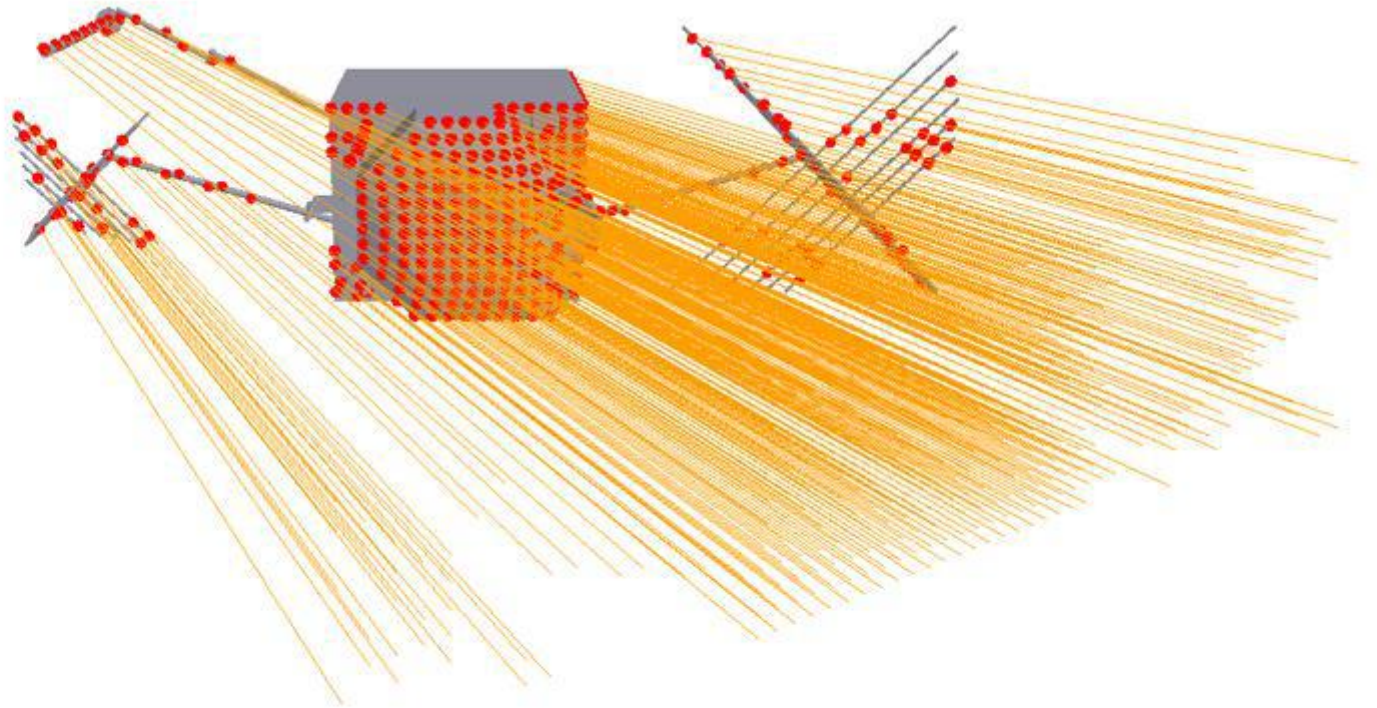
Resultant acceleration computed for that radiation source direction

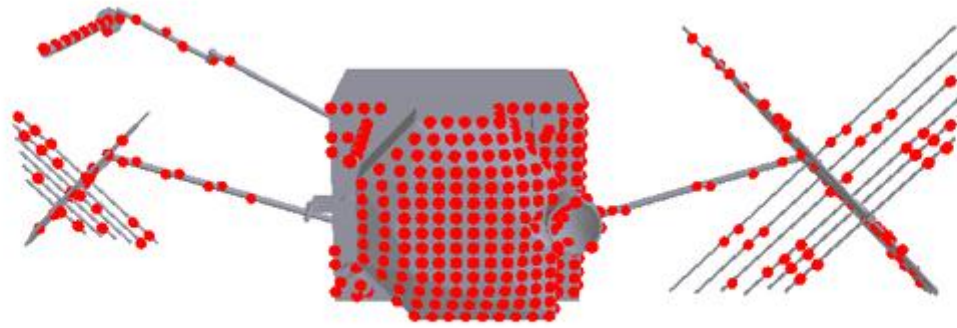
**Process is repeated for other incoming flux directions**

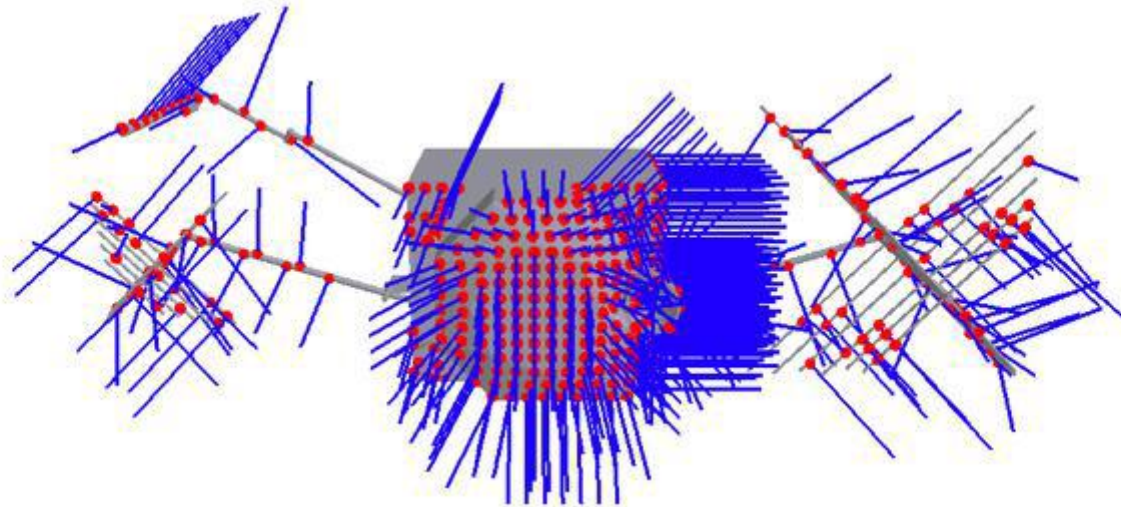




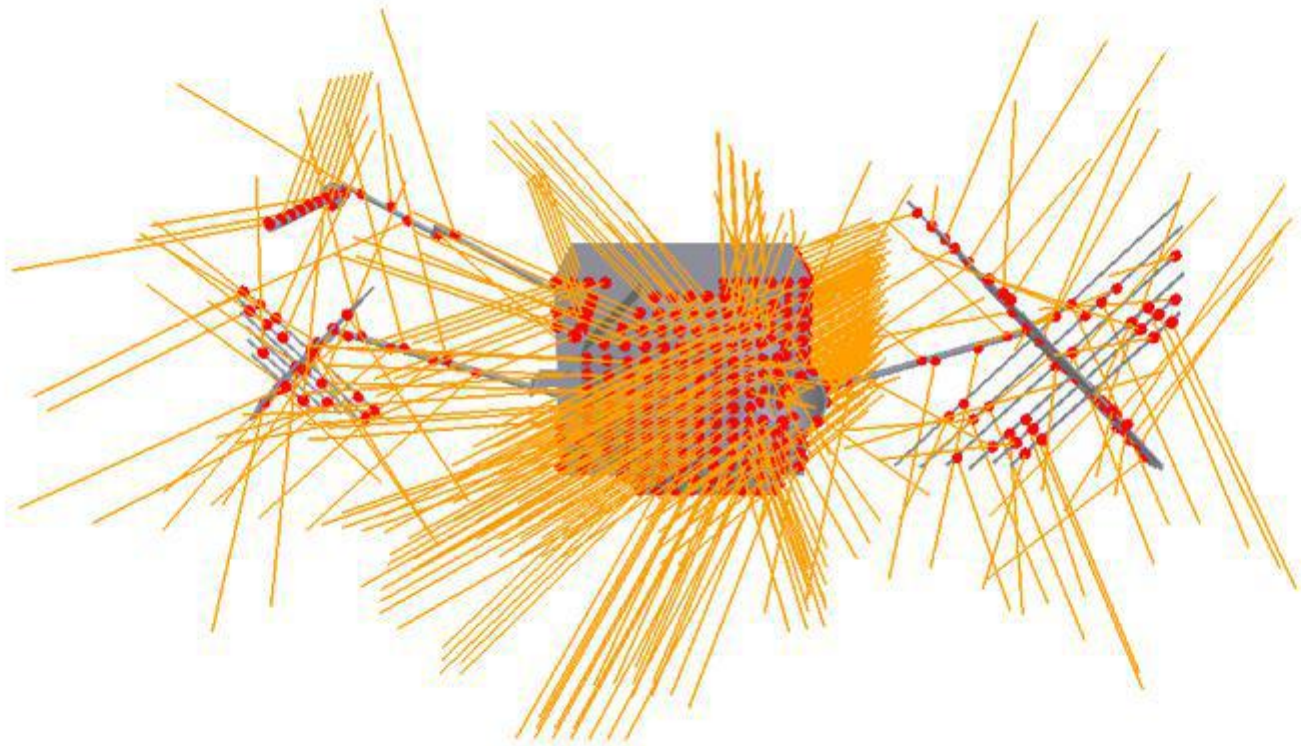




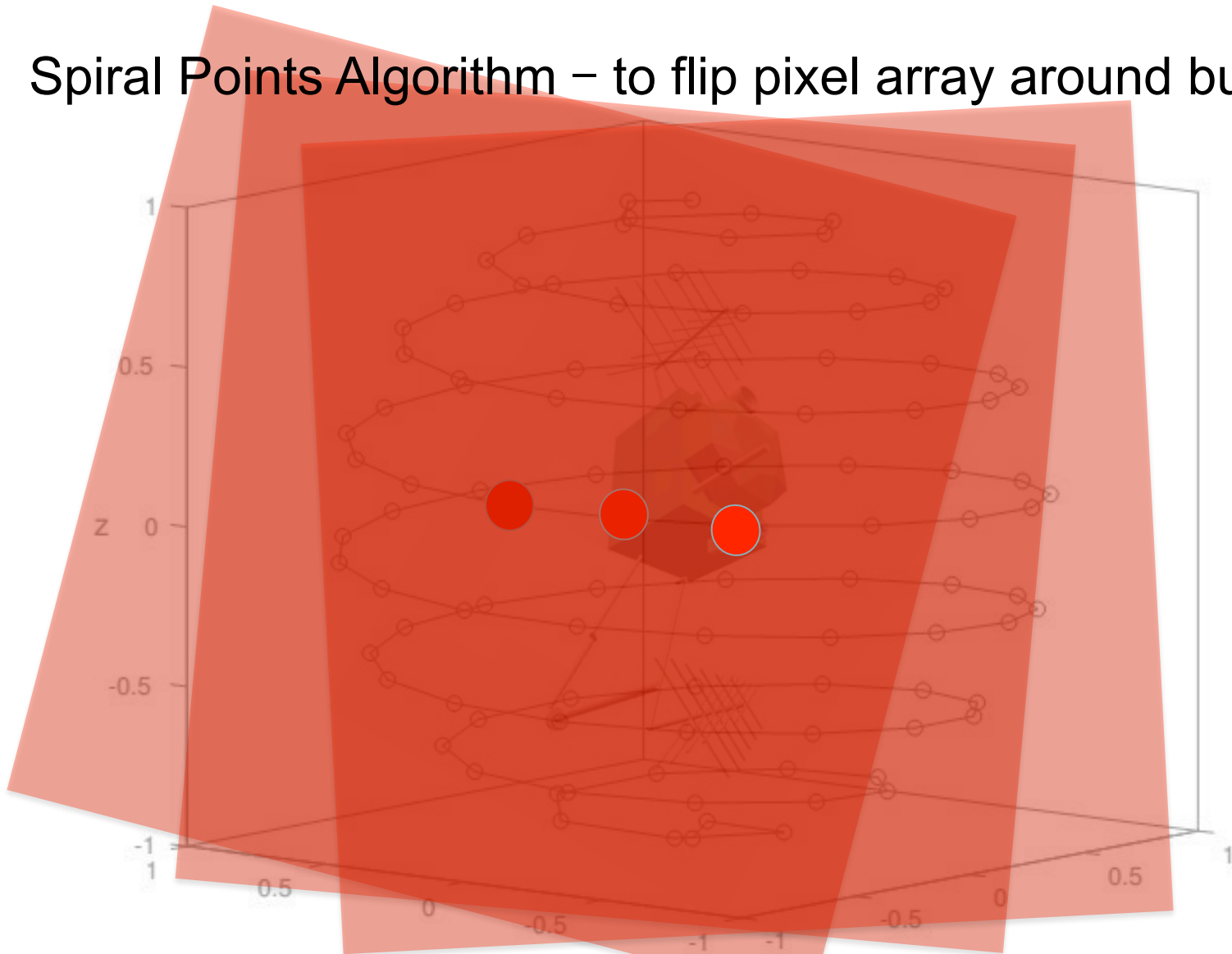




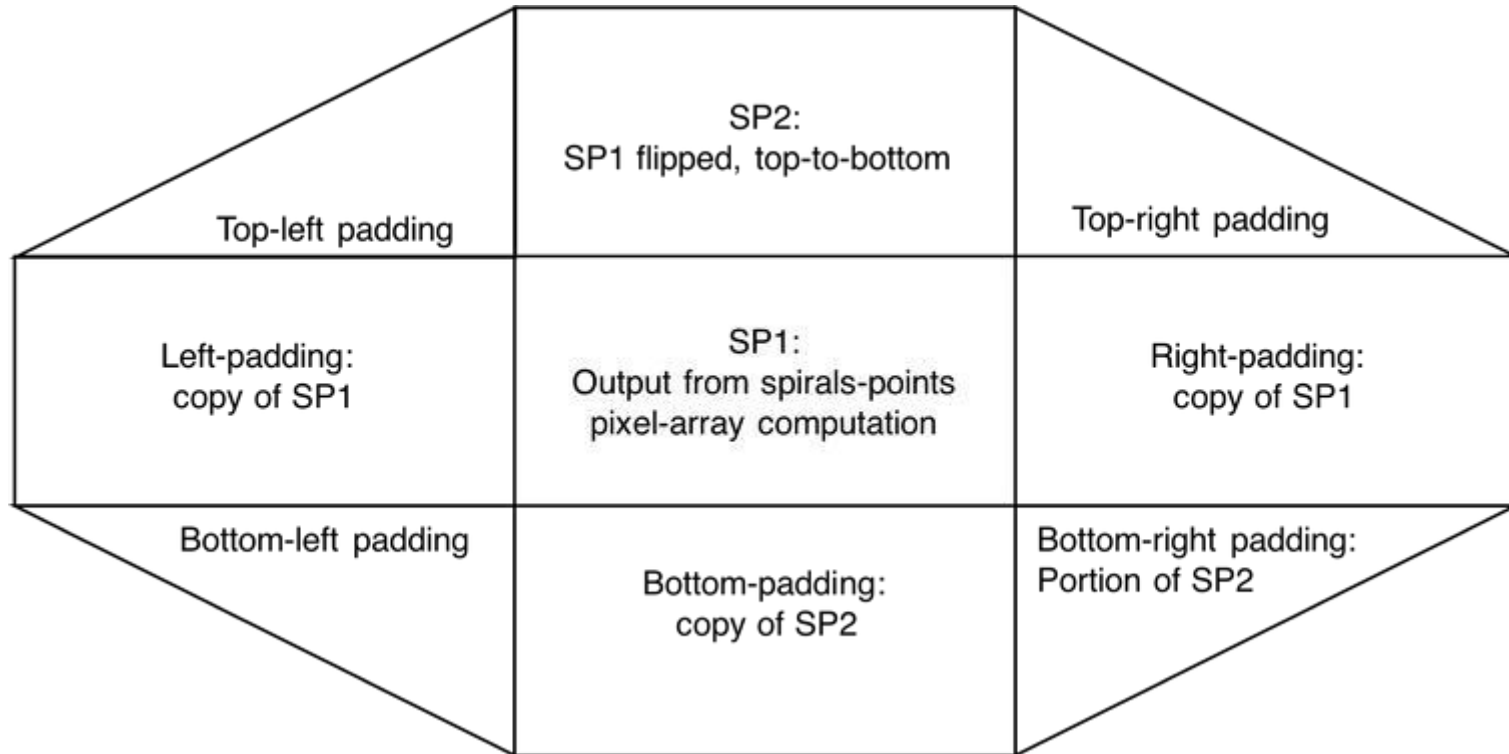




## Spiral Points Algorithm – to flip pixel array around bus



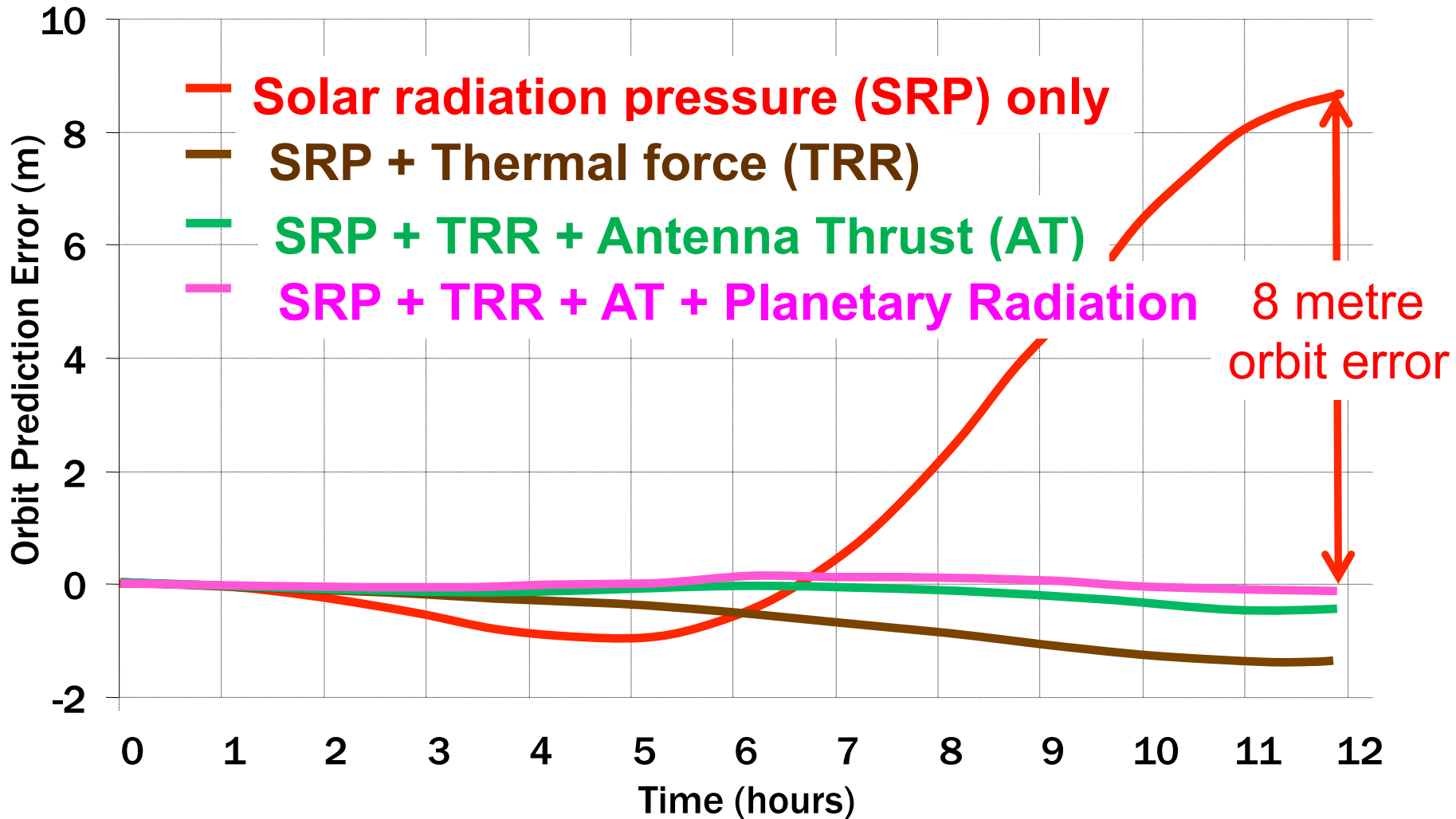
*A priori* model computation uses 10,000 spiral points, at 1mm pixel resolution



- Schematic representation of the padded spiral points data set used to avoid discrepancies at the grid edges during the grid file production
- Technical paper in submission to explain process



Along-track orbit prediction errors over 12 hours for one GPS IIR satellite with different photon-based force models



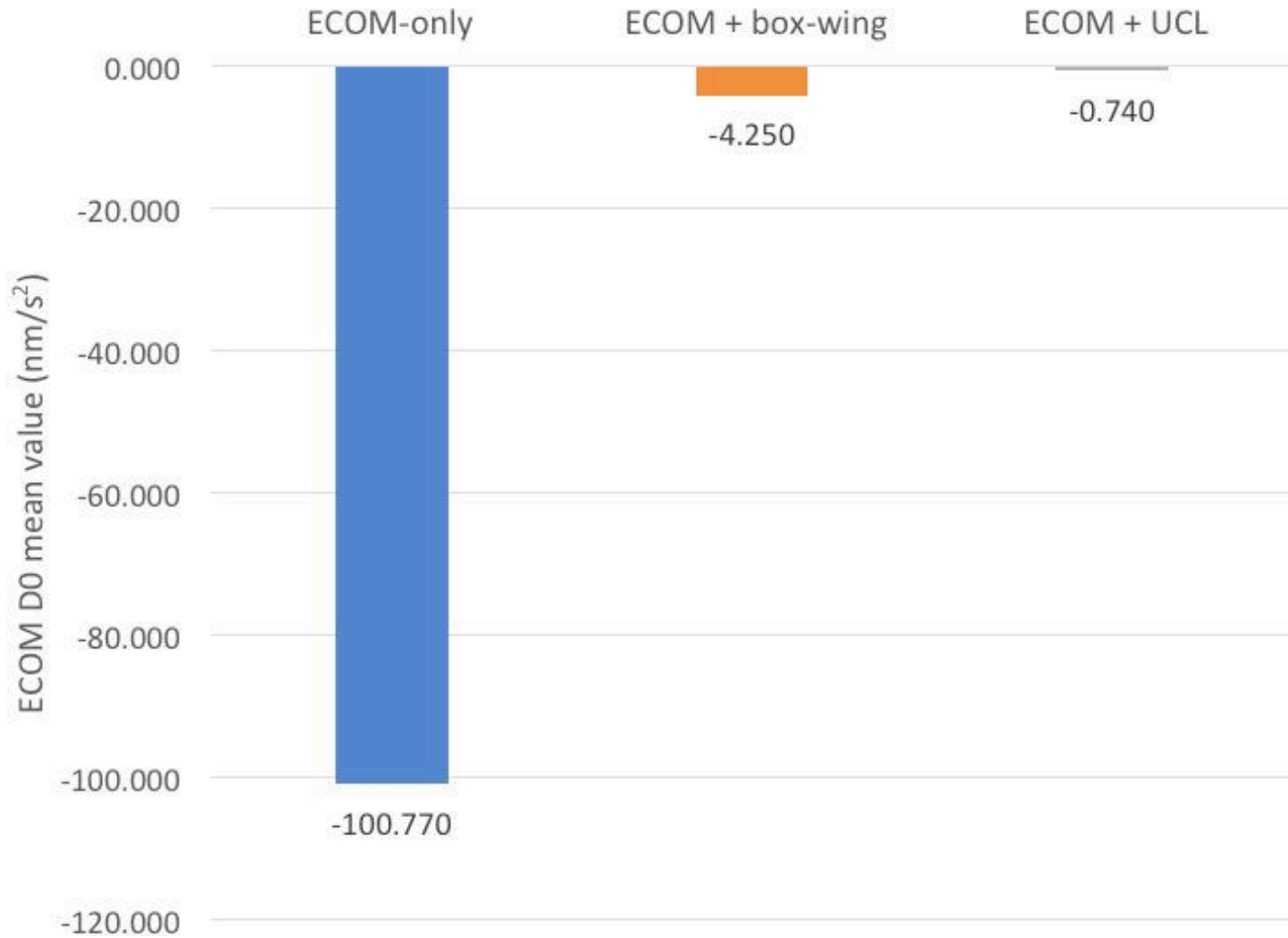
## Description of Experiment

- Software: NAPEOS
- 100 station global network
- One year of daily orbits
- Three contrasting force model parameterizations
- Analysis: values of empirical parameters, orbit overlaps

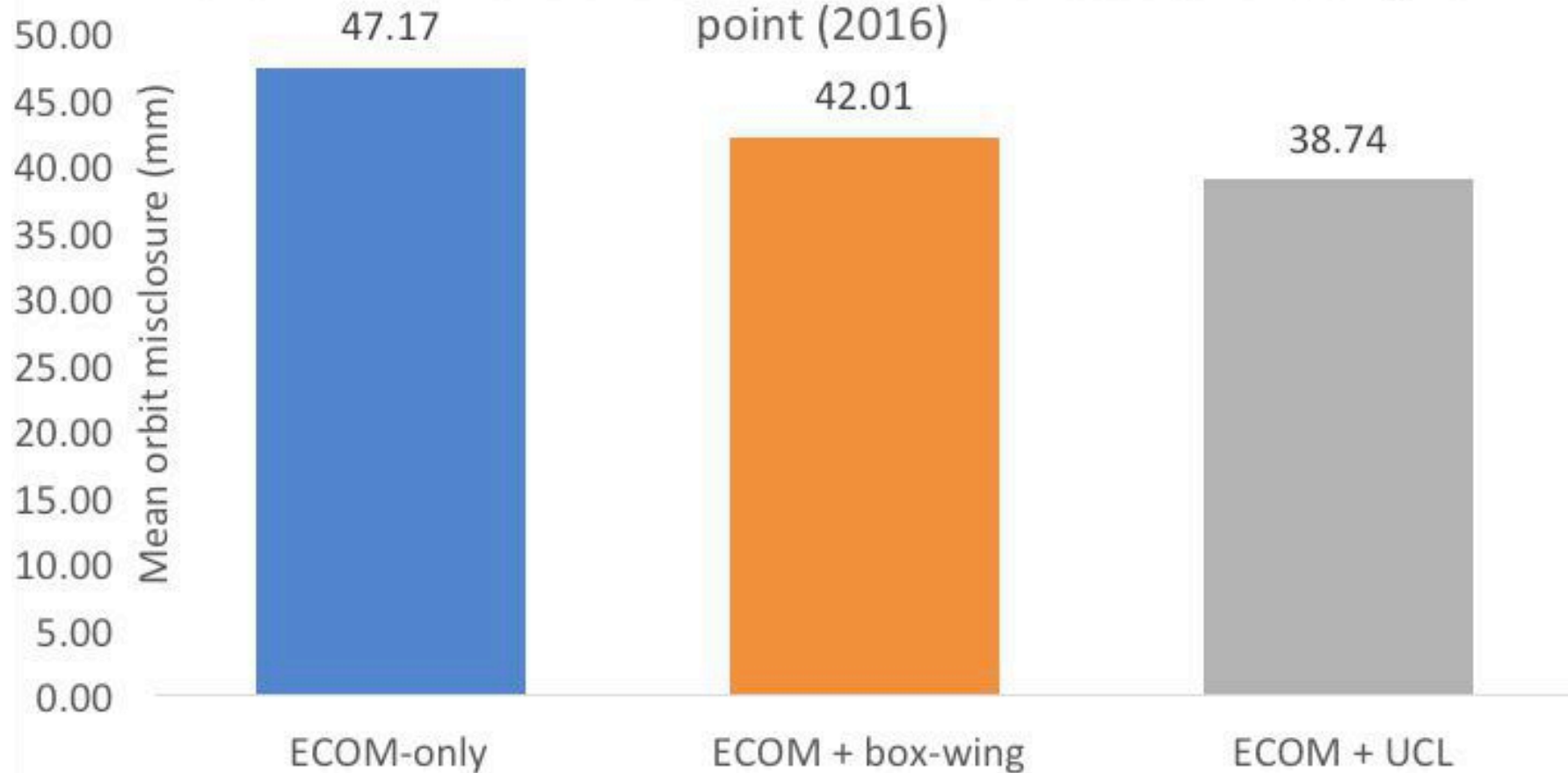
## Force model parameterizations

1. ECOM: No *a priori* model, 5 ECOM parameters (constants  $D_0$ ,  $Y_0$ ,  $B_0$ , and the cosine and sine terms in the B-direction) and 3 constrained along-track parameters (constant and cosine and sine with argument of latitude as period).
2. ECOM + Box-wing: Same estimation strategy as ECOM-only, but with an *a priori* box-wing model.
3. UCL model: the only difference with strategy 2 is that the box-wing model is replaced by the UCL bus 'grid file' model + solar panels SRP force.

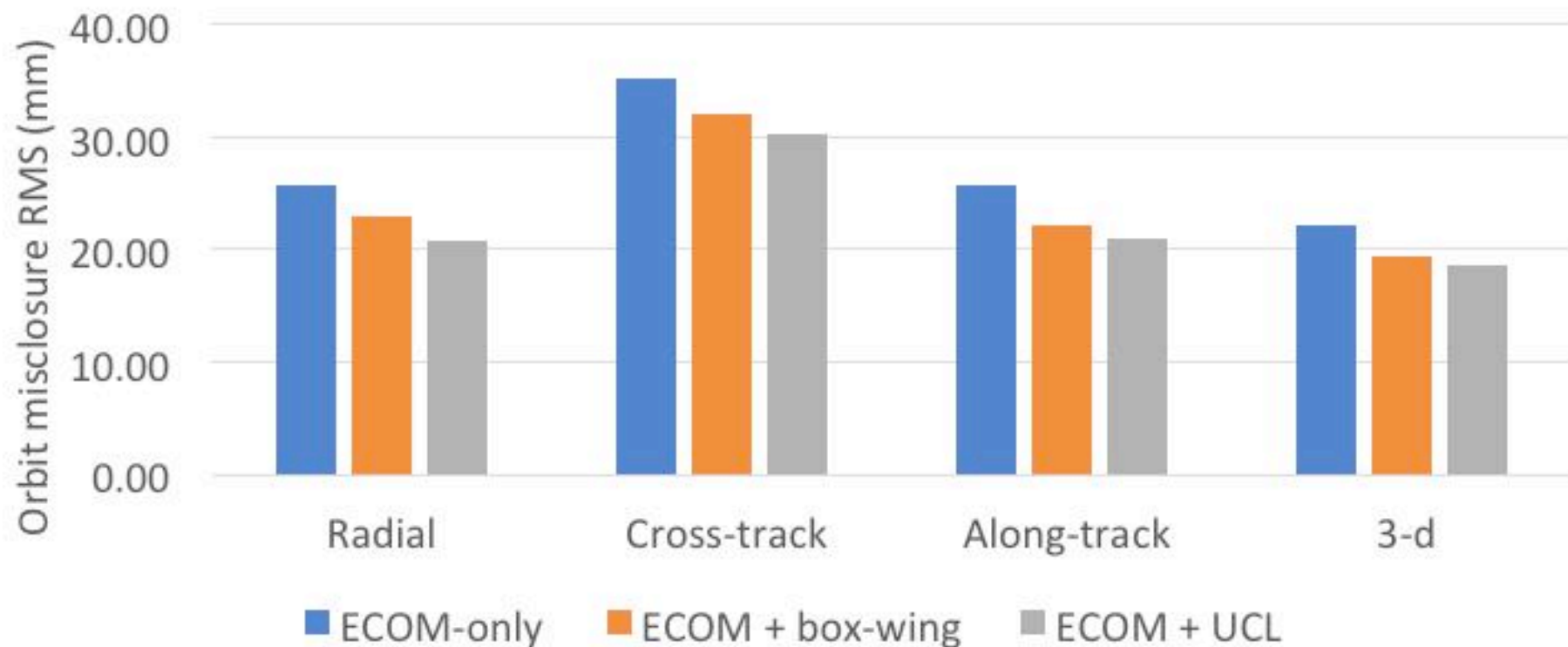
GPSIIR: Mean value of the ECOM D0 parameter (2016)



GPS IIR: Mean of 3-d orbit overlap differences at the midnight point (2016)



GPS IIR: RMS of orbit overlap differences at the midnight point  
(2016)



## Conclusions

- UCL's grid file bus modelling has been applied successfully to LEO spacecraft (JPL, GSFC) but has not been tested on GNSS by the IGS
- Tests show encouraging results for orbit improvements in accuracy of physical modelling and orbit overlaps
- UCL/Positim/GMV/ESTEC are applying this technique to Galileo IOV and FOC right now
- We have demonstrated improved precision – the aim of this workshop!