

# Refined and site-augmented tropospheric delay models for GNSS applications

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# Troposphere delay modeling

$$\Delta L(e) = \Delta L_h^z \cdot mf_h(e) + \Delta L_w^z \cdot mf_w(e)$$

- $\Delta L^z$ : from IGS
- $\Delta L_h^z$ : calculated from  $p$  (measured or taken from models)
- $\Delta L_w^z$ : calculated via  $\Delta L^z - \Delta L_h^z$
- $mf_h, mf_w$ : from real-time mapping functions such as VMF1

**BUT:** Many applications without access to data from NWM or IGS

=> empirical troposphere models

# GPT2w

## Global Pressure and Temperature 2 wet (Böhm et al., 2015)

Empirical (blind) troposphere model providing:

$a_h$        $a_w$        $p$        $T$        $e$        $T_m$        $\lambda$

↓            ↓            ↓

$mf_h$        $mf_w$        $\Delta L_h^z$

$$\Delta L_w^z = 10^{-6} * \left( k'_2 + \frac{k_3}{T_m} \right) * \frac{R_d e}{(\lambda + 1) g_m}$$

formula of Askne and Nordius (1987)

Can we improve the empirical  $\Delta L_w^z$  by including in situ measured meteorological data?

# Augmentation of $\Delta L_w^z$

- no in situ measurements (= empirical only)

$$\Delta L_w^z = L_{wGPT2w}^z$$

- in situ measurement of  $T$ :

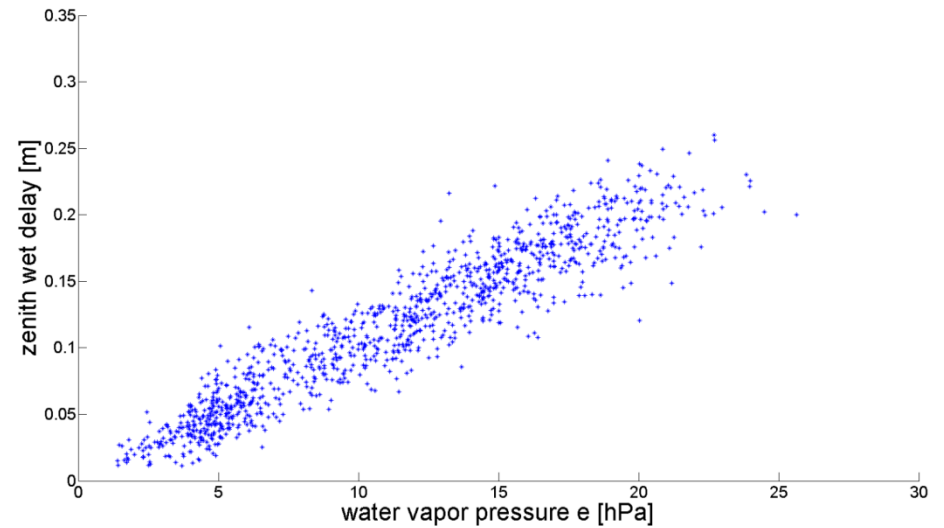
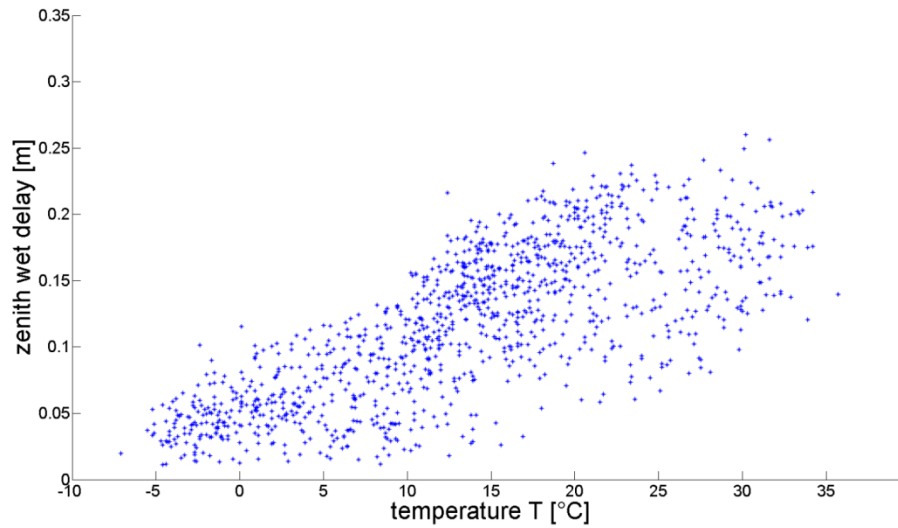
$$\Delta L_w^z = L_{wGPT2w}^z + M * (T_{GNSS} - T_{GPT2w})$$

- in situ measurement of  $T$  and  $e$ :

a.) 
$$\Delta L_w^z = L_{wGPT2w}^z + M_1 * (T_{GNSS} - T_{GPT2w}) + M_2 * (e_{GNSS} - e_{GPT2w})$$

b.) 
$$\Delta L_w^z = 10^{-6} * \left( k'_2 + \frac{k_3}{T_{mGPT2w}} \right) * \frac{R_d e}{(\lambda_{GPT2w} + 1) g_m}$$

# Augmentation of $\Delta L_w^z$



Correlation plots for BZRG

Overall correlations:

**T** with  $\Delta L_w^z$ : 0.65

**e** with  $\Delta L_w^z$ : 0.85

Universal, global coefficients M1, M2:

M1 =  $5 \cdot 10^{-4}$  [m/°C<sup>-1</sup>]

M2 = 0.0092 [m/hPa<sup>-1</sup>]

If user measures **T** and **e** => improve  $\Delta L_w^z$  :

$$\Delta L_w^z = L_{wGPT2w}^z + M_1 * (T_{GNSS} - T_{GPT2w}) + M_2 * (e_{GNSS} - e_{GPT2w})$$

# Data

## GNSS Data:

- 55 globally distributed IGS stations
- 4 epochs per day in 2013
- zenith total delay ( $\Delta L^z$ ) from IGS final tropospheric SNX-TROPO

## Meteo Data:

p, T, e from

1) close-by weather stations

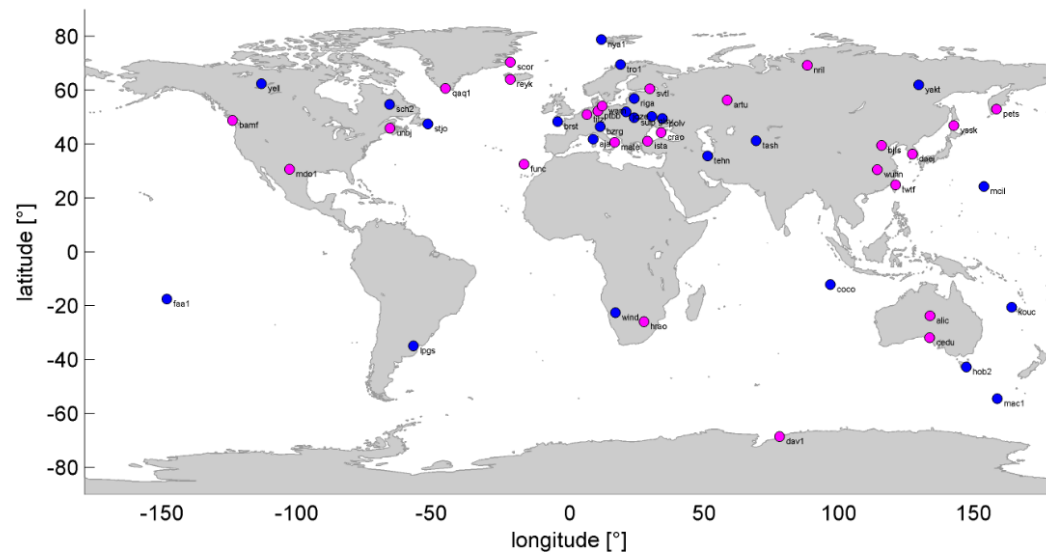
(provided by ZAMG, blue dots)

- max. 10km  $\leftrightarrow$  and 100m  $\updownarrow$  away
- high quality

2) in-situ measurements (provided

by IGS, pink dots)

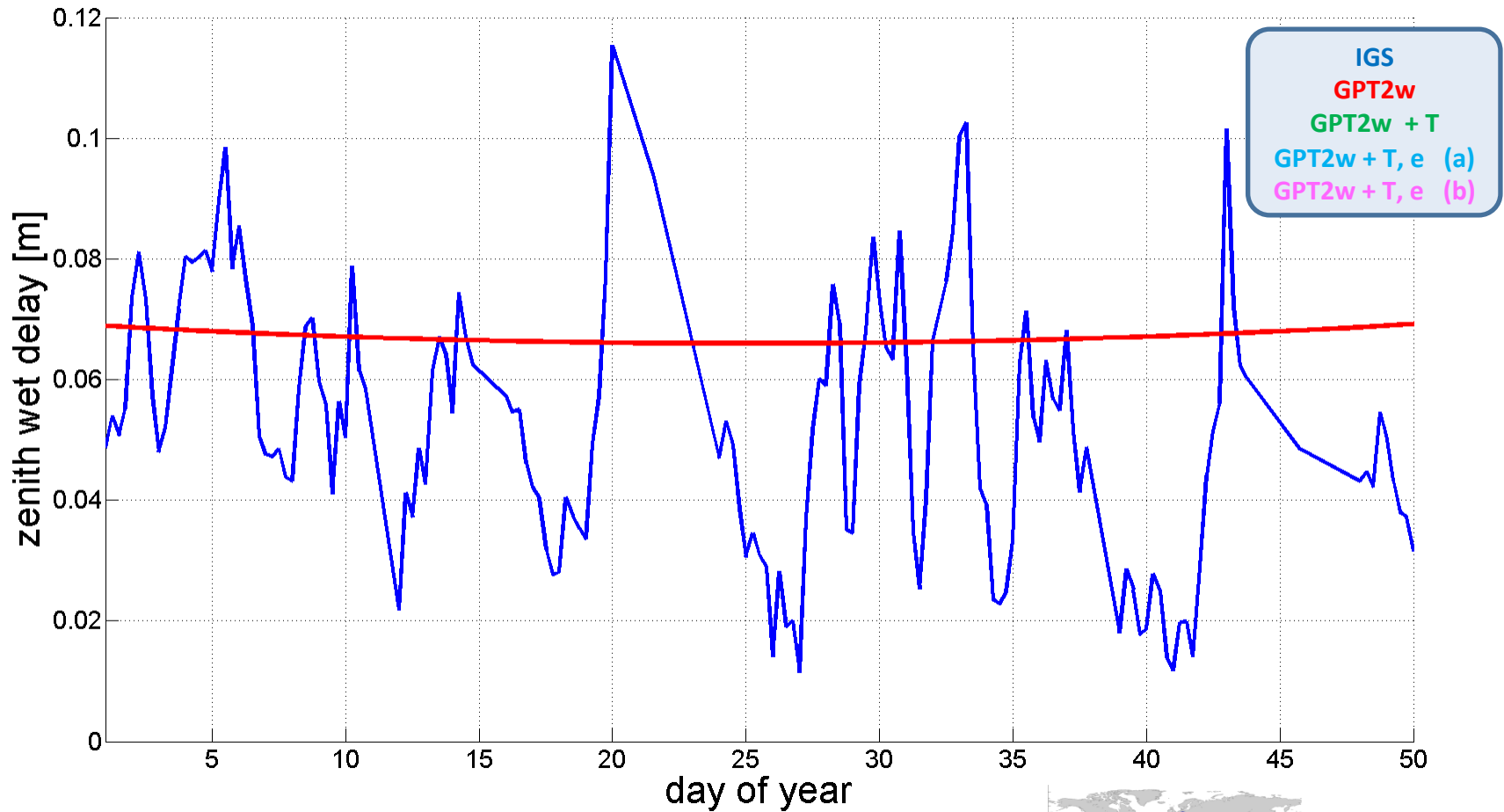
- moderate quality



p  $\rightarrow$  Extrapolation / Saastamoinen  $\rightarrow \Delta L_h^z$

$\Delta L_w^z = \Delta L^z - \Delta L_h^z \Rightarrow$  Considered as „true“ values

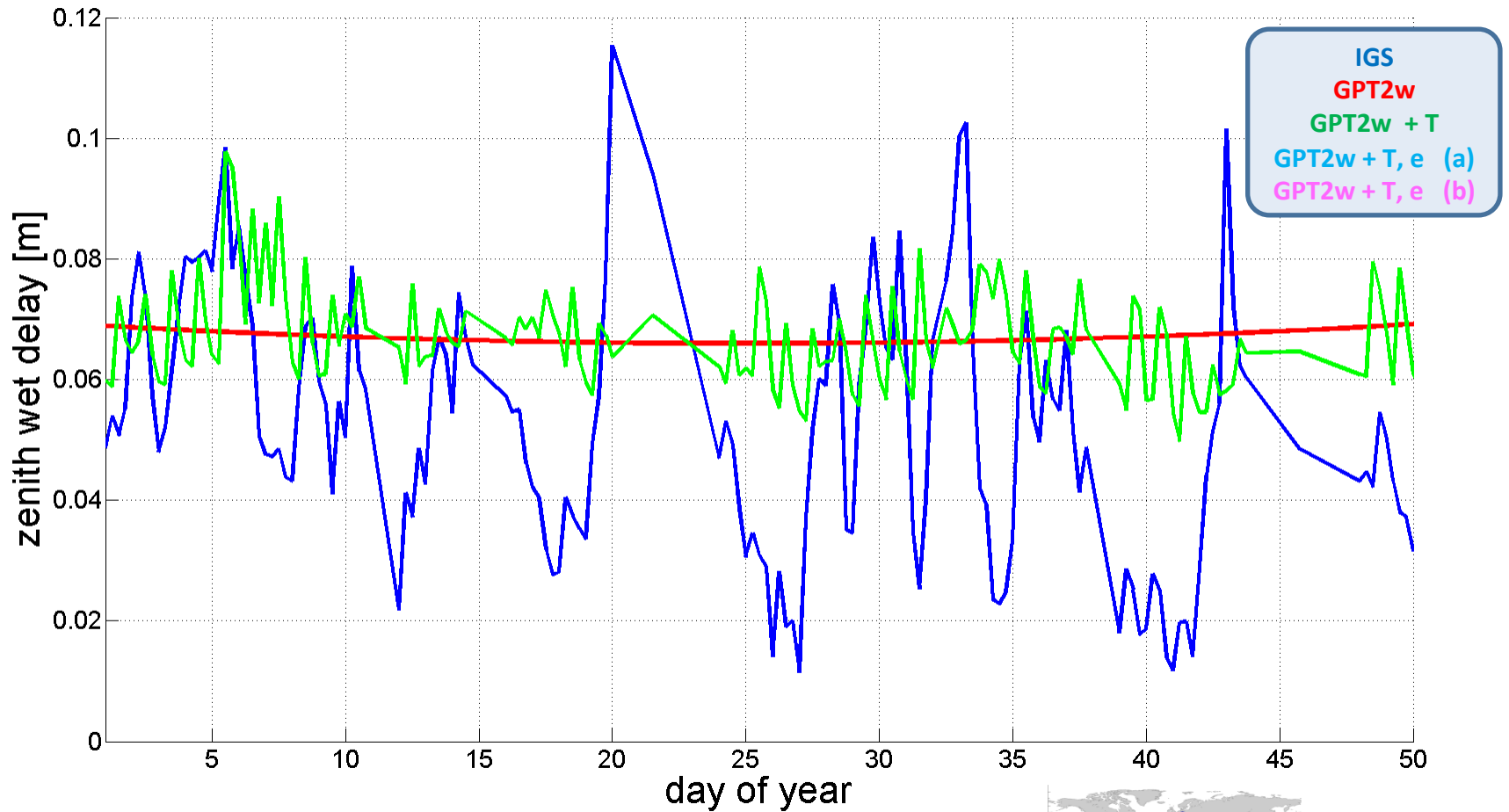
# Results



Comparison of  $\Delta L_w^z$  for BZRG



# Results

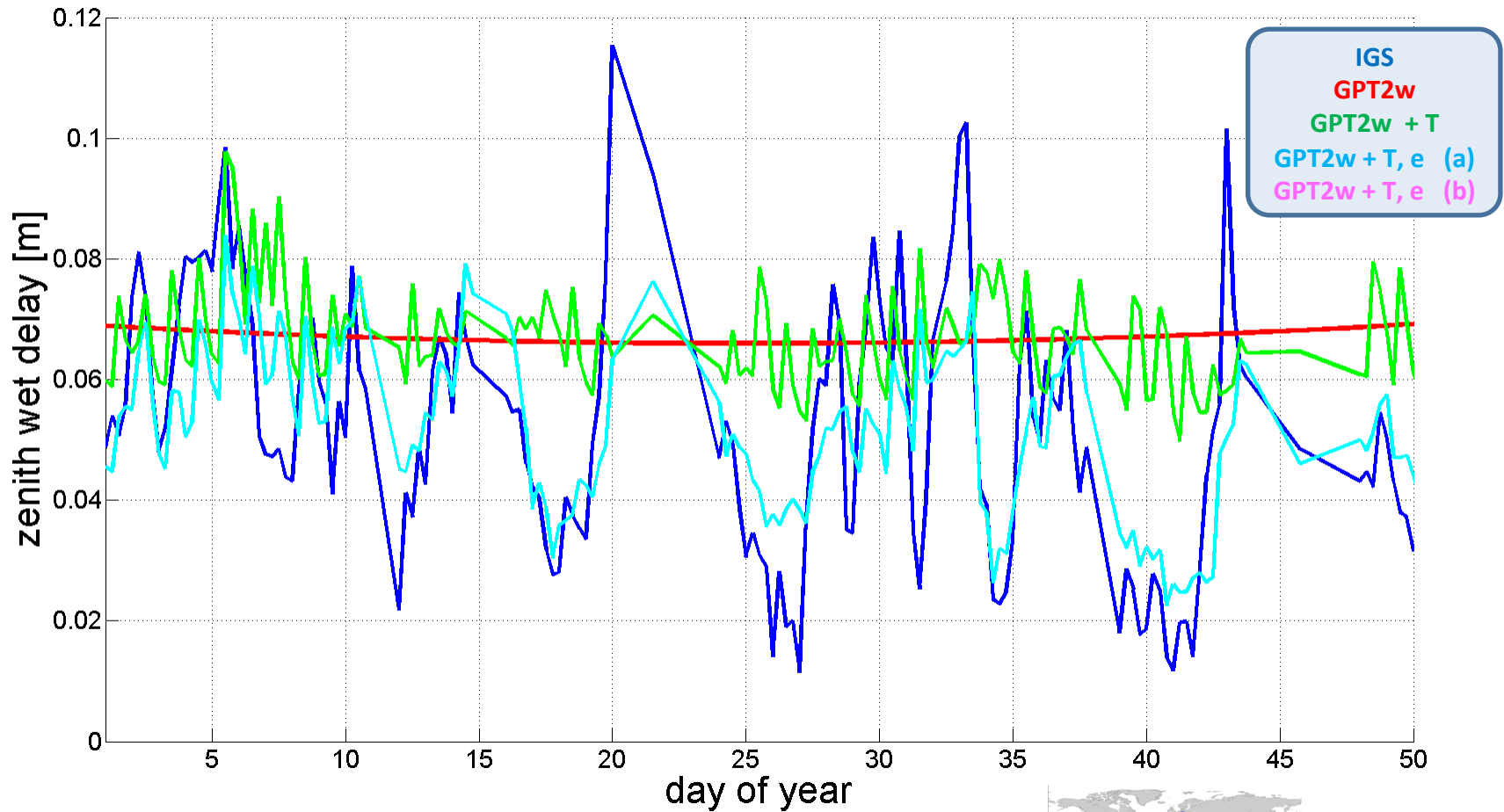


Comparison of  $\Delta L_w^z$  for BZRG





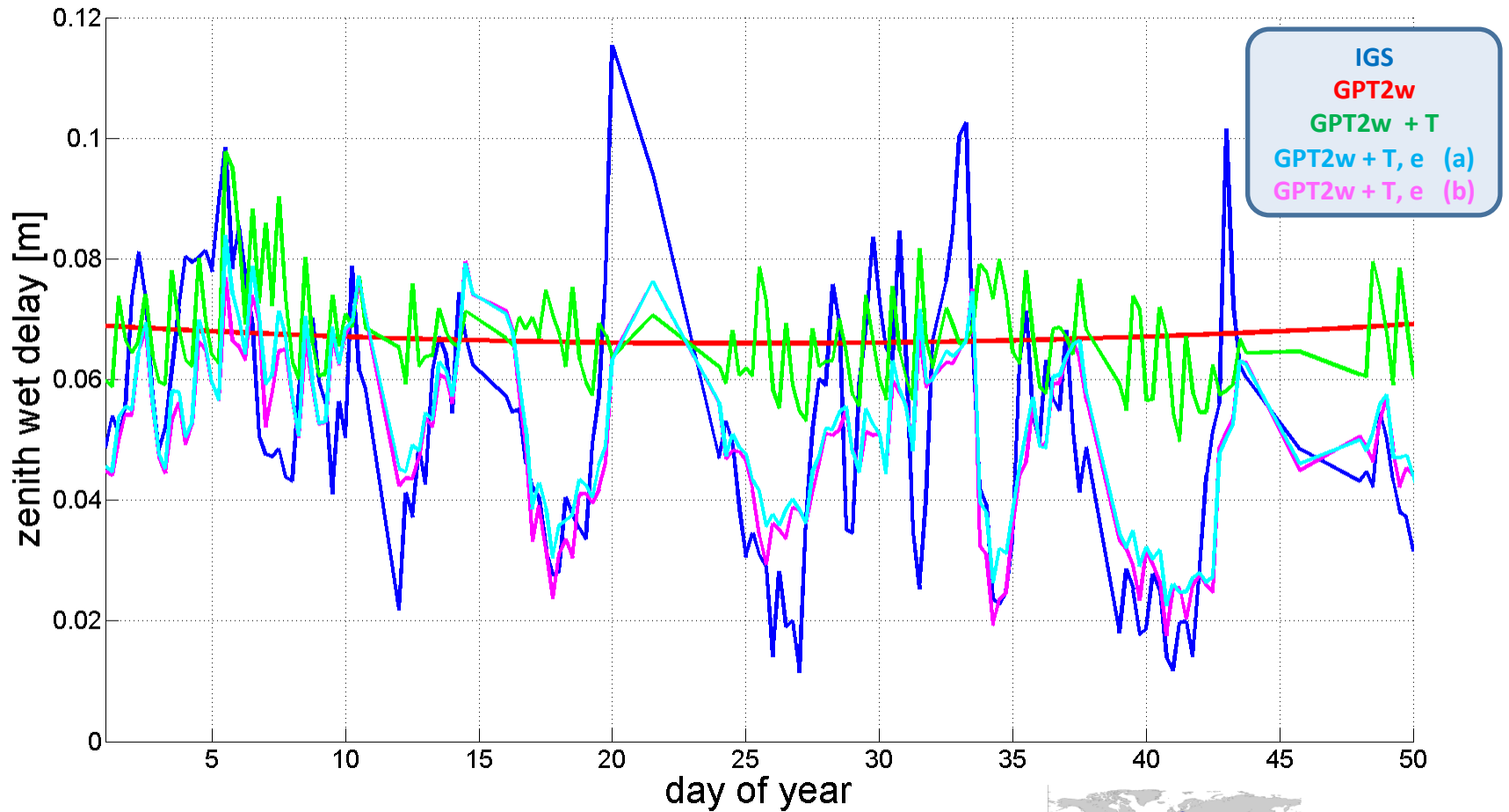
# Results



Comparison of  $\Delta L_w^z$  for BZRG



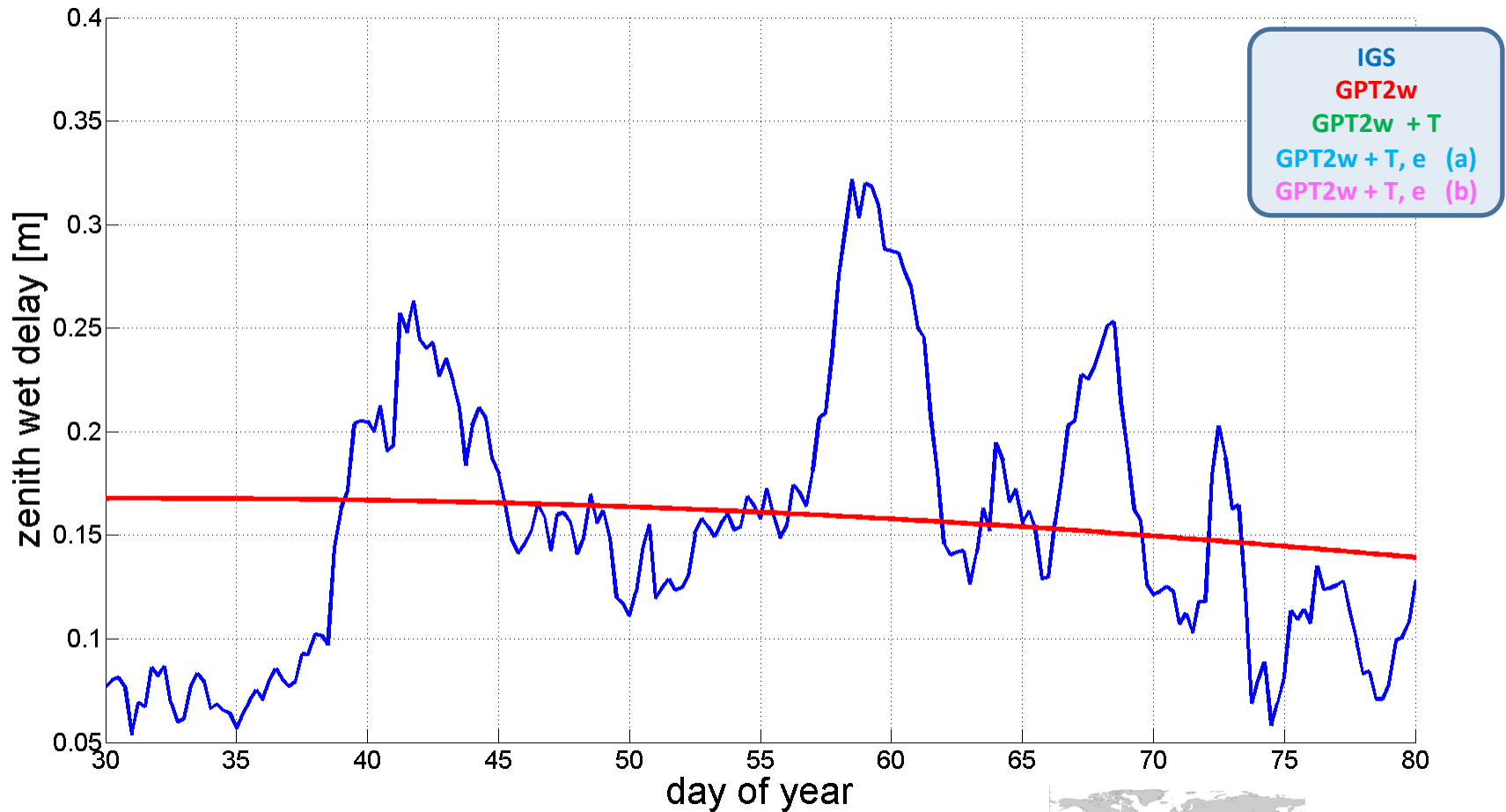
# Results



Comparison of  $\Delta L_w^z$  for BZRG



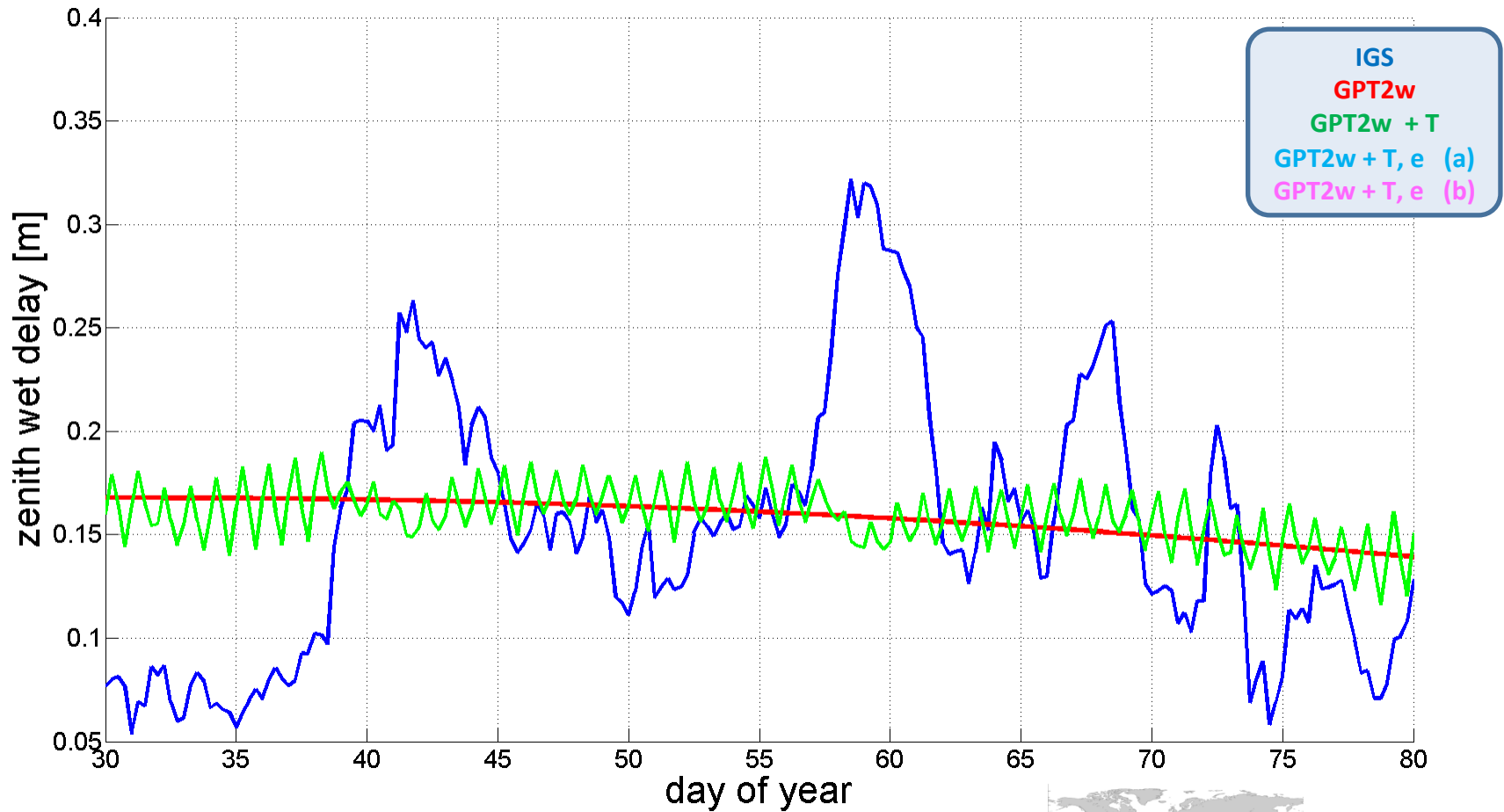
# Results



Comparison of  $\Delta L_w^z$  for ALIC



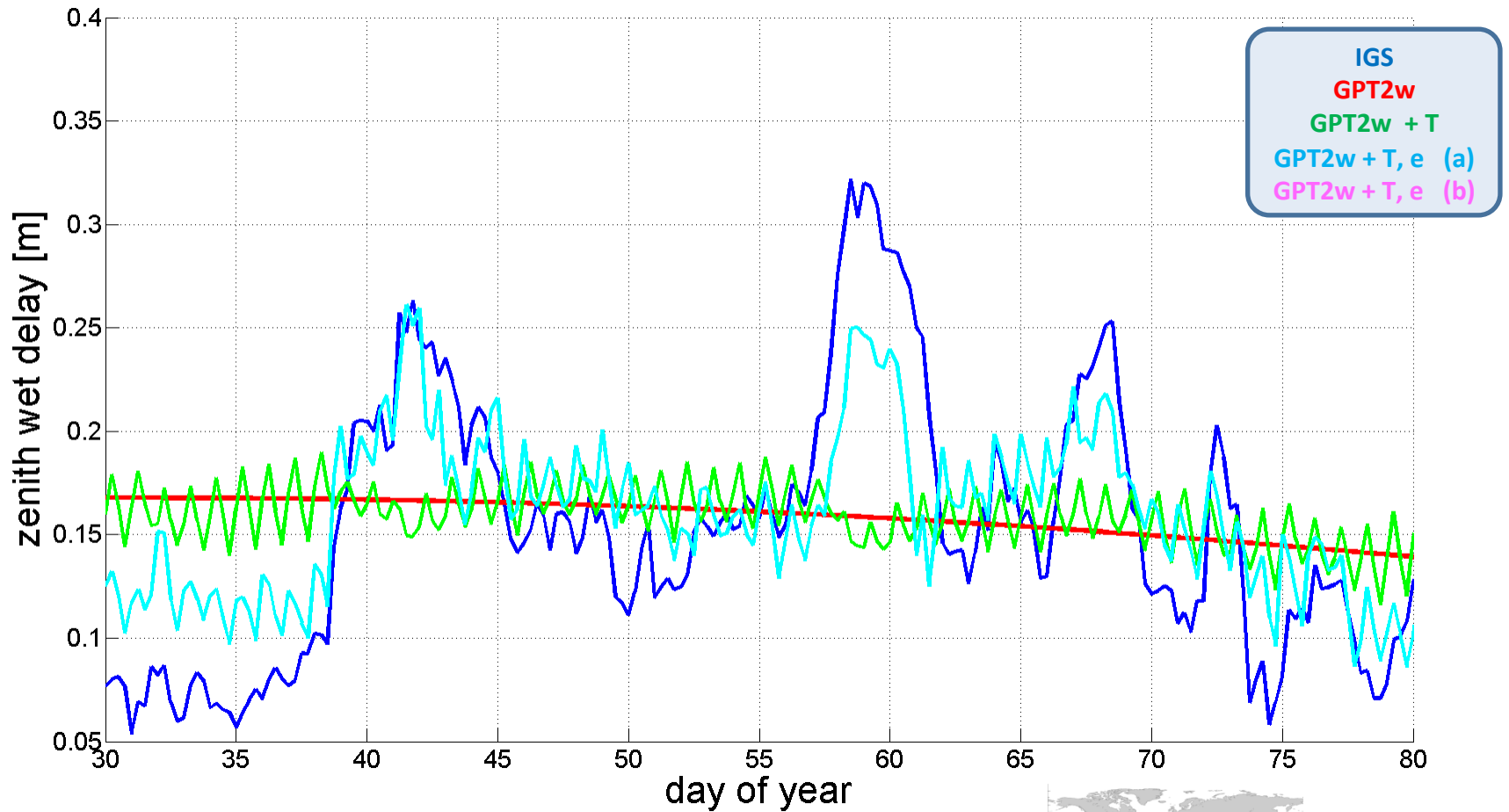
# Results



Comparison of  $\Delta L_w^z$  for ALIC



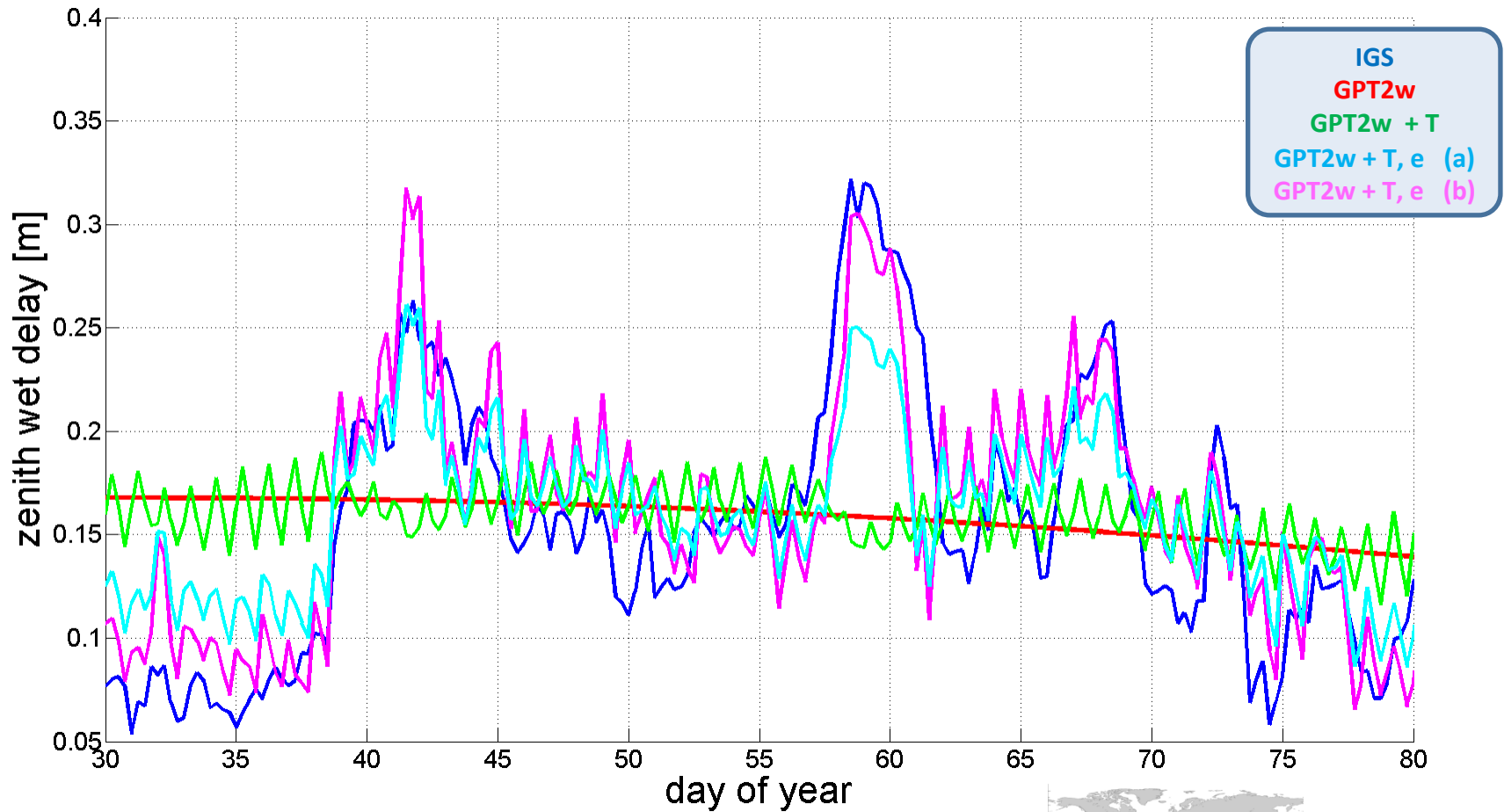
# Results



Comparison of  $\Delta L_w^z$  for ALIC



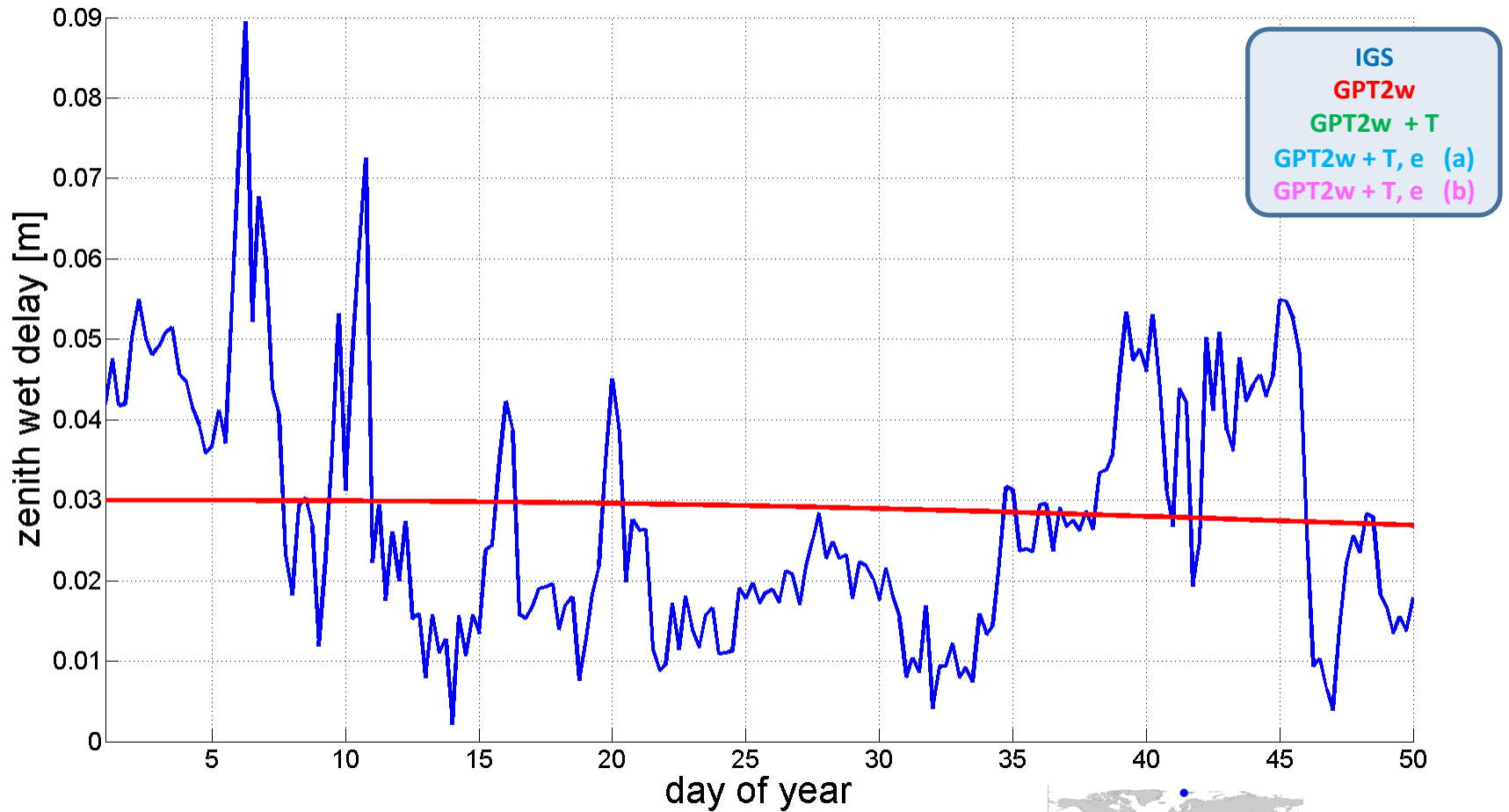
# Results



Comparison of  $\Delta L_w^z$  for ALIC



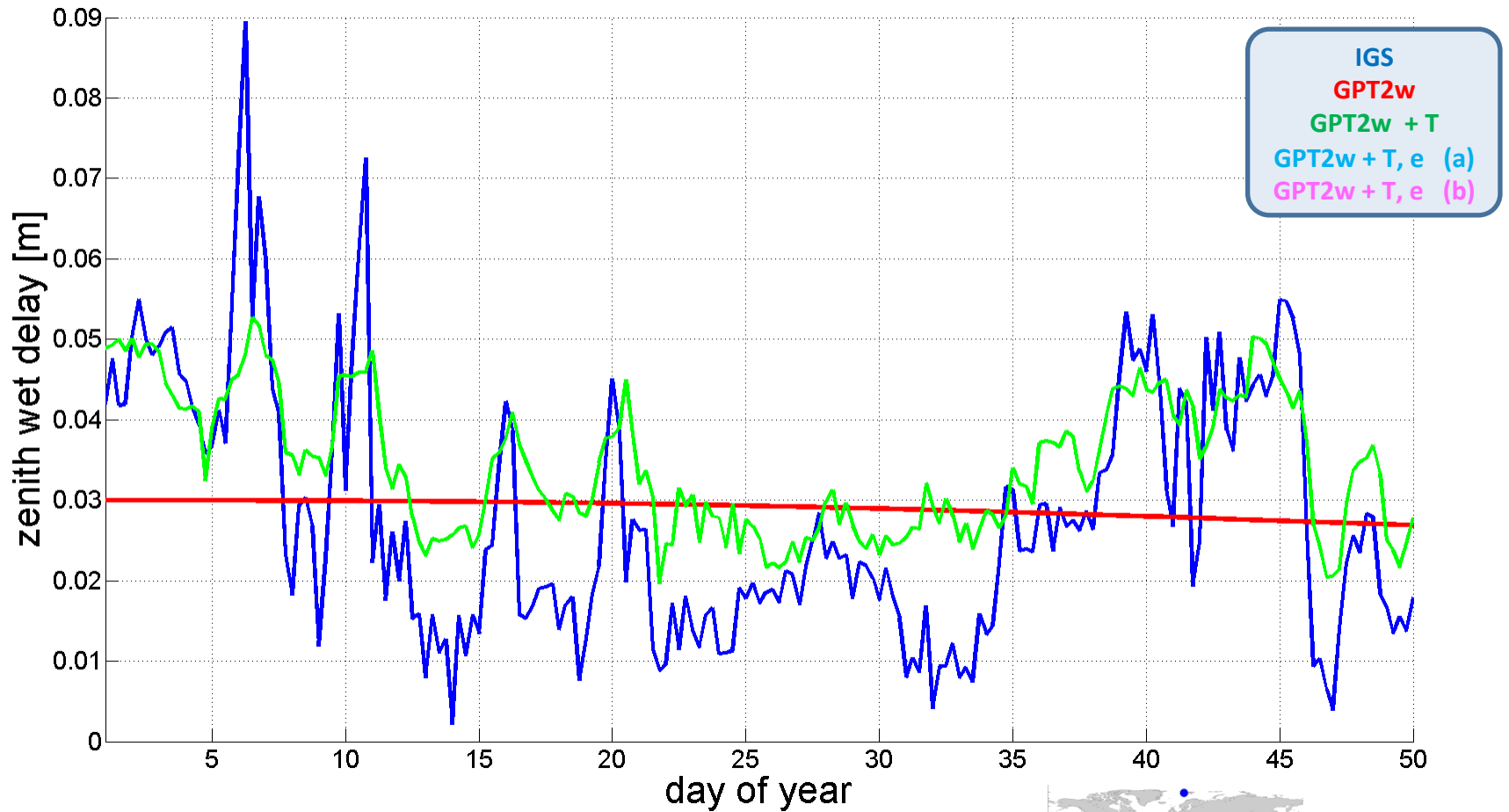
# Results



Comparison of  $\Delta L_w^z$  for NYA1



# Results

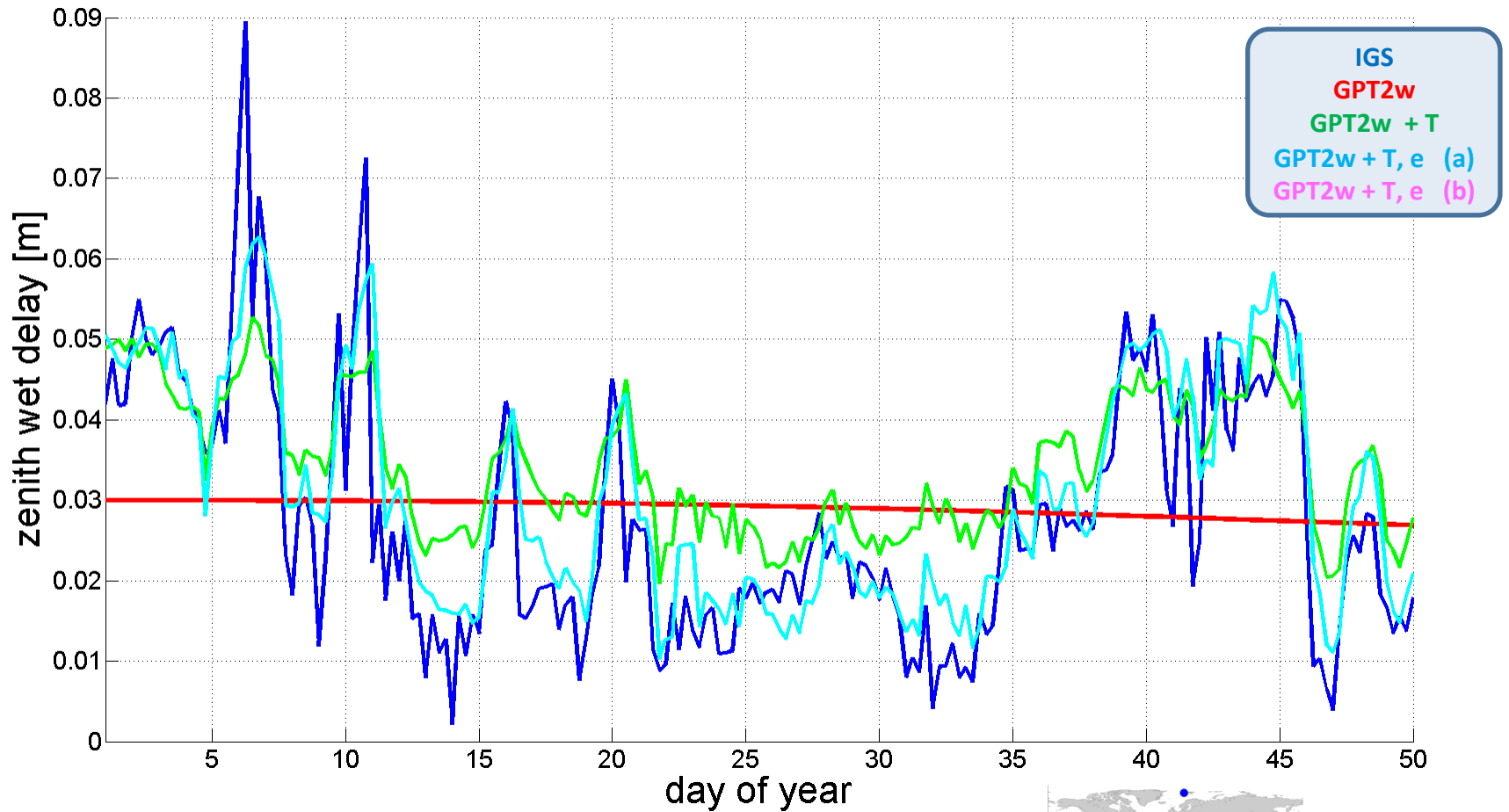


Comparison of  $\Delta L_w^z$  for NYA1





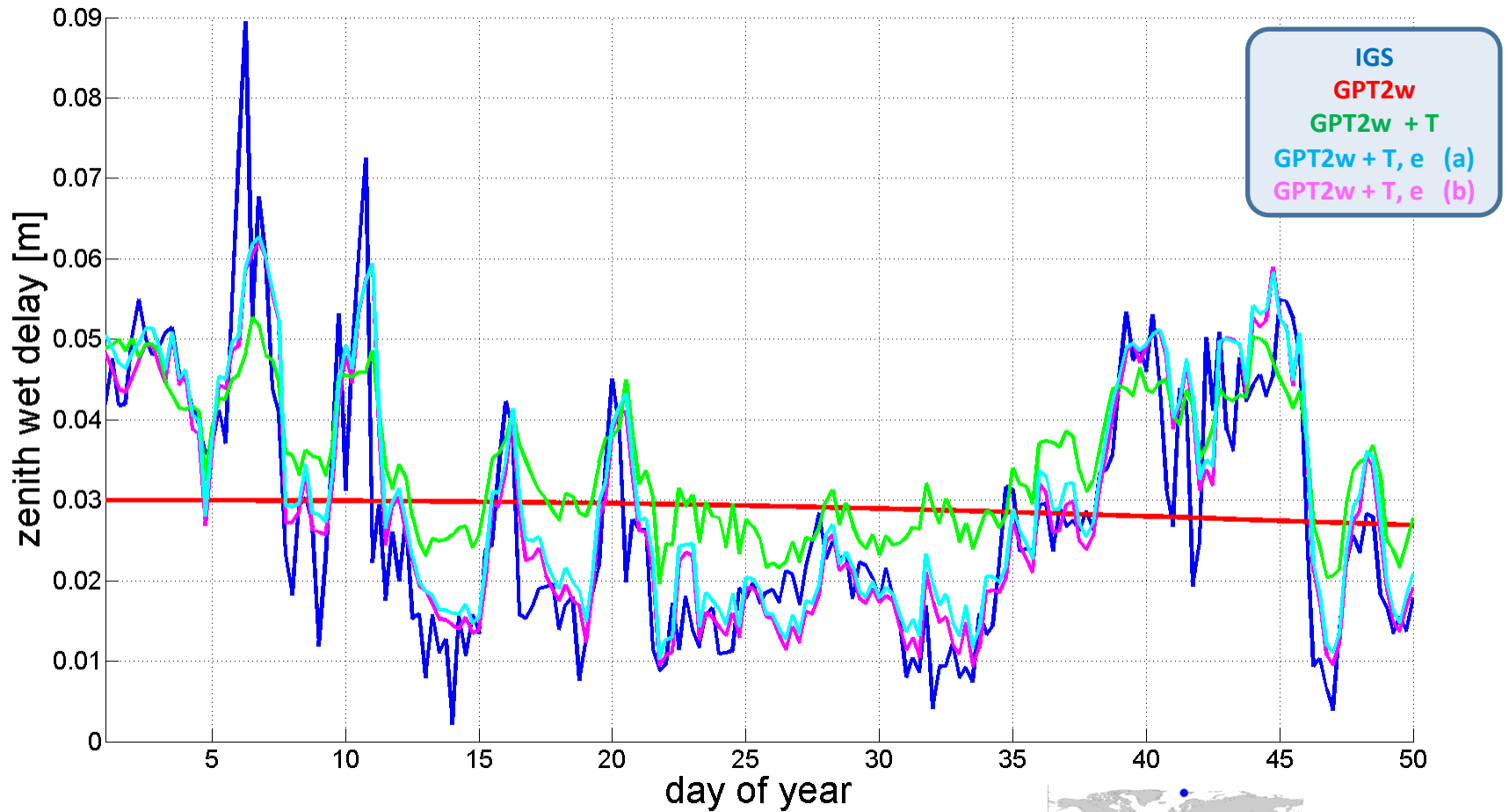
# Results



Comparison of  $\Delta L_w^z$  for NYA1



# Results



Comparison of  $\Delta L_w^z$  for NYA1



# Results

Comparison of “true”  $\Delta L_w^z$  from IGS with reproduced  $\Delta L_w^z$ :

- Mean absolute difference in  $\Delta L_w^z$  (averaged over all stations and epochs)

	$\Delta L_w^z$ [cm] (1)	$\Delta L_w^z$ [cm] (2)
empirical only (= GPT2w)	2.8	2.8
empirical + <b>T</b>	2.7	2.6
empirical + <b>T</b> and <b>e</b> (a)	<u>2.0</u>	<u>2.1</u>
empirical + <b>T</b> and <b>e</b> (b)	2.0	2.1

$$= \text{mean}(|\Delta L_{wIGS}^z - \Delta L_{wGPT2w}^z|)$$

$$= \text{mean}(|\Delta L_{wIGS}^z - \Delta L_{wGPT2wMOD(2)}^z|)$$

$$= \text{mean}(|\Delta L_{wIGS}^z - \Delta L_{wGPT2wMOD(3a)}^z|)$$

$$= \text{mean}(|\Delta L_{wIGS}^z - \Delta L_{wGPT2wMOD(3b)}^z|)$$

- Correlation coefficient (averaged over all stations and epochs)

	Corr. Coeff. (a)	Corr. Coeff. (b)
empirical only (= GPT2w)	0.70	0.73
empirical + <b>T</b>	0.73	0.76
empirical + <b>T</b> and <b>e</b> (a)	<u>0.86</u>	<u>0.86</u>
empirical + <b>T</b> and <b>e</b> (b)	0.86	0.86

# Conclusions

- GPT2w well suited for site-augmented approach using in situ measurements of **T** and **e**
- in situ measurement of **T** yields small improvement in zenith wet delay  $\Delta L_w^z$  (~5%)
- additional in situ measurement of **e** yields significant improvement in zenith wet delay  $\Delta L_w^z$  (~30%)  
=> not much difference which formula is used for **e**
- In general, best performance of site-augmented GPT2w is achieved in dry regions

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