

GALILEO on board the International Space Station and highly accurate GNSS/ACES time and frequency transfer based on phase clocks

Drazen SVEHLA¹, Markus ROTHACHER², Marek ZIEBART³, Christophe SALOMON⁴

¹Technical University of Munich, Germany

²GeoForschungsZentrum Potsdam, Germany

³University College London, UK

⁴Laboratoire Kastler Brossel, Ecole Normale Supérieure,
Universite Pierre and Marie Curie, Paris, France

ACES Mission on board ISS

ACES= **A**tomic **C**lock **E**nsemble in **S**pace

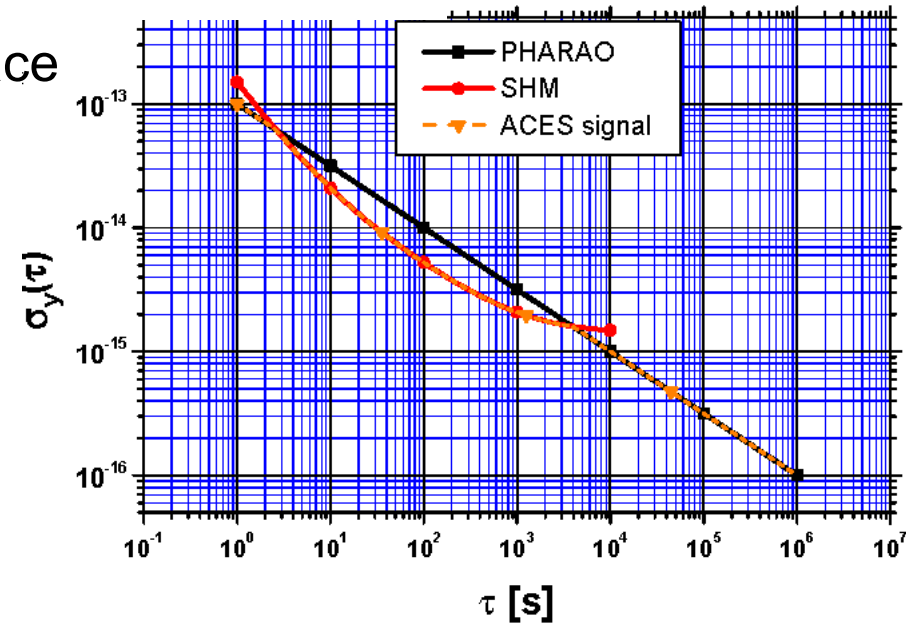
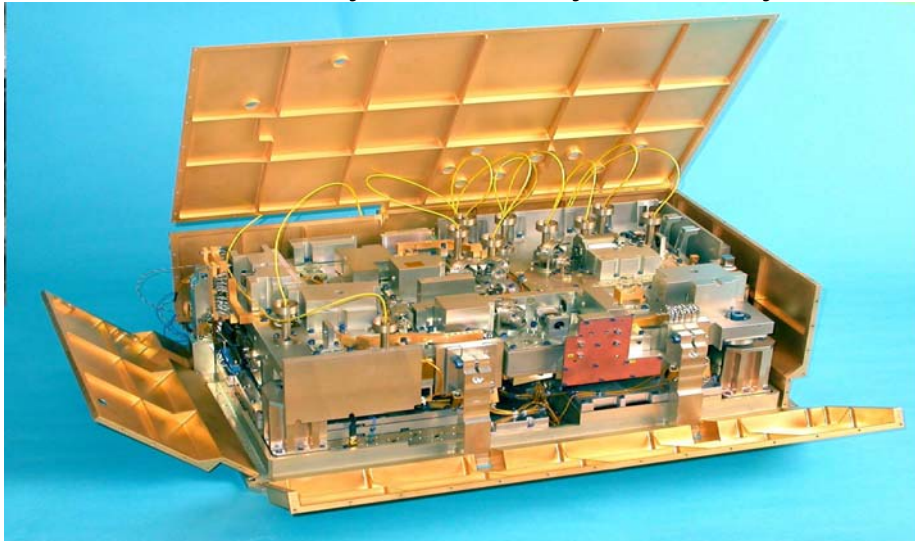
Launch date: 2010

Mission duration: 18 months

Scientific objectives:

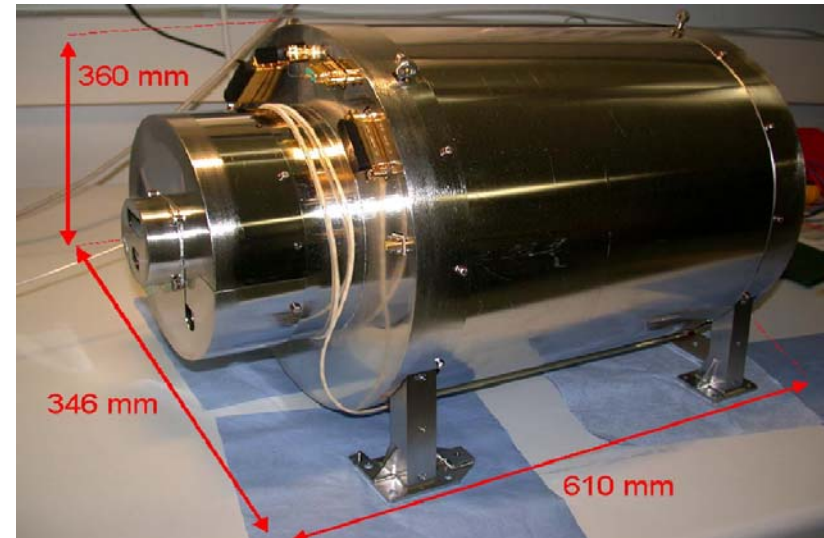
- Tests of general relativity (red-shift)
- Tests of fundamental physics (variations in α)
- Time and frequency transfer

PHARAO - Cold atom clock (cesium fountain)
long term performance, $\tau > 45$ min,
stability & accuracy 10^{-16} /day



Space H-maser

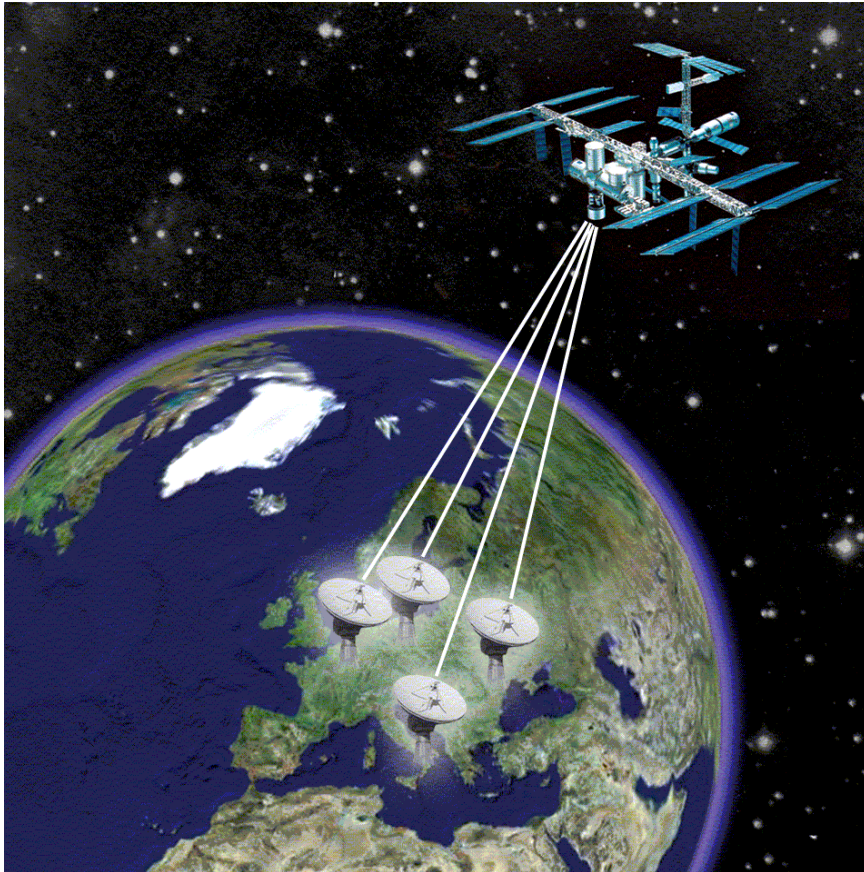
short term performance, $\tau < 45$ min



(Cacciapouti, Dimarcq, Salomon, 2005)

Common View

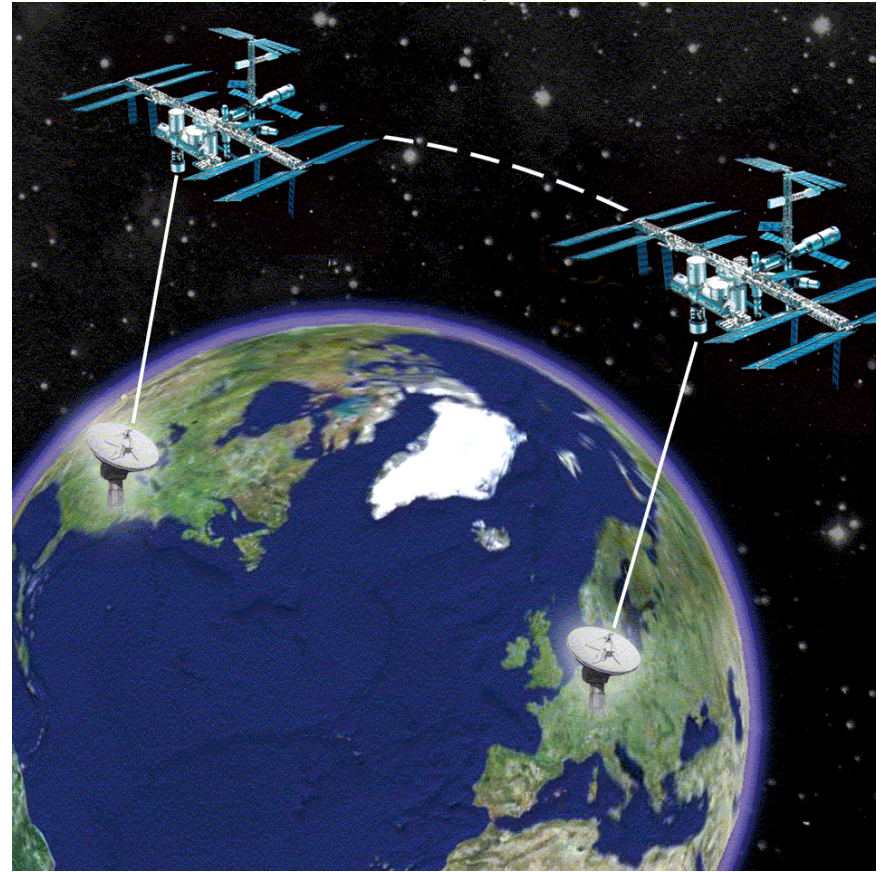
Ground to ground clock comparison
Governed by short-term stability
< **0.3 ps** over one ISS pass (300 s)



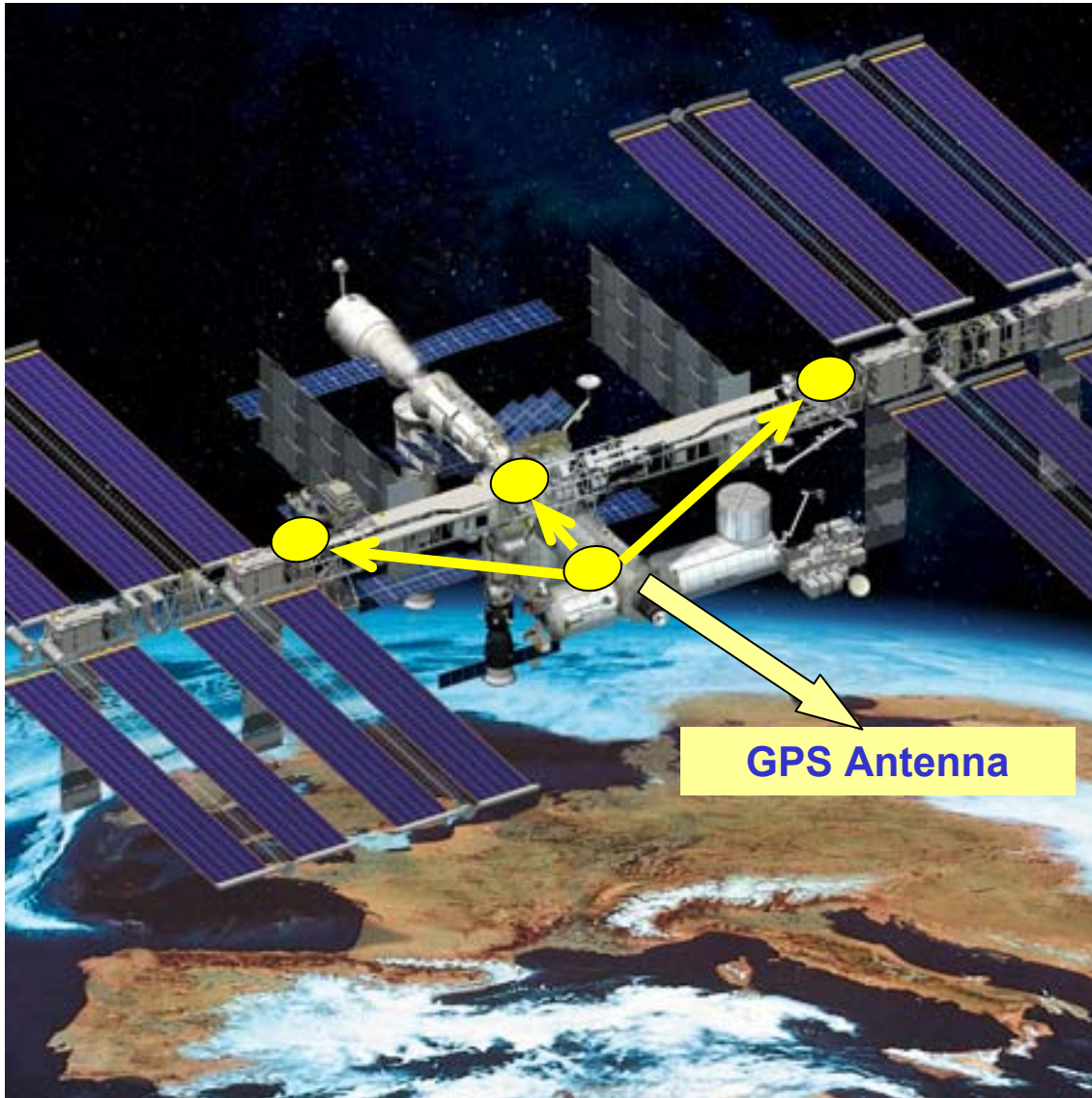
(Aguilar et al. 2005 ACES Workshop)

Non-Common View

Ground-to-space-to-ground clock comparison
Governed by long term stability
< **2 ps** for 1000 s time interval
< **20 ps** for 1 day time interval



ISS Reference System



One or four
GPS/GALILEO Antennas:

- Attitude
- ISS deformation
- Space Shuttle docking

Centre of Mass monitoring
("geocentre")

ISS dynamics monitoring fully
geometrically

Atmosphere density retrieval
using ISS as a sensor

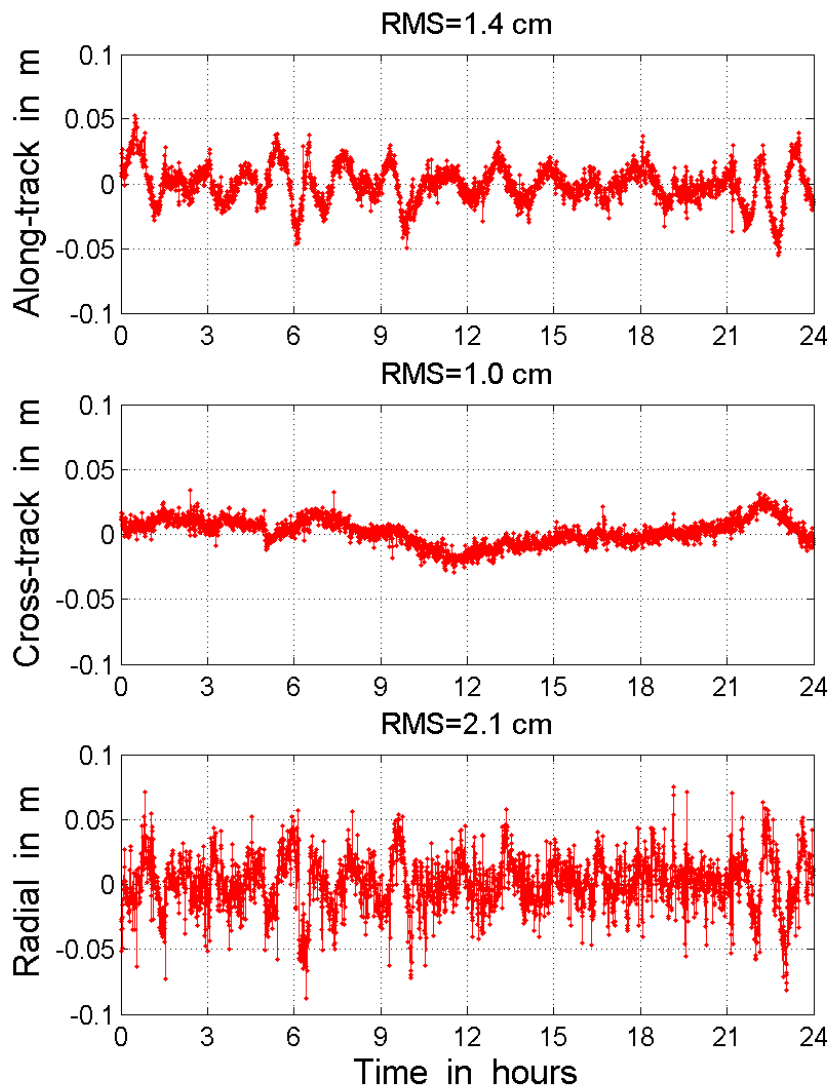
Proposal submitted to the ESA Announcement of Opportunity: Life and Physical Sciences and Applied Research Projects 2004

We proposed to ESA to place a geodetic dual-frequency GPS/Galileo receiver on board the Space Station including a set of one/four GPS/GALILEO antennas in order to:

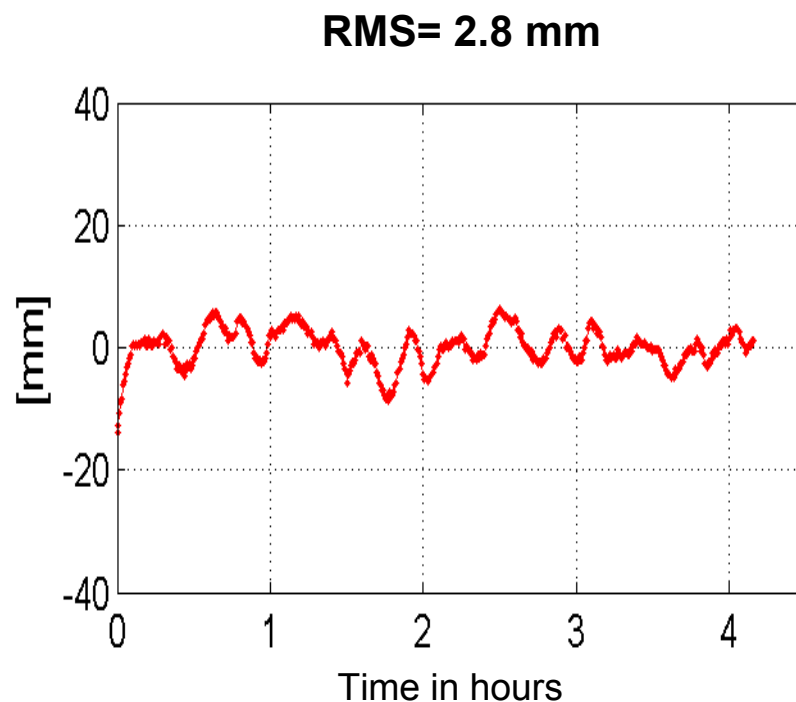
1. establish a highly accurate **reference system for the ISS** and its local environment
 - to monitor ISS centre of mass
2. Space Station **kinematic and reduced-dynamic POD** with an accuracy of 1-3 cm
 - to monitor ISS dynamics fully geometrically
3. compute the relative positions between the **three/four GPS antennas** with the mm-accuracy
 - high-precision attitude information
 - relative positioning of the "Canadian arm" or the Space Shuttle docking
 - monitor deformation of the ISS platform
4. use the ISS solar panels as a sensor to retrieve **atmosphere density** and derive **TEC**
 - ISS orbits close to equator ($i=51.6^\circ$)
5. Galileo/GPS precise **time/frequency transfer**
 - Galileo/GPS receiver driven by the external frequency from the ACES clock ensemble

Motivation – 3 Different POD Strategies

Kinematic POD GRACE-A



GRACE GPS Baseline with FIXED ambiguities



(Status 2003-2004)

Reduced-Kinematic POD

CHAMP day 200/2002

Kinematic POD with dynamic information in order to reduce influence of weak geometry and phase breaks (jumps).

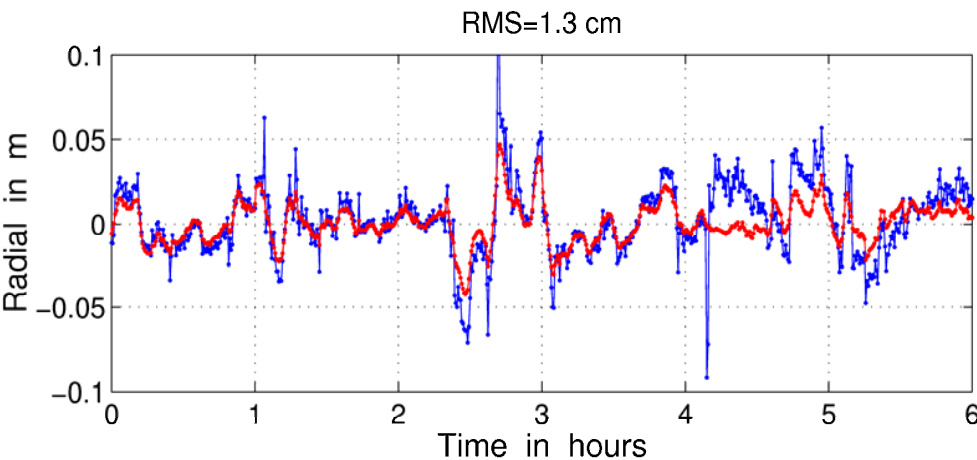
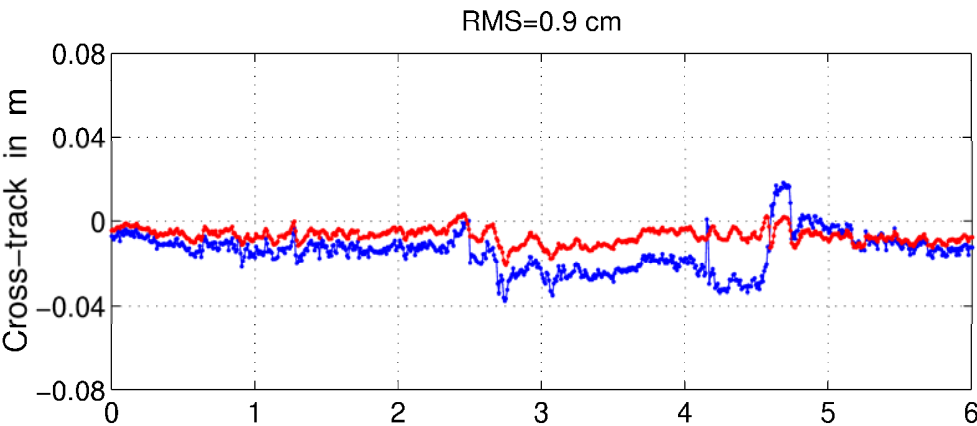
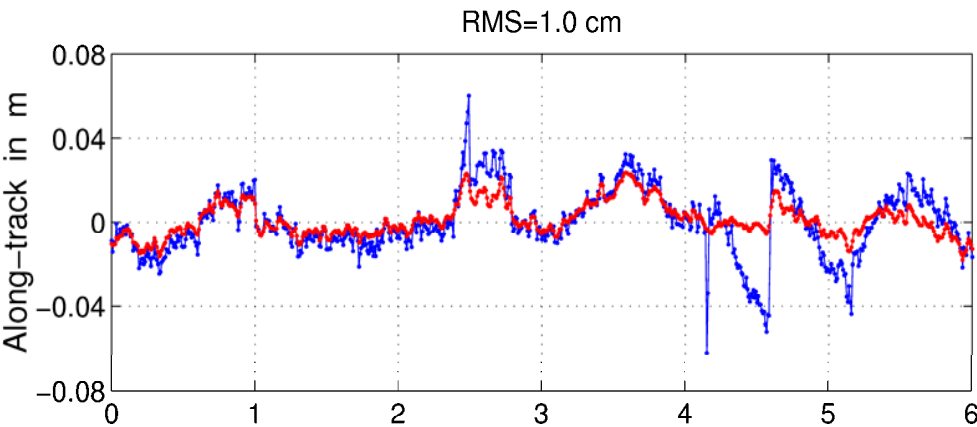
Methods:

- Absolute constraints to the a priori orbit
- **Relative constraints (applied to kinematic position differences over time w.r.t. corresponding differences stemming from the dynamic orbit)**
- Gauss-Markov process

Normal system solution:

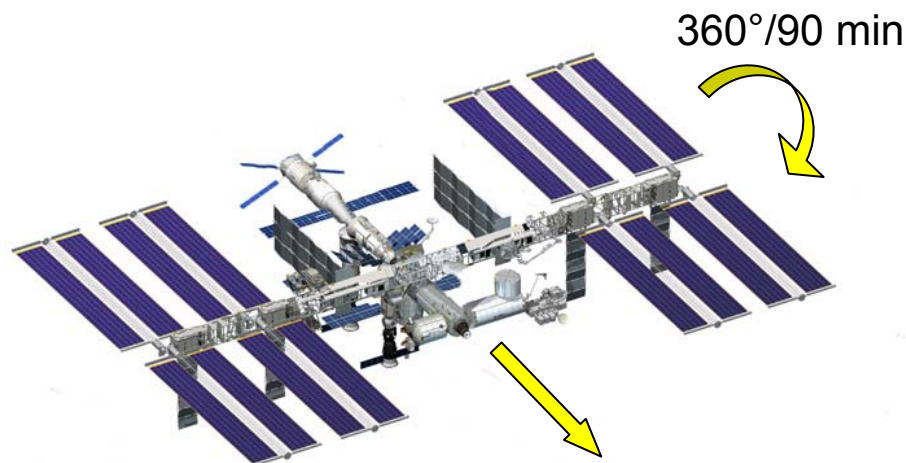
- Full normal matrix inversion (86400 kinematic coordinates for one-day arc)
- $L - U$ factorization (block tridiagonal system), block forward elimination and back substitution.

Characteristics:
Smoothing effect

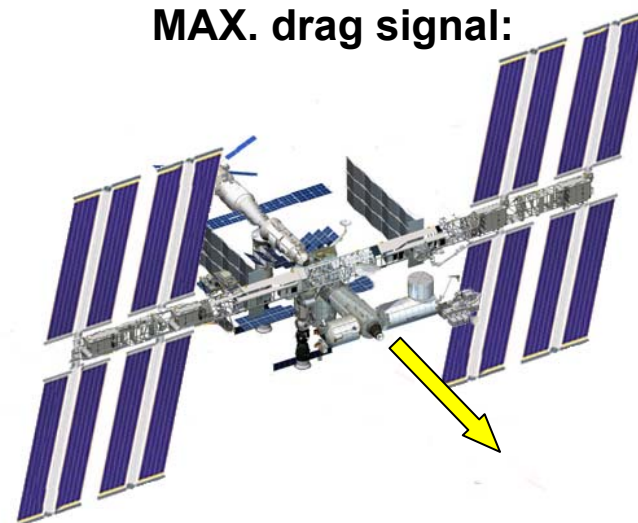


Retrieving the air density using Space Station as a sensor

MIN. drag signal:



MAX. drag signal:



360°/90 min

Form factor considerably larger for ISS compared to CHAMP and GRACE

Drag signal considerably larger than gravity field errors.

Around 2010-2012 solar maximum to be expected (**max. drag signal**).

Multipath: almost clean antenna horizon (since several ISS modules cancelled)

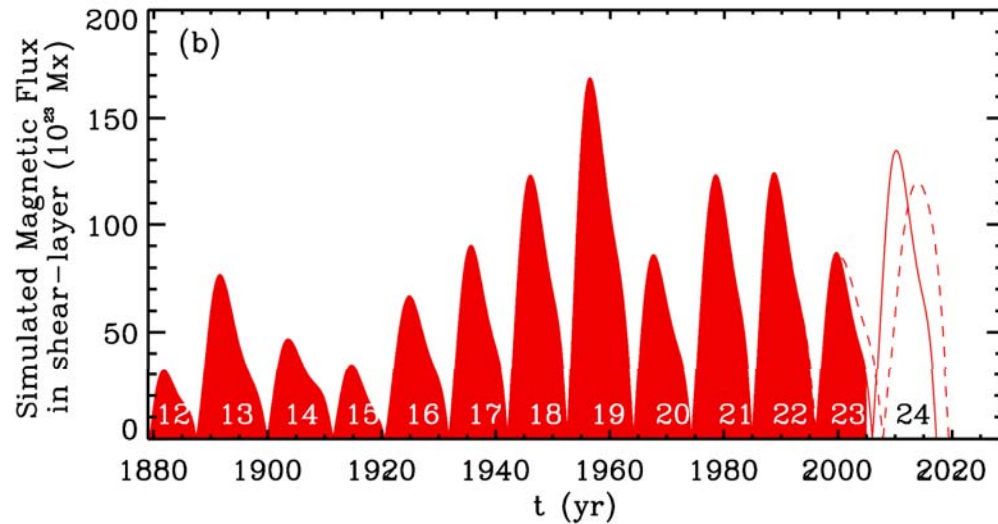
No near field multipath (top of Columbus)

atmospheric density

$$a = \frac{1}{2} C_d \rho v_r^2 \frac{A}{m}$$

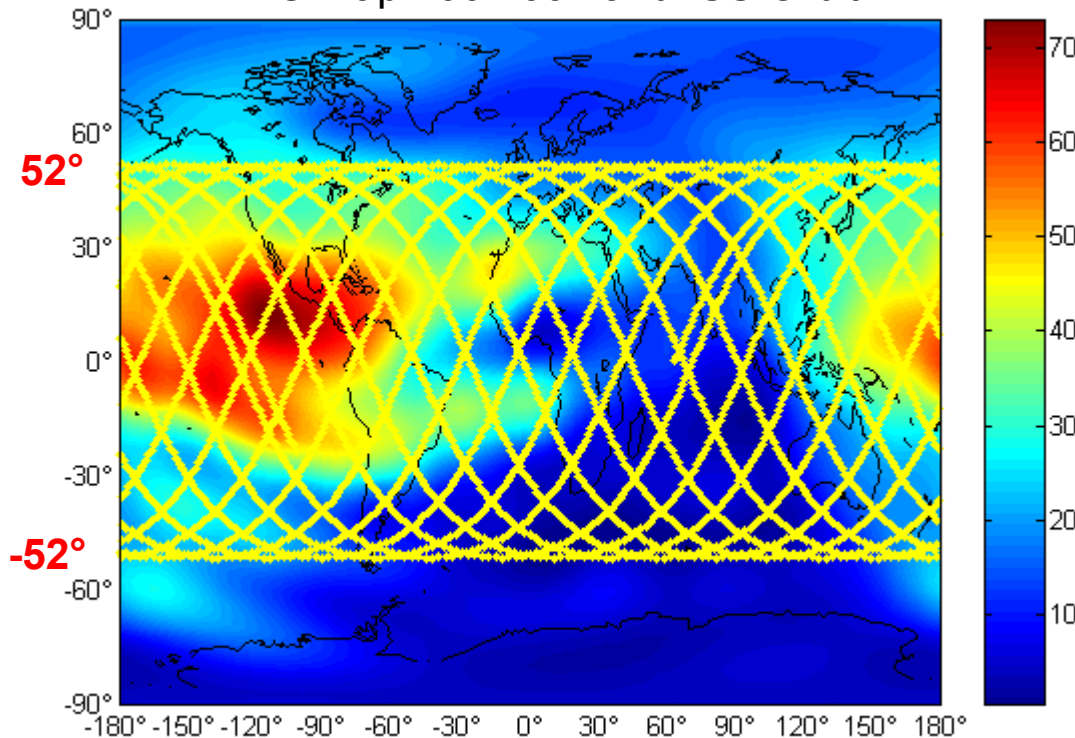
a → atmospheric drag
 C_d → cross section area
 ρ → atmospheric density
 v_r → LEO velocity relative to the atmosphere
 A → cross section area
 m → mass of the satellite

Solar Maximum in 2010-2012



The next solar max. will be 30-50% stronger than the last one (GRL paper, Dikpati et al. 2006)

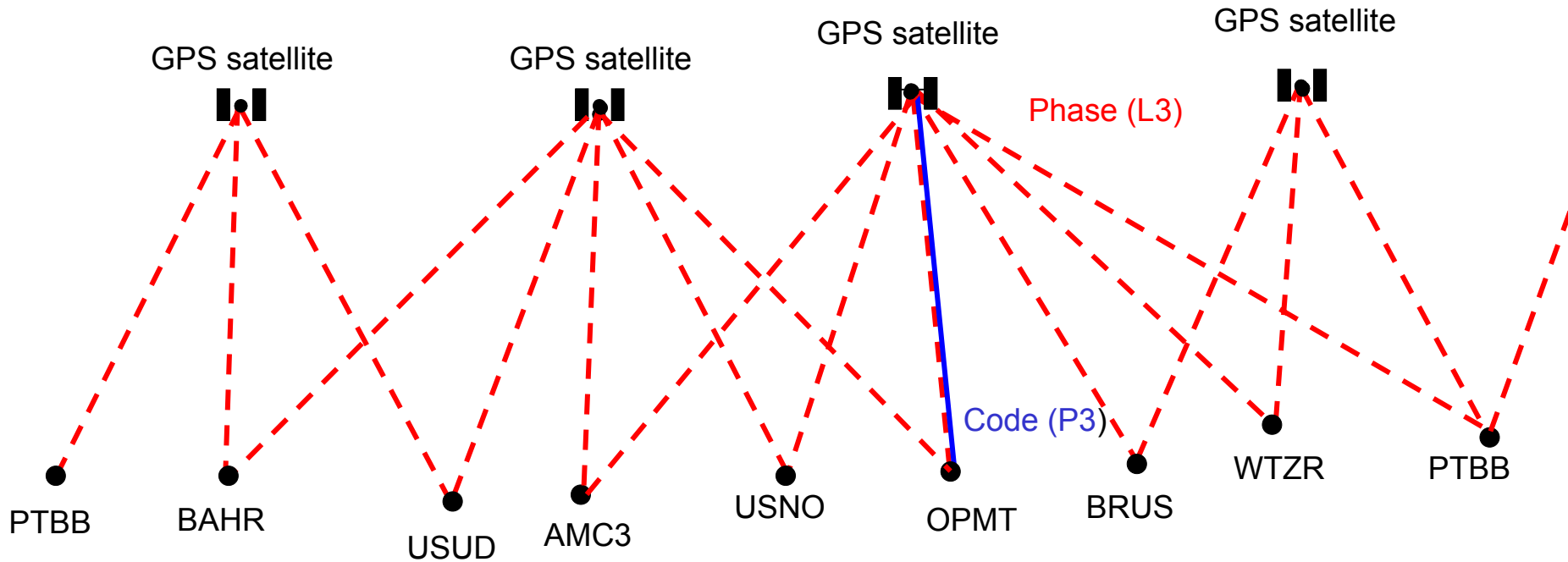
TEC map 200/2002 and ISS Orbit



ISS orbits close to equator
Inclination = **51.6°**

Phase Clocks

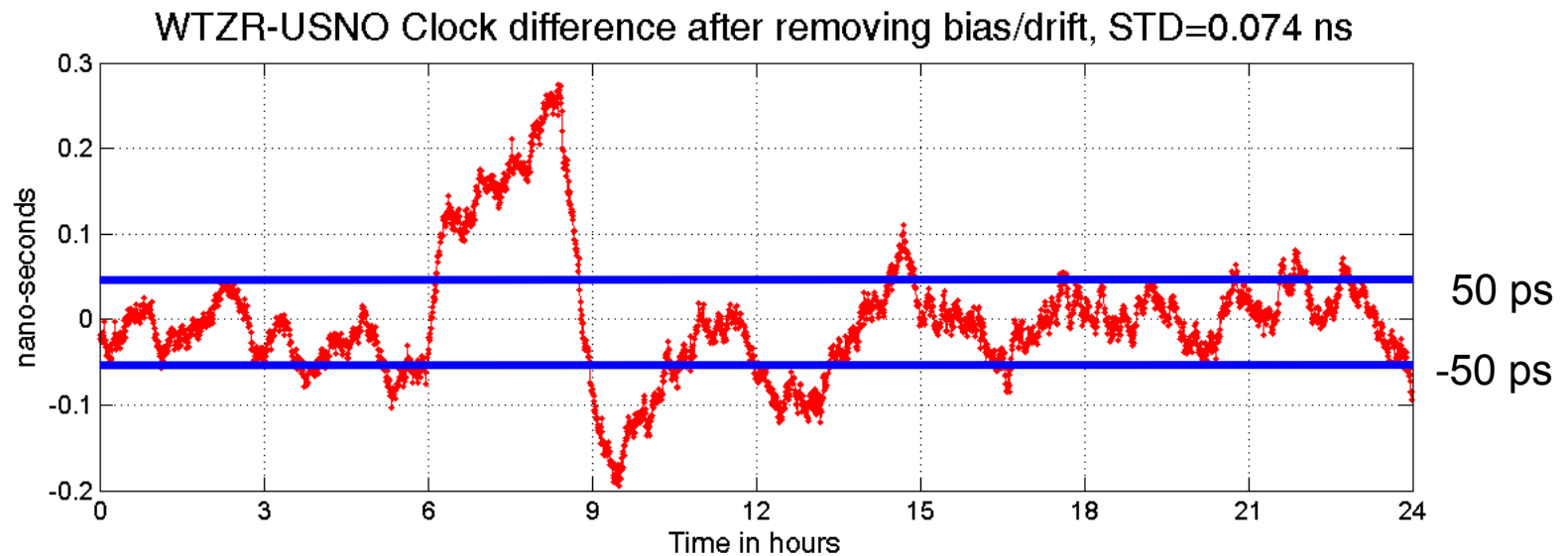
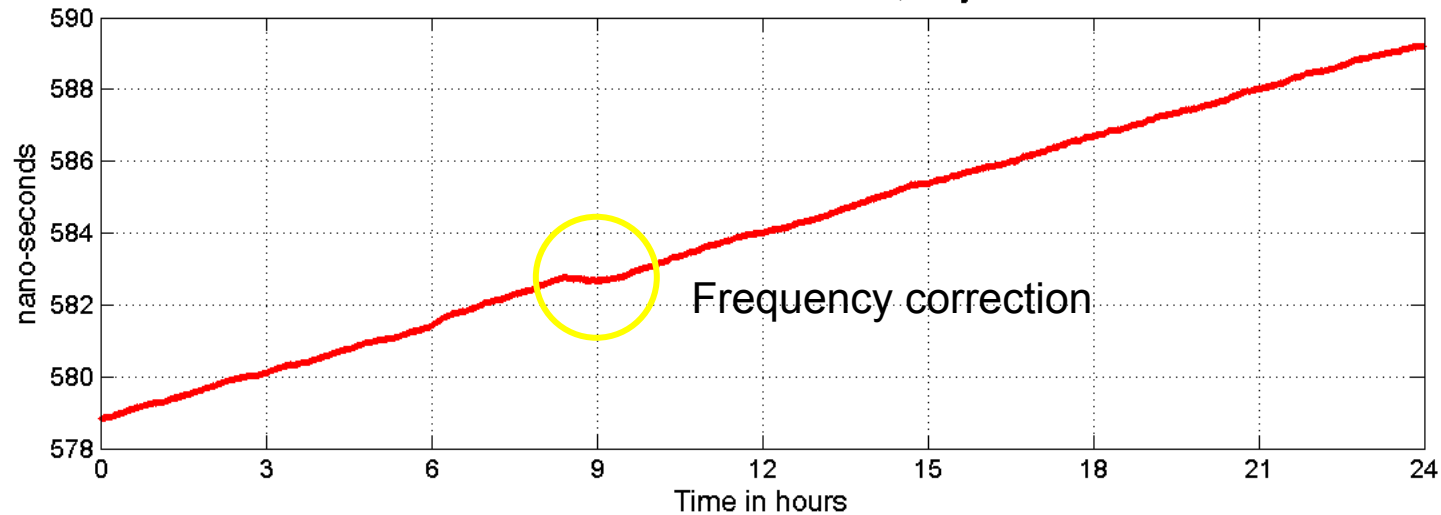
- **PHASE CLOCKS:** GPS satellite/station clocks estimated using **only phase data**
- **Estimated Parameters :** GPS/station clock parameters every 30 sec + ambiguities
- one clock bias over all clock labs (PPP is done using phase data only)
- code measurements only for approximate clock synchronization
- **code noise+multipath+DCBs+ICB are avoided**
- combined GALILEO/GPS solutions: inter-GNSS clock bias absorbed by ambiguities



Clock comparison using Phase Clocks

(Wetzell, Germany – USNO, US)

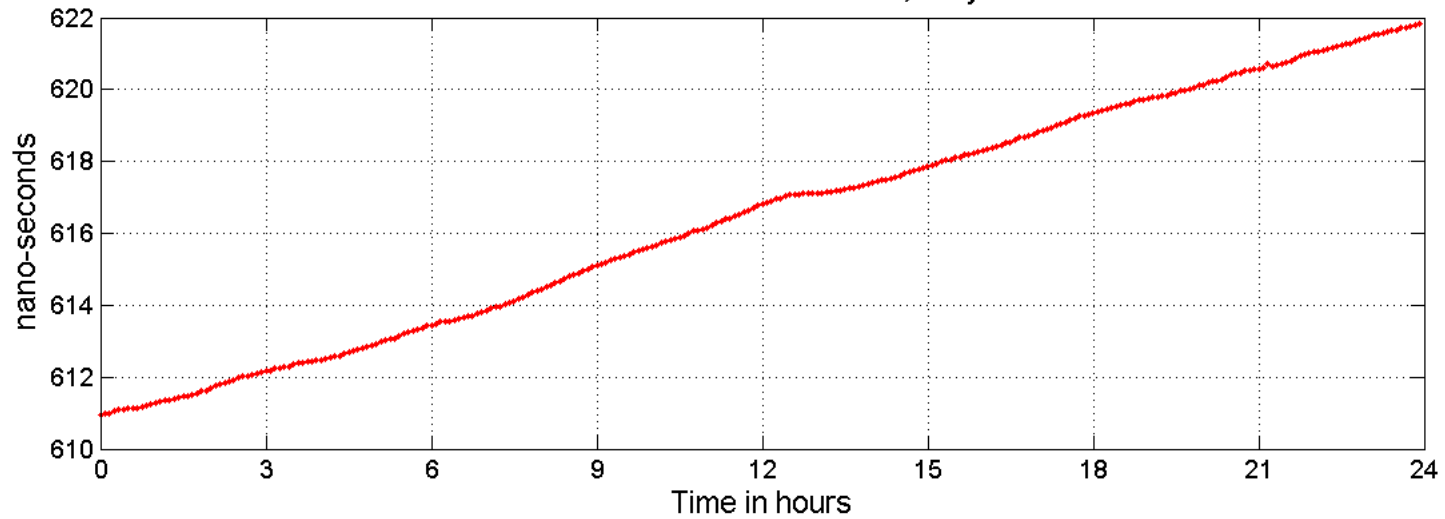
WTZR-USNO Clock difference, day 197/2003 (Status 2003-2004)



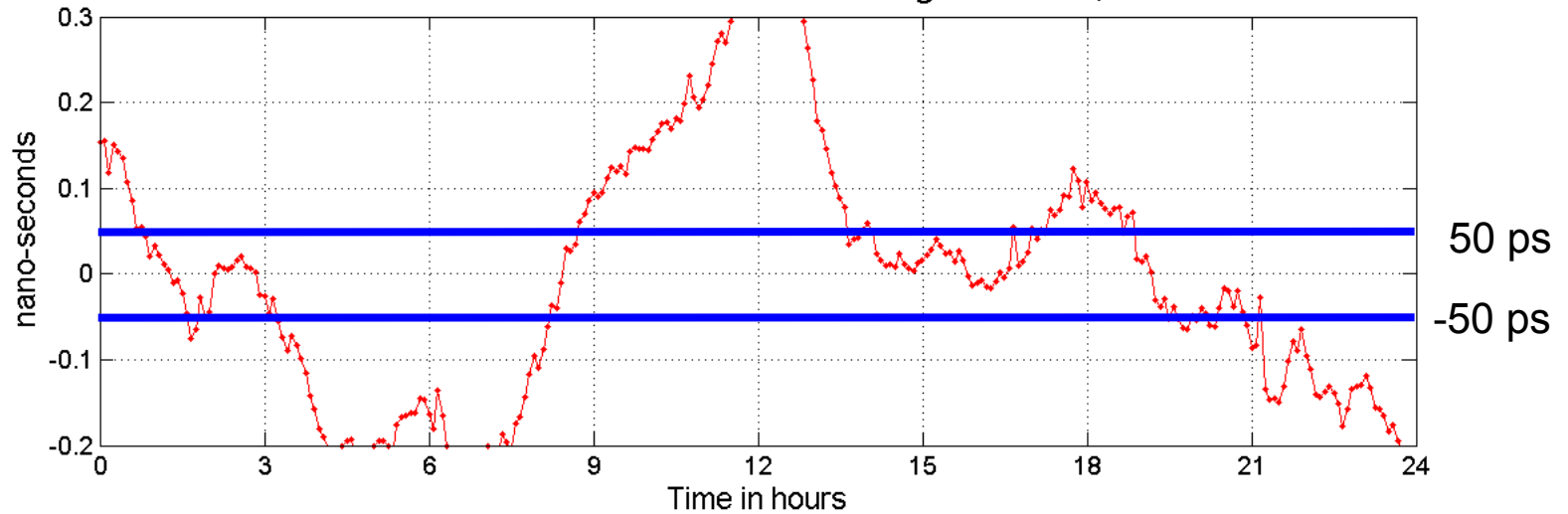
Only phase clocks estimated. Troposphere (TZD), station coord., EOPs, etc., fixed to IGS

CODE 5-min Clock

WTZR-USNO Clock difference, day 200/2003



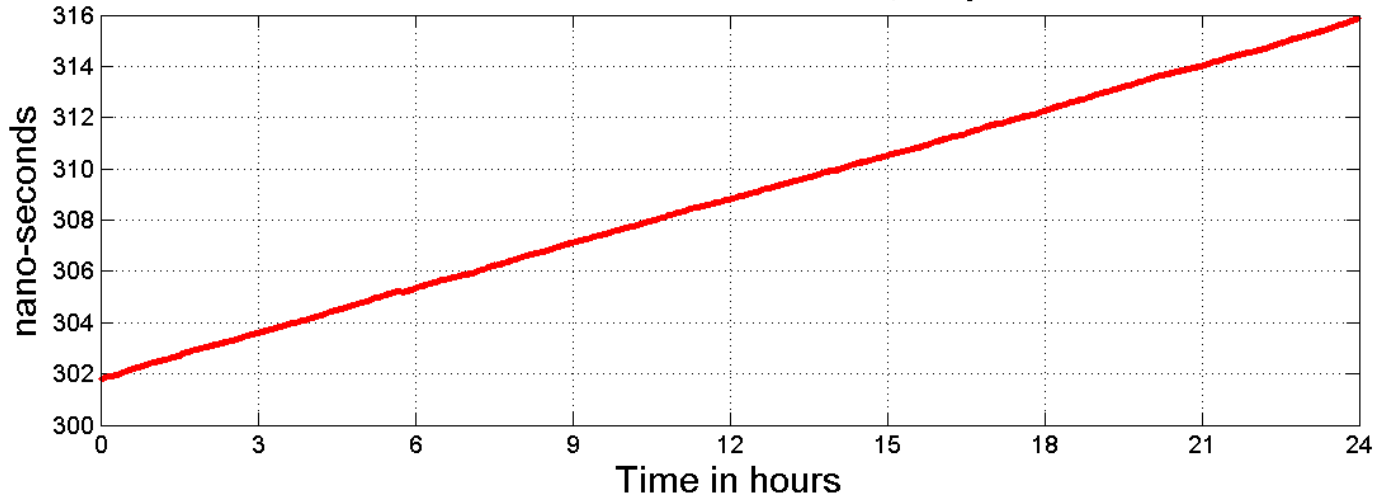
WTZR-USNO Clock difference after removing bias/drift, STD=0.151 ns



Clock comparison using Phase Clocks

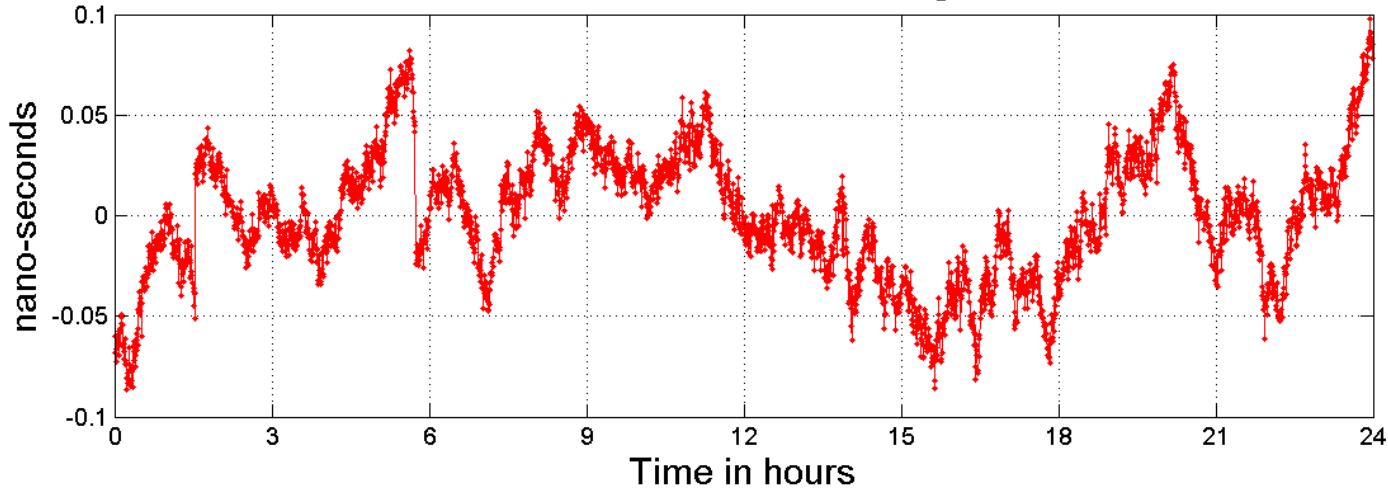
(Westerbork, The Netherlands – USNO, US)

WSRT-USNO Clock difference, day 196/2003



1cm \approx 33 ps

WSRT-USNO Clock difference after removing bias/drift, STD=0.032 ns



(3.7×10^{-16})

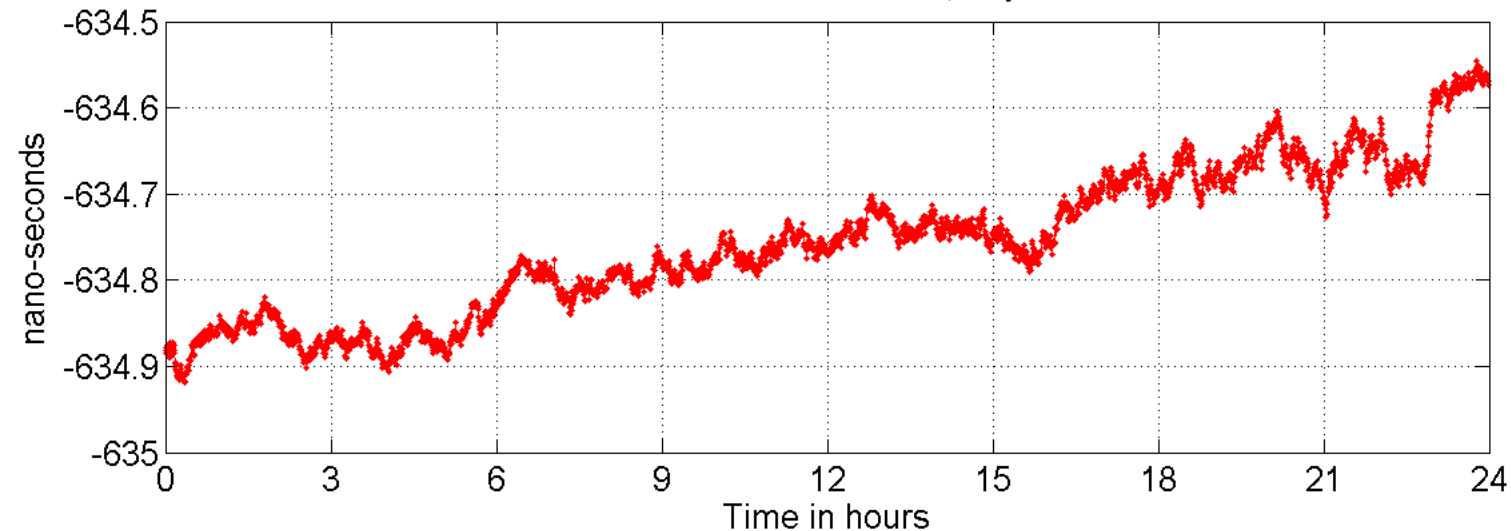
\approx 9 mm

Only phase clocks estimated. Troposphere (TZD), station coord., EOPs, etc., fixed to IGS

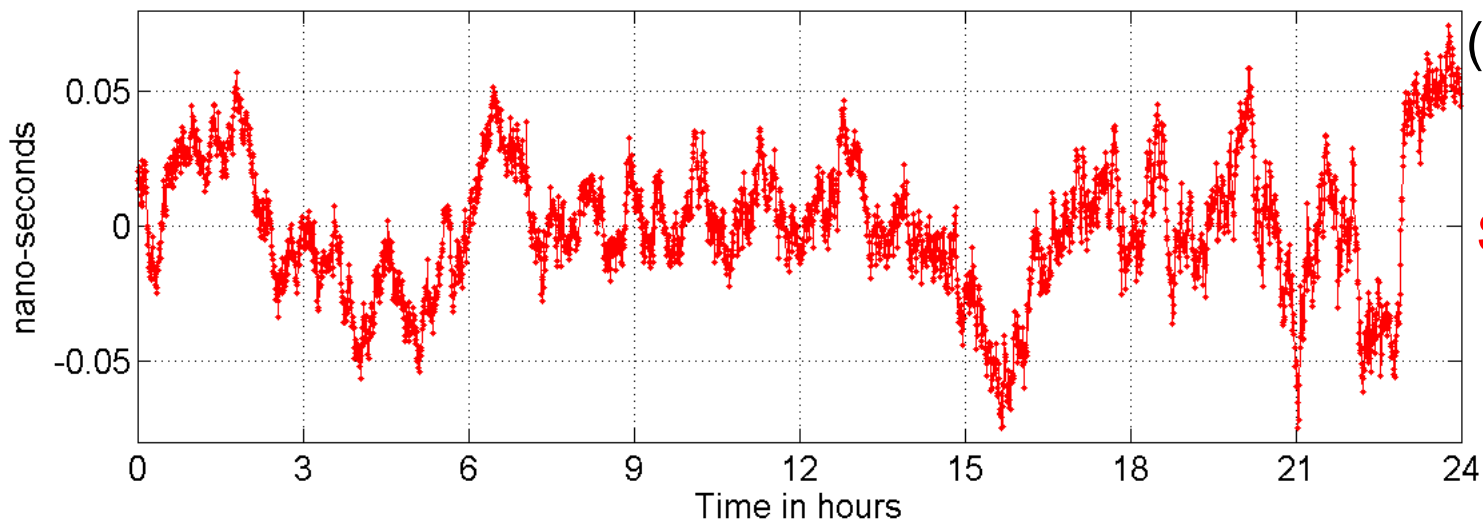
Phase Clocks

AMC2-USNO Clock difference, day 196/2003

(Colorado Springs – USNO)



AMC2-USNO Clock difference after removing bias/drift, STD=0.025 ns



$(2.9 \times 10^{-16}$ per day)

≈ 7 mm

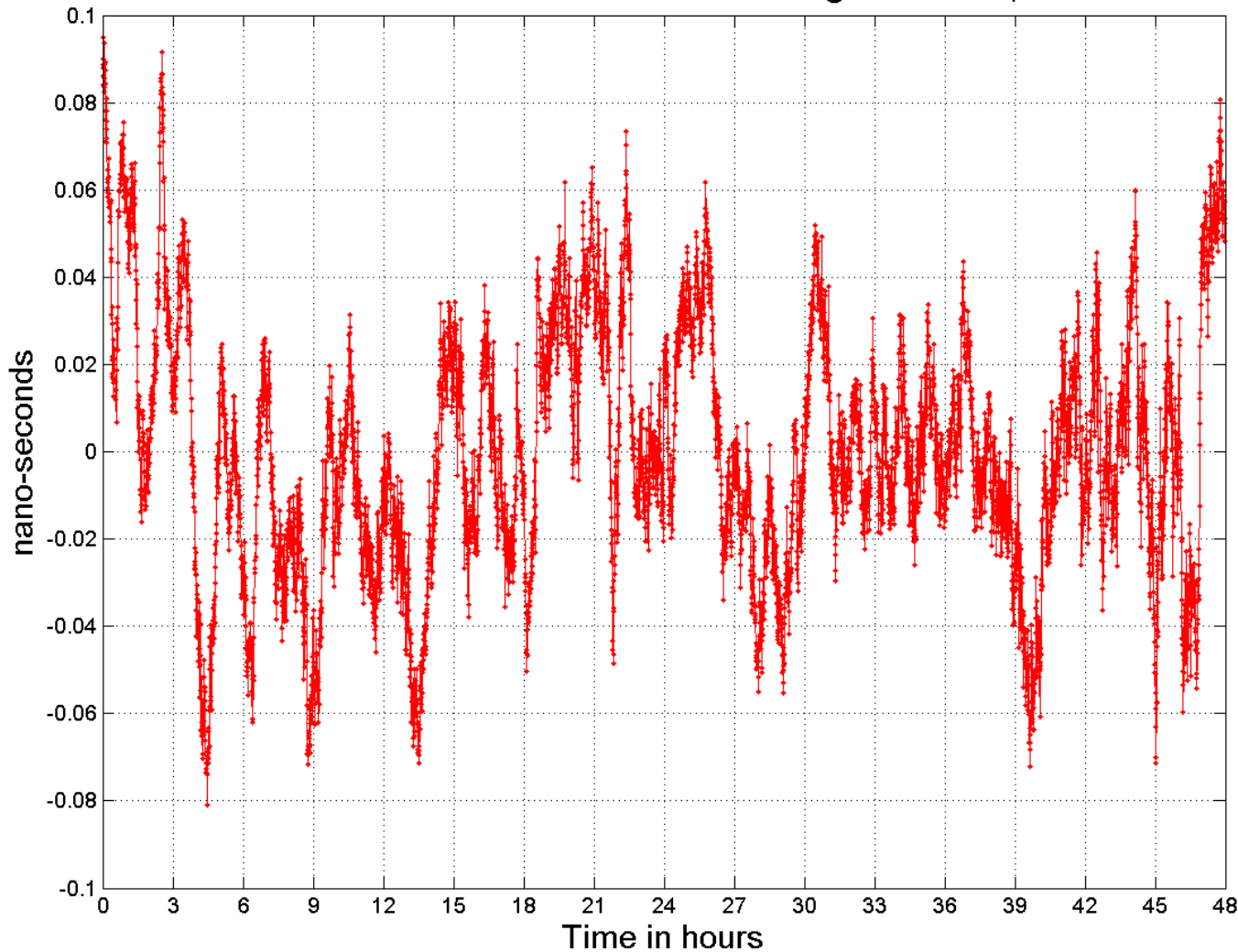
Stability of GPS
receiver and
H-maser

Only phase clocks estimated. Troposphere (TZD), station coord., EOPs, etc., fixed to IGS

Phase Clocks over several days

(Colorado Springs, US – USNO, US)

AMC2-USNO Clock difference after removing bias/drift, STD=0.029 ns



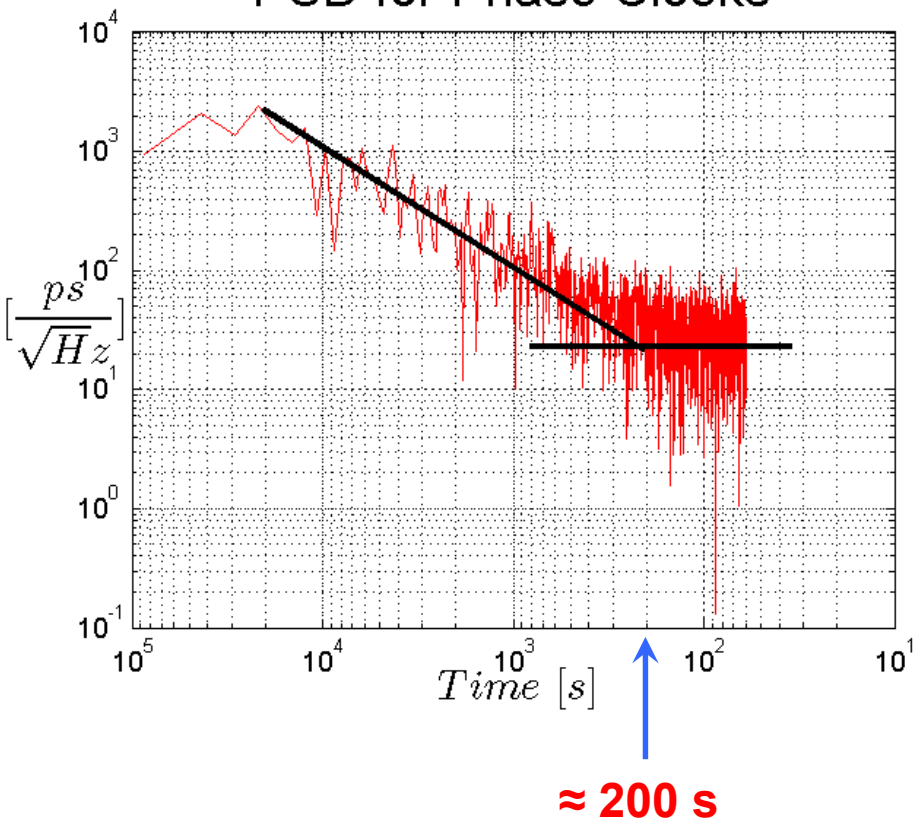
1cm \approx 33 ps

relative
precision
(3.3×10^{-16})

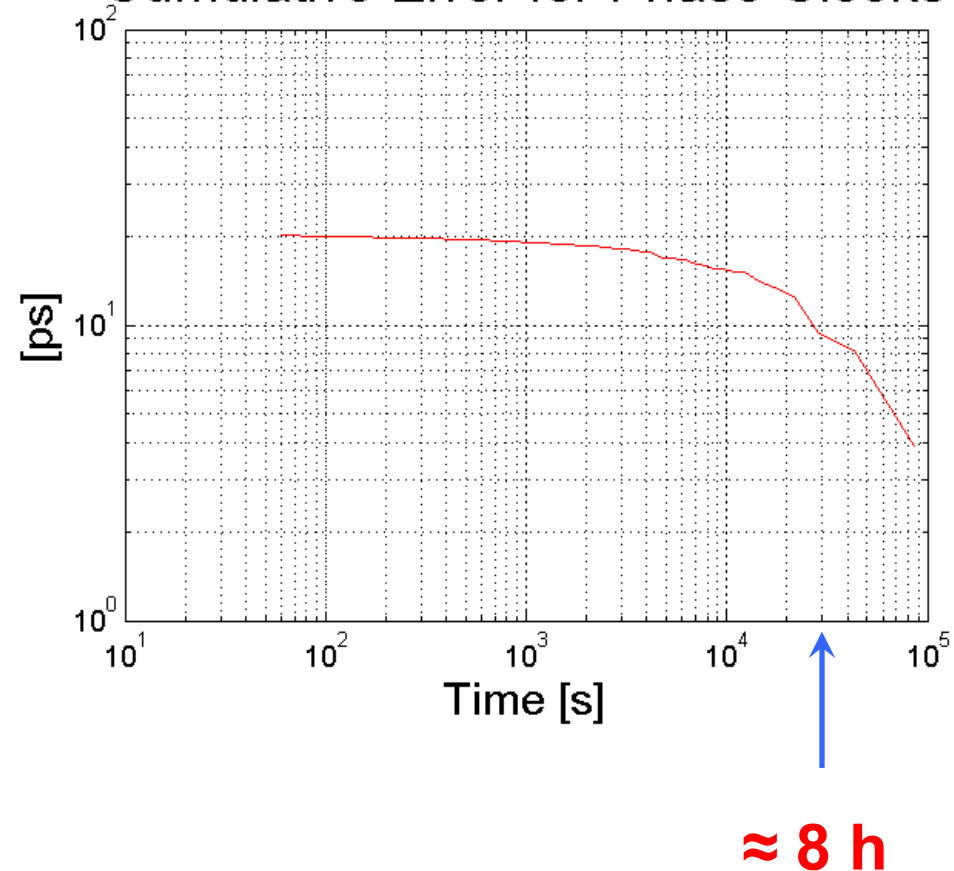
Only phase clocks estimated. Troposphere (TZD), station coord., EOPs, etc., fixed to IGS

Phase Clock – Power Spectral Density

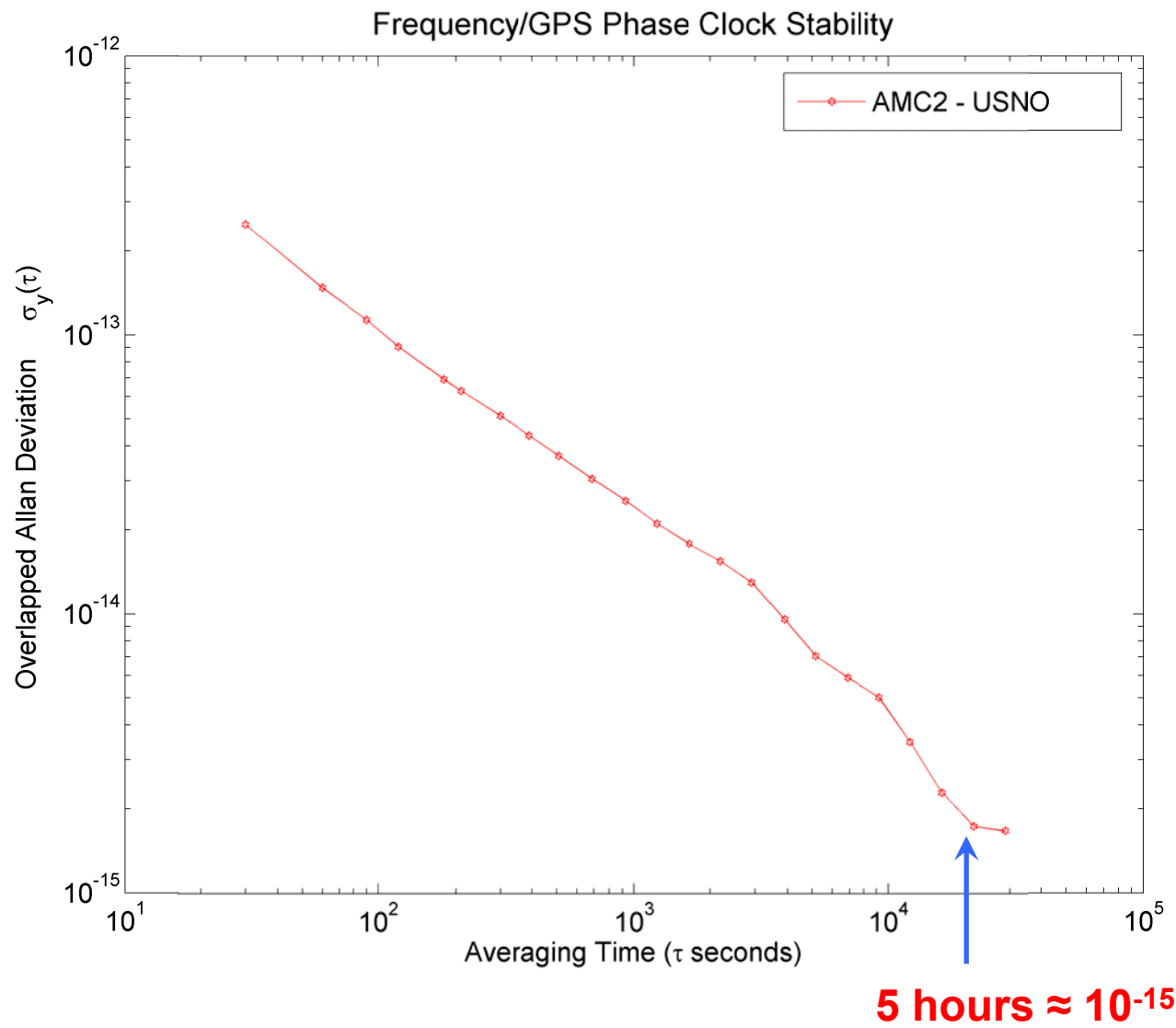
PSD for Phase Clocks



Cumulative Error for Phase Clocks



Phase Clocks - Allan Deviation



Allan deviation computed
using the program
CANVAS

Simulation of the GPS, GALILEO and MWL measurements for the SPACE STATION

Space Station: $i=51.6^\circ$, altitude=400 km

GPS constellation + **GALILEO** constellation = 58 satellites

ground clock labs

GPS observables:

L1, L2 $\sigma(L1)=\sigma(L2)= 3$ mm

GALILEO observables:

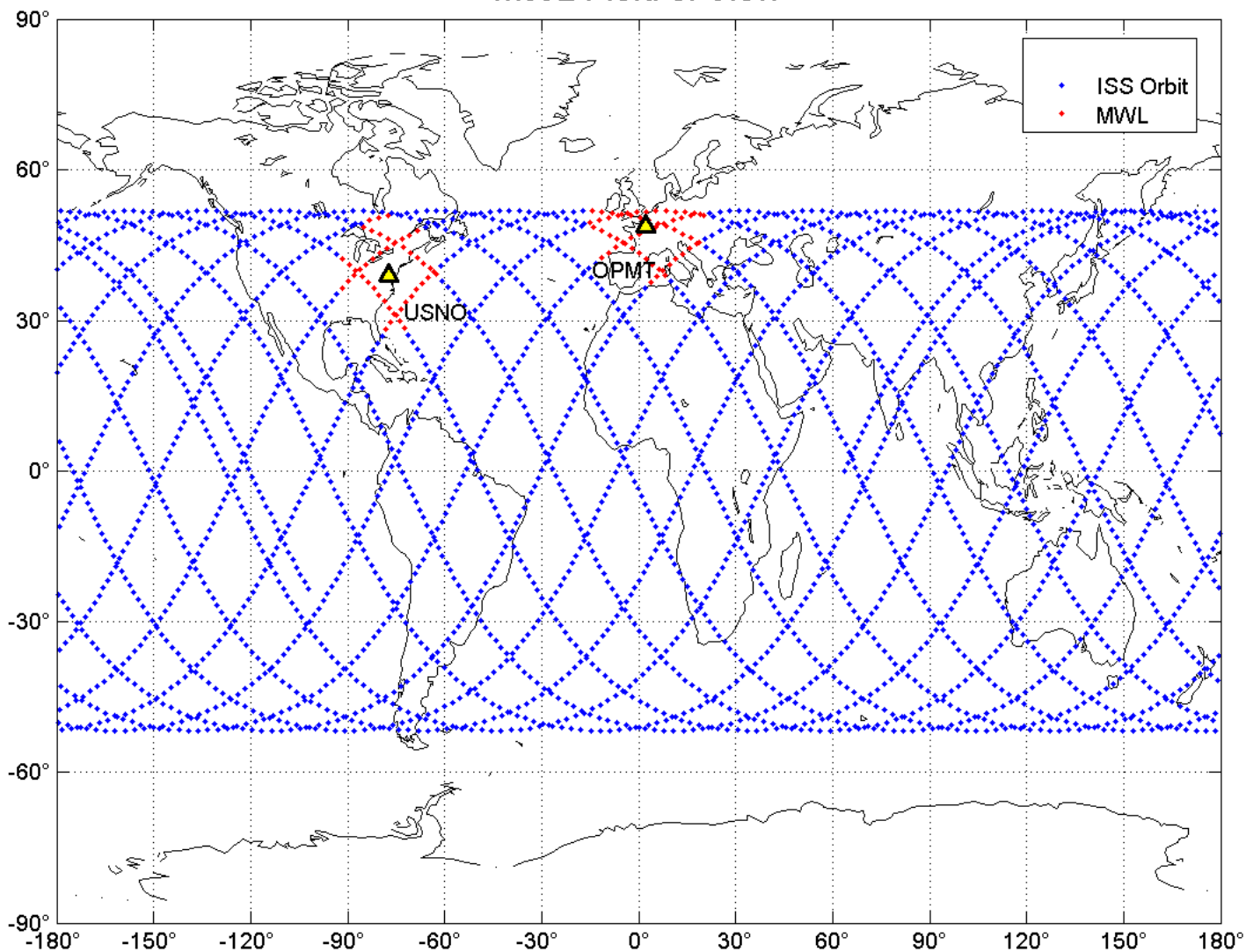
L1, E5a $\sigma(L1)=\sigma(E5a)= 3$ mm

ACES MWL observables: (simulated as biased range)

Ku (13.475Ghz), Ku (14.70333Ghz), $\sigma(Ku)= 0.3$ mm

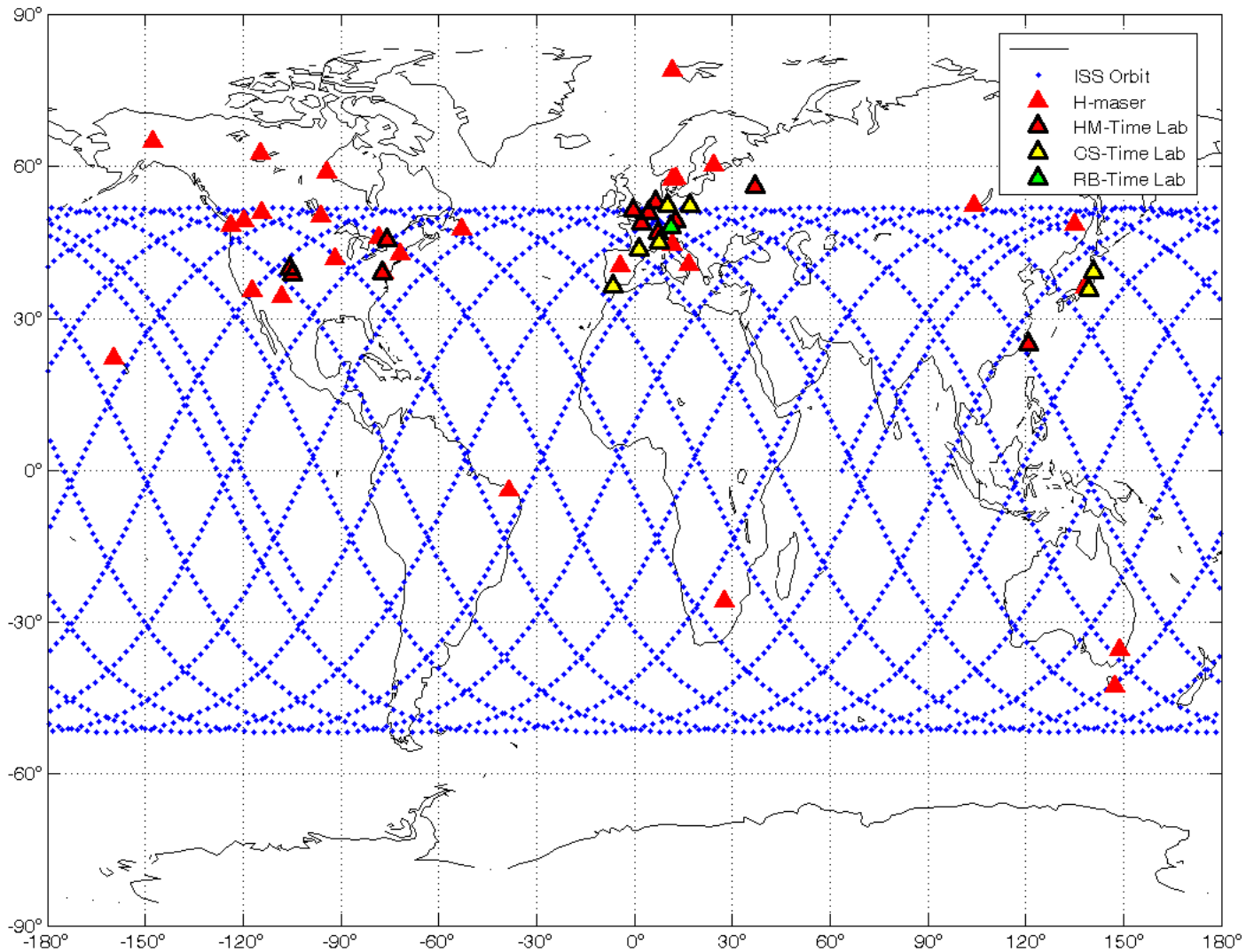
ACES MWL

MWL Field of View



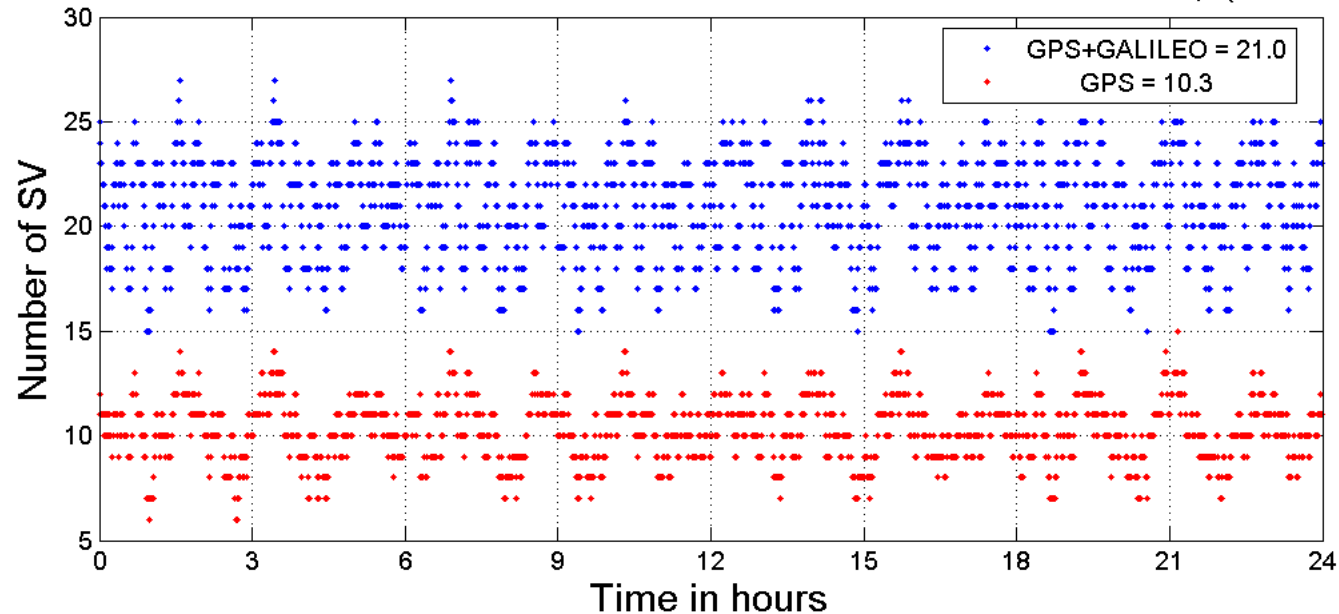
ACES and IGS clocks

H-masers and Time Labs in the IGS Network

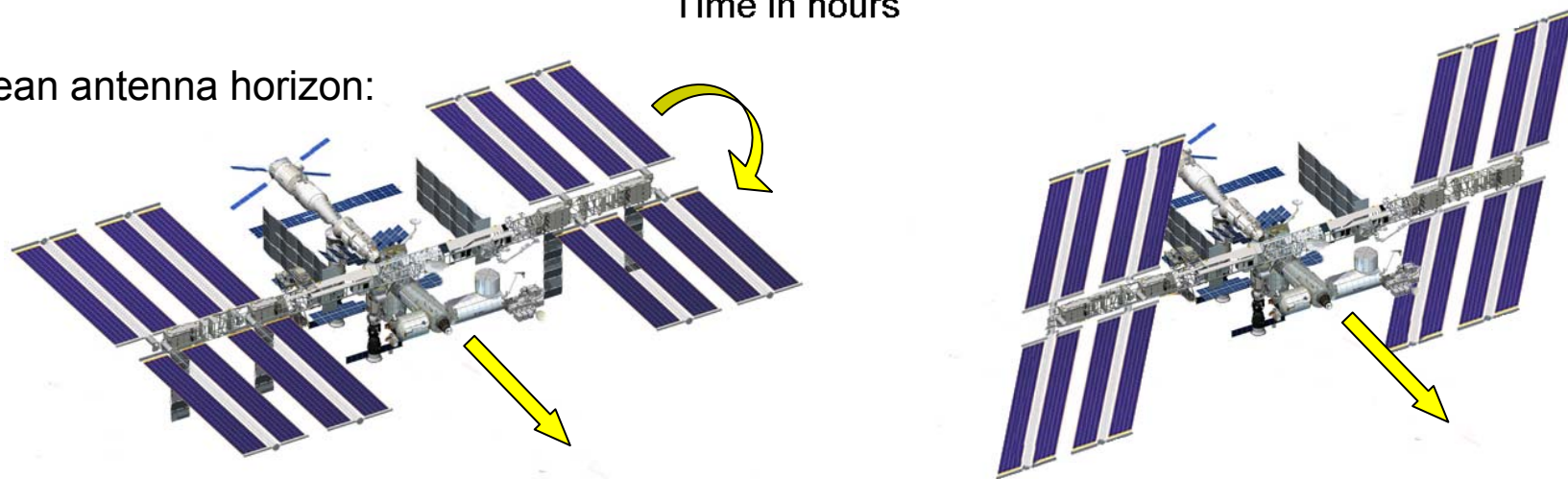


GPS and GALILEO on board Space Station

Number of visible GPS & GALILEO satellites from the ISS, (0° cut-off)

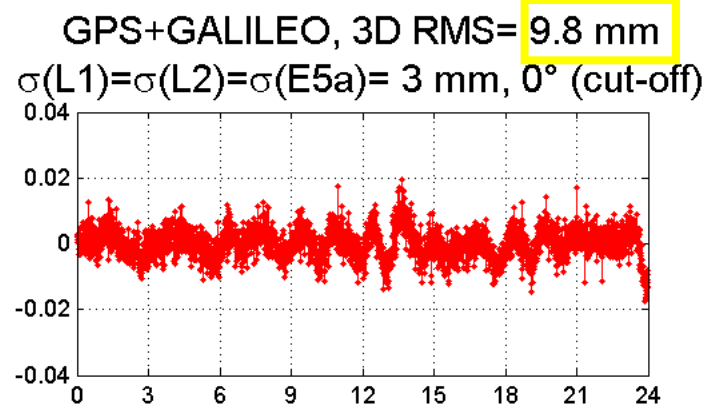
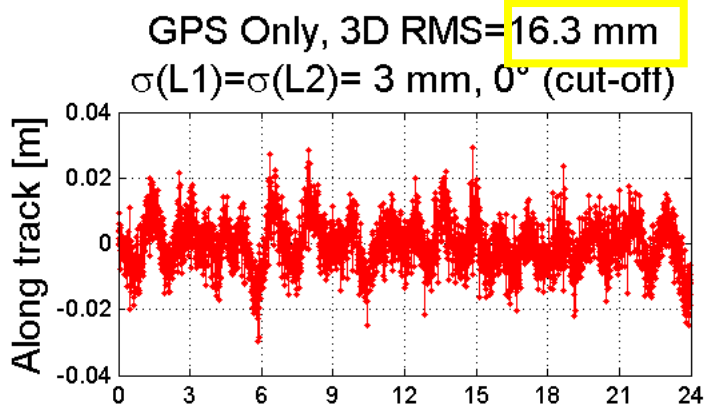


Clean antenna horizon:

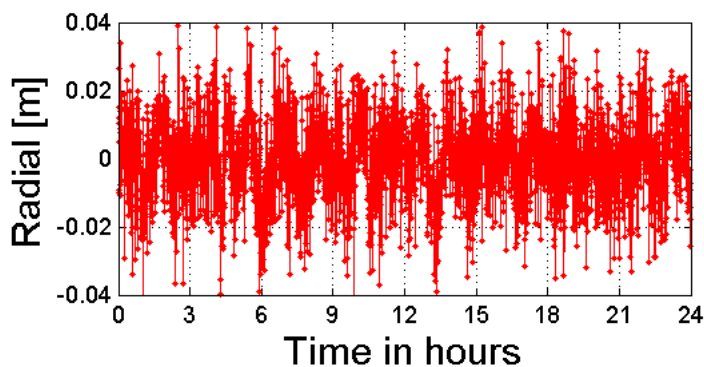
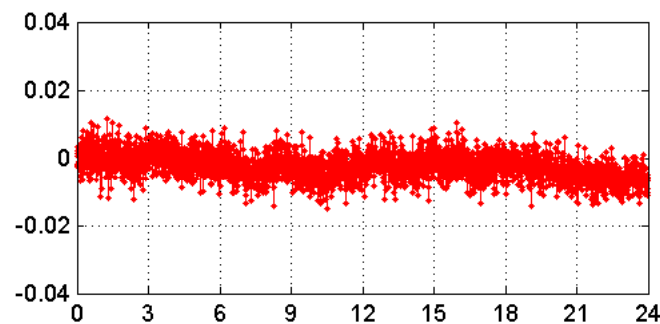
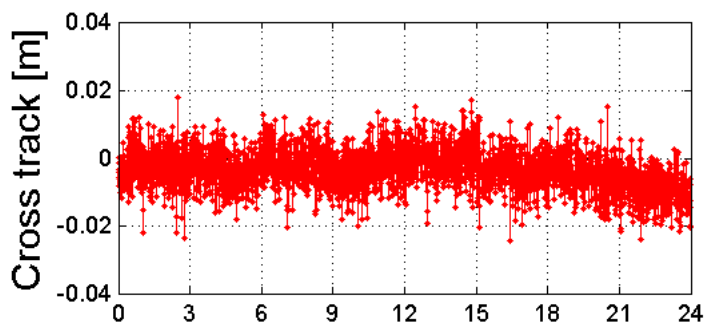


rotation of solar panels: 360° per orbit (ca. 90 min)

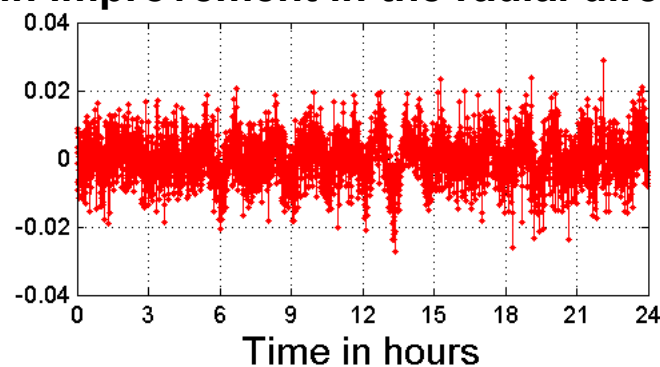
GALILEO+GPS: Kinematic POD for Space Station



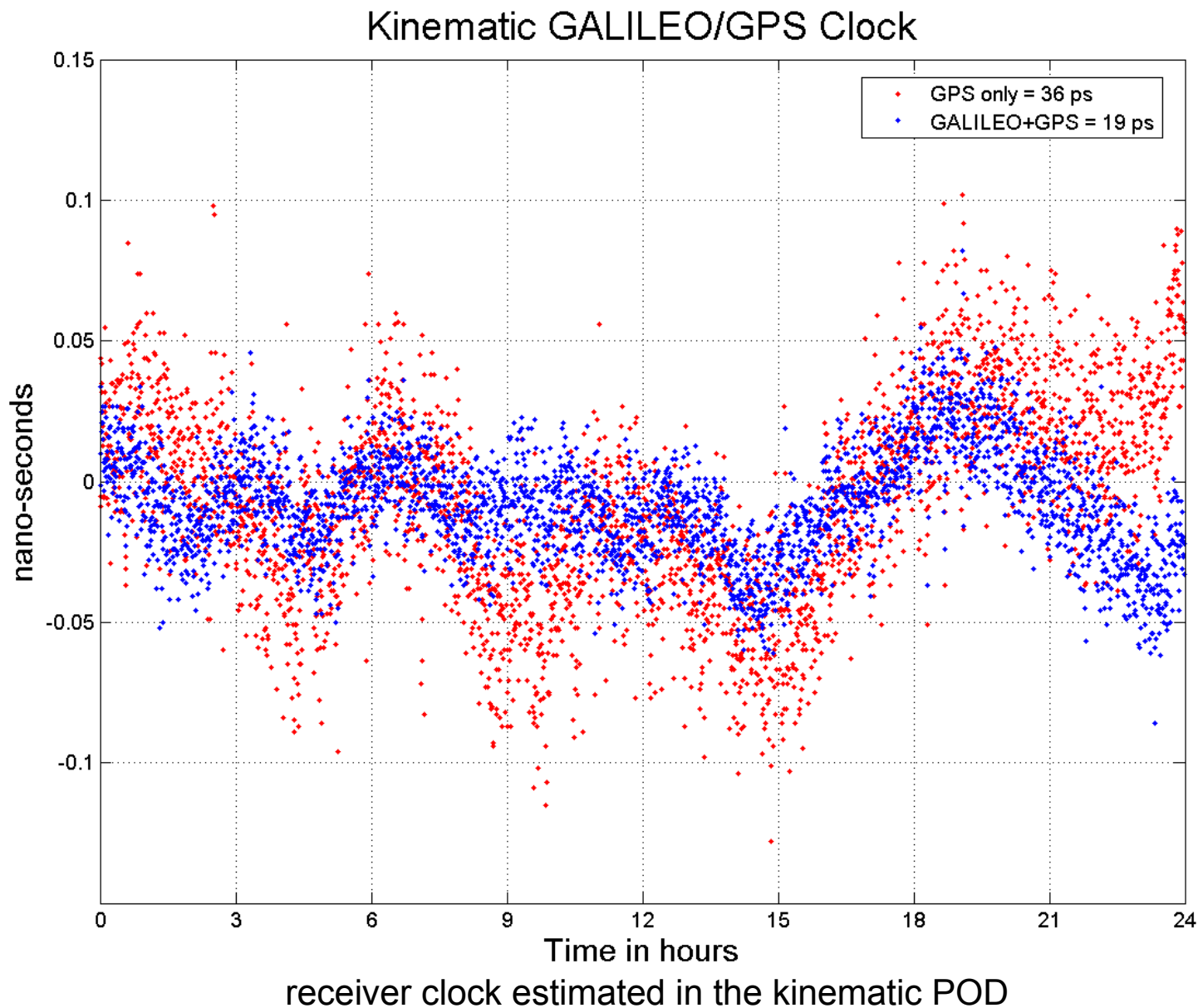
improvement
2.5x



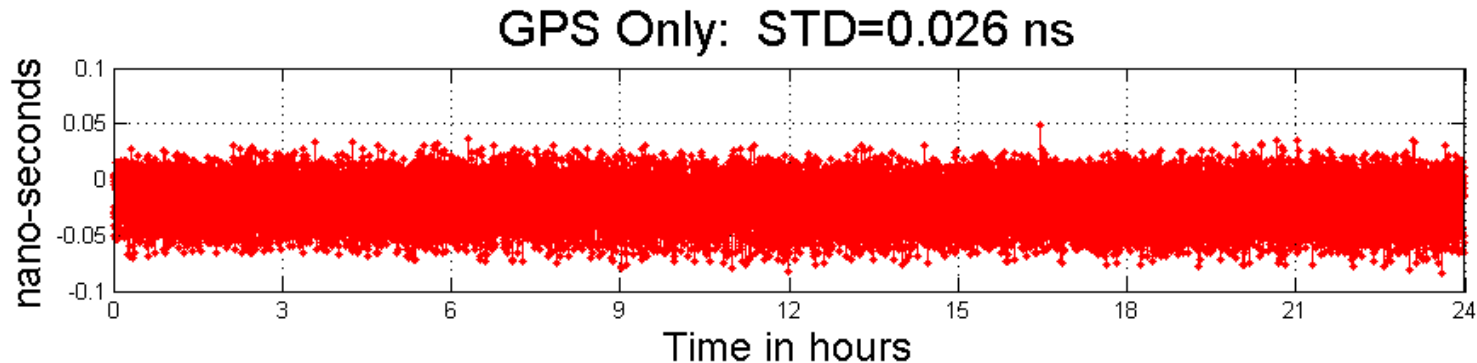
main improvement in the radial direction (height)



GALILEO+GPS: Kinematic POD for Space Station



Combined GPS/GALILEO/MWL frequency transfer (MWL simulated as biased phase)



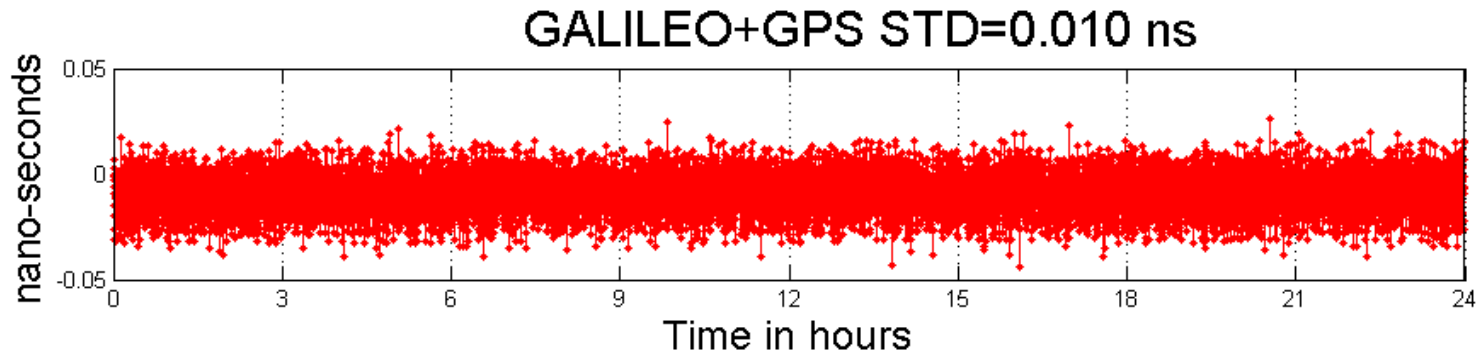
GPS observables:

L1, L2 $\sigma(L1)=\sigma(L2)= 3 \text{ mm}$ $\rightarrow L3 \approx 9 \text{ mm}$

GALILEO observables:

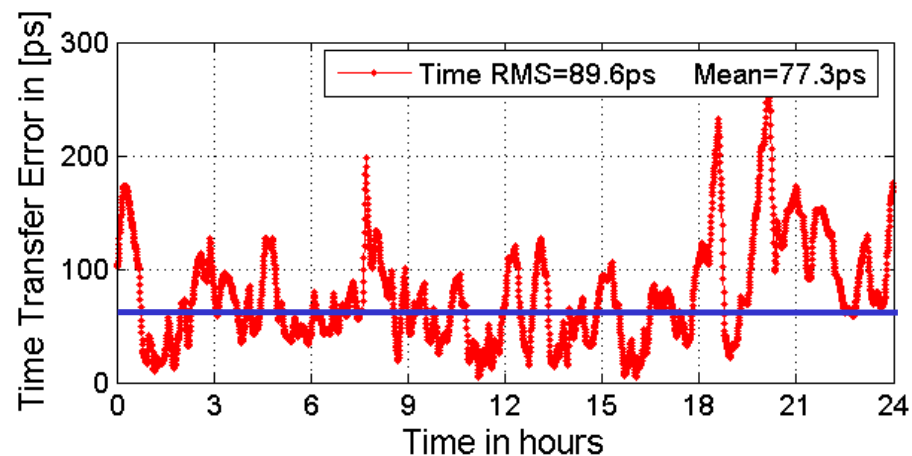
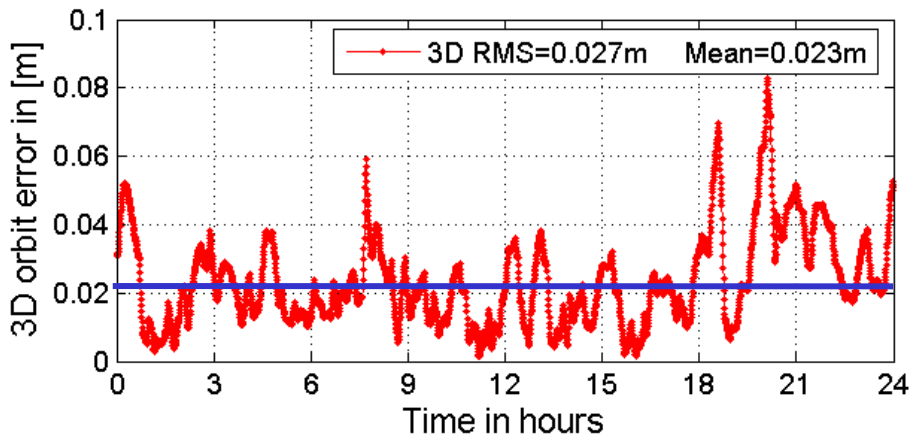
L1, E5a $\sigma(L1)=\sigma(E5a)= 3 \text{ mm}$ $\rightarrow L3 \approx 9 \text{ mm}$

improvement
2.5x

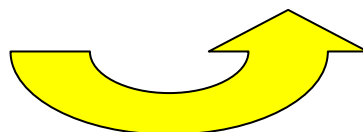


Orbit Accuracy and Time Transfer - GRACE

Orbit Error vs. Time Transfer Error

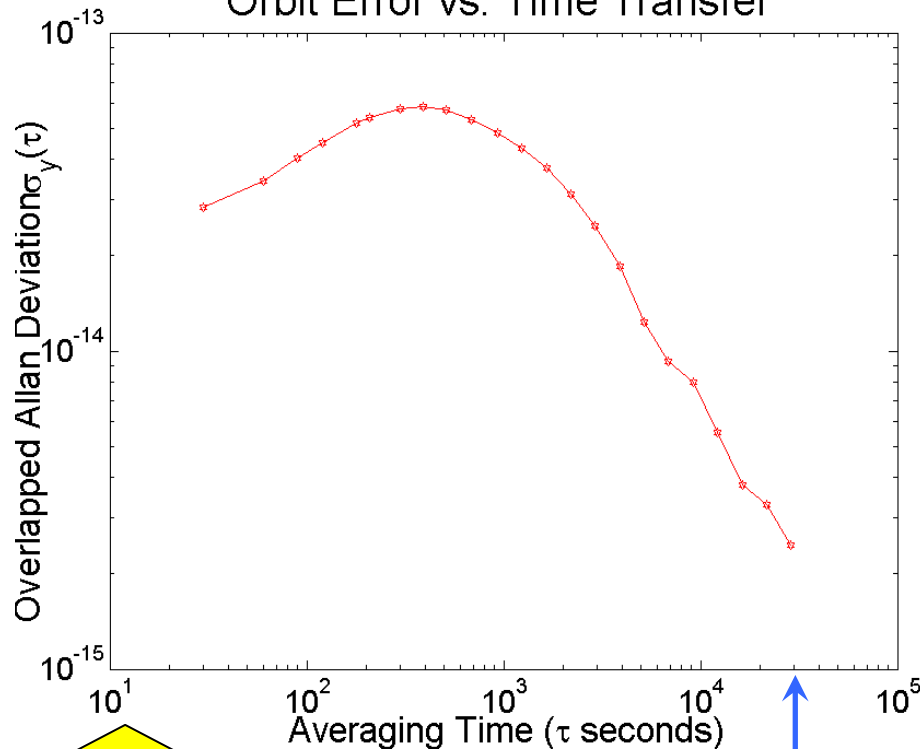


1cm \approx 33 ps



Allan deviation computed using the program CANVAS

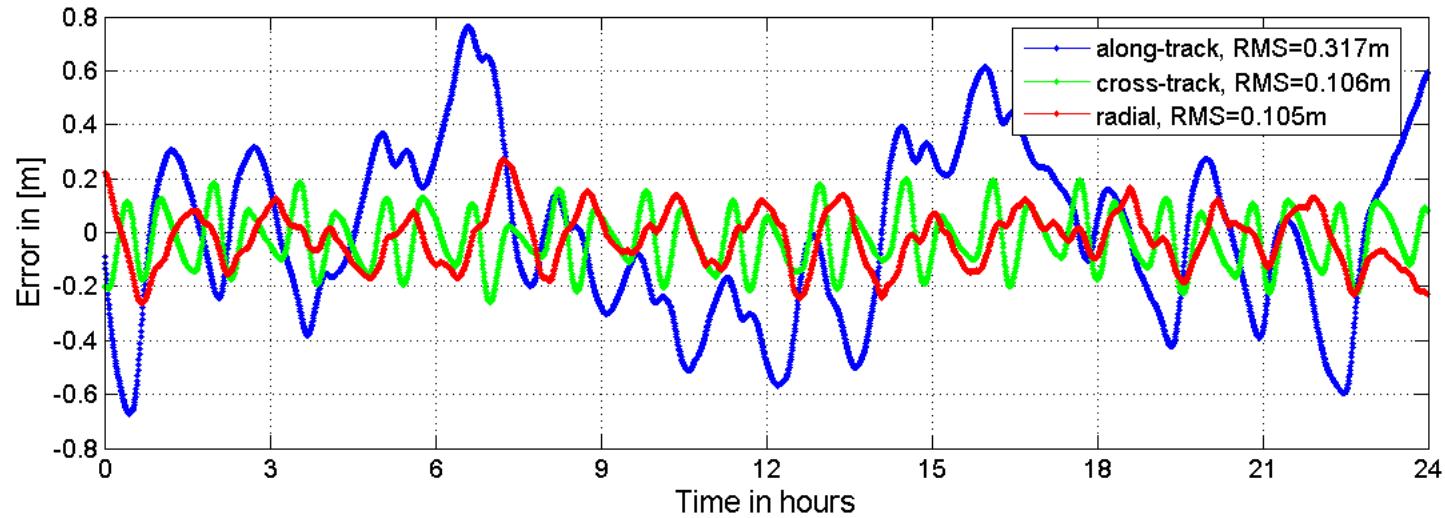
Orbit Error vs. Time Transfer



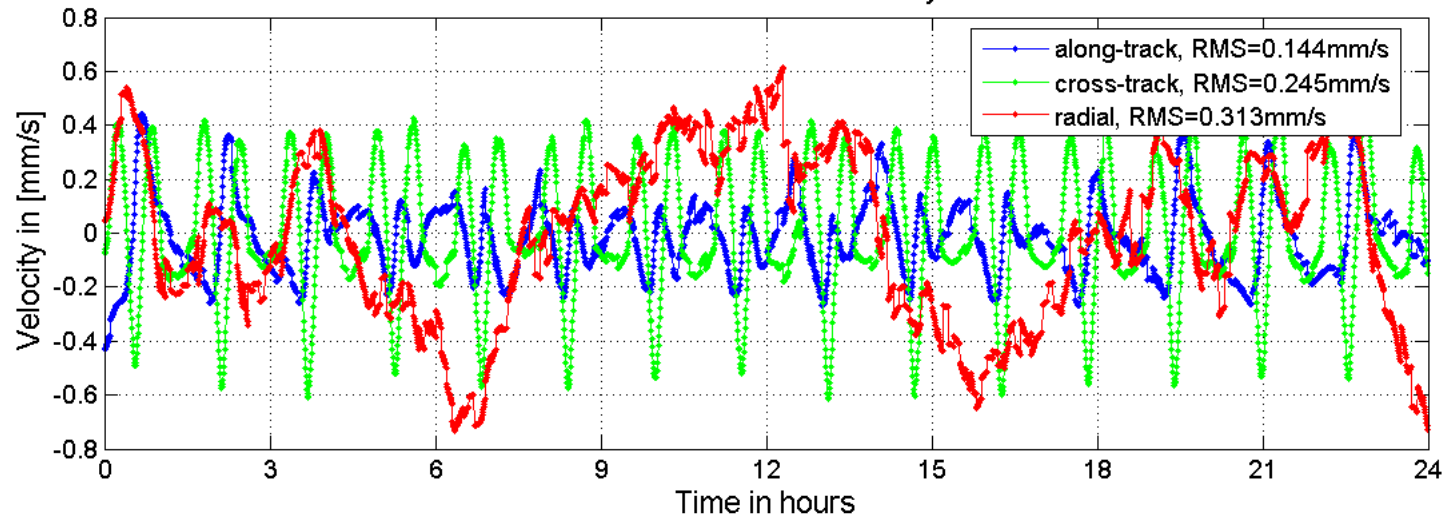
8 hours \approx 10^{-15}

Orbit Error and Frequency Shift

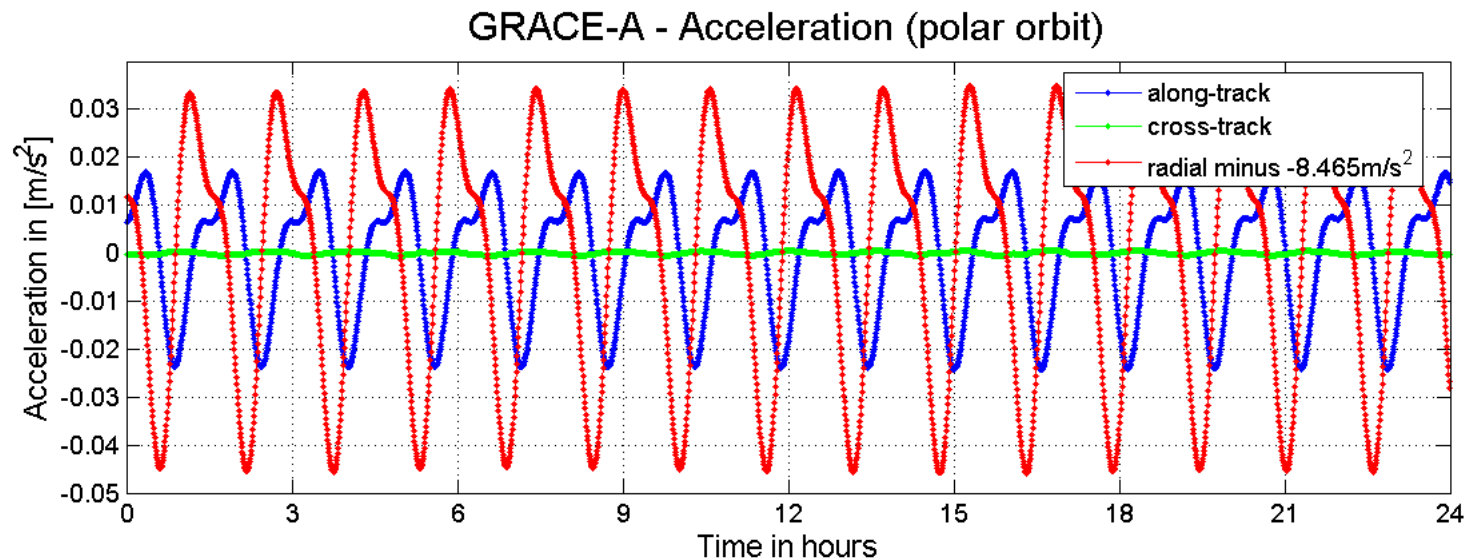
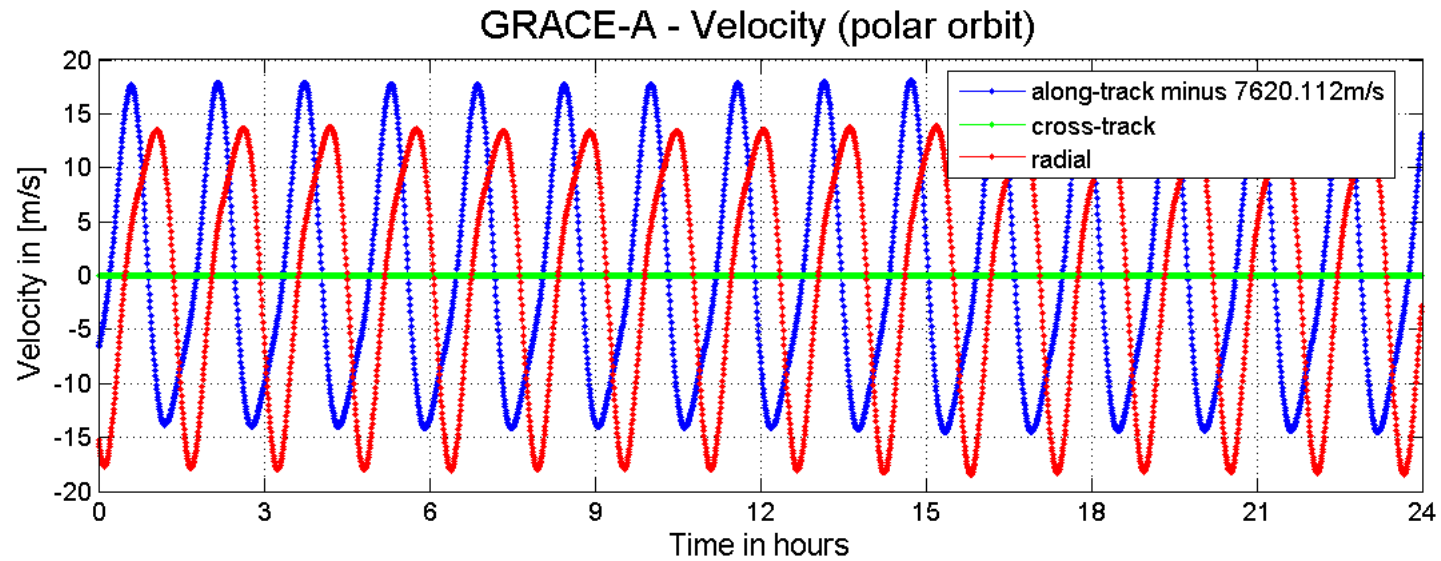
Orbit Error - Position



Orbit Error - Velocity

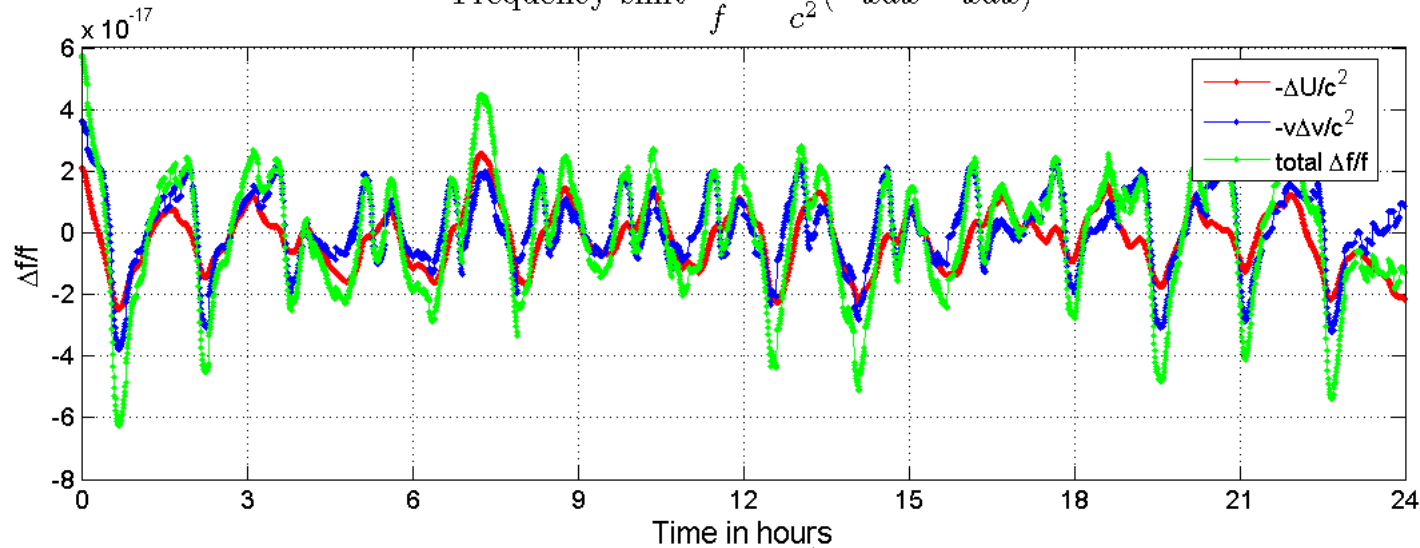


Orbit Error and Frequency Shift

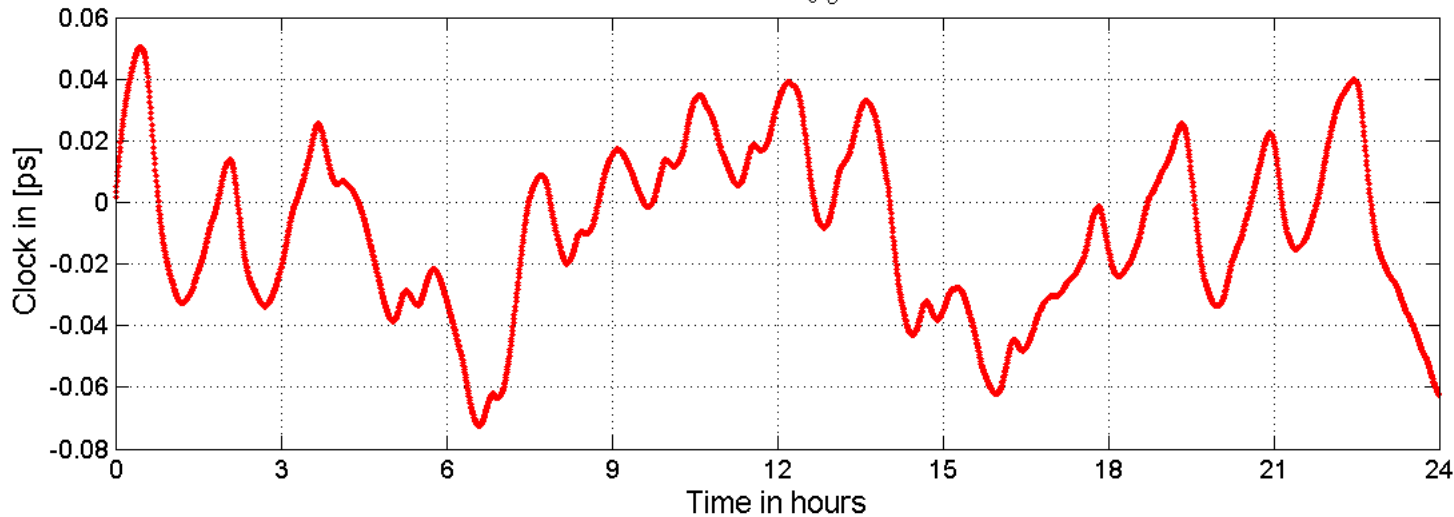


Orbit Error and Frequency Shift

$$\text{Frequency shift } \frac{df}{f} = \frac{1}{c^2}(-\ddot{\vec{x}}d\vec{x} - \dot{\vec{x}}d\dot{\vec{x}})$$



$$\text{Accumulated clock } \frac{1}{c^2} \int_0^t (-\ddot{\vec{x}}d\vec{x} - \dot{\vec{x}}d\dot{\vec{x}}) dt$$

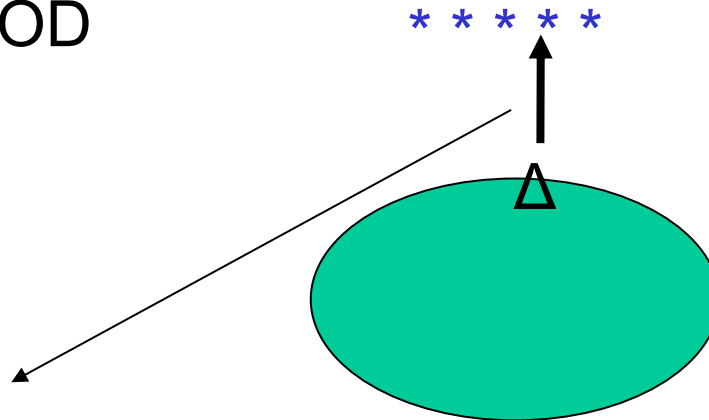


LEO Constellation + ACES for Space Geodesy

* * * * *

GPS&GALILEO
satellites

altitude above 1000 km
 \approx 1cm-POD



LEO Constellation+ACES
IGS Station

Link with following techniques:
GPS+SLR+DORIS+MWL+VLBI

ESA Topical Team on ACES POD and Geodesy

Objectives:

- POD for ACES
- Time and frequency transfer
- Relativistic Geodesy (gravity from clocks)

Gravitational frequency shift $\Delta f/f = \Delta W/c^2$ $10^{-16} \approx 1$ m